

# **Class 13: The IMF: Observations**

**ASTR 4008 / 8008, Semester 2, 2020**

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# Outline

- General considerations: resolved vs. unresolved, field vs. cluster
- Resolved populations
  - The IMF in the field
  - The IMF in star clusters
  - The most massive clusters
- Unresolved populations
  - $H\alpha$ -based methods for star-forming galaxies
  - Spectral feature methods for passive galaxies
  - M/L methods for passive galaxies

# General considerations

- Massive stars have very short lifetimes. Implications:
  - Can only study massive part of the IMF in young regions
  - Can be hard to study the low-mass part of the IMF in these regions —worse statistics, and usually not on the main sequence yet
  - As a result, studies of low-mass and high-mass parts of the IMF often done separately, in different regions and with different methods
- Individual stars are only resolvable out to  $\sim$ M31 distances. Within this distance, star-forming environment properties cover the range:
  - Metallicity  $Z/Z_{\odot} \sim 0.2$  (SMC) to 2 (MW centre)
  - Gas surface density (at kpc scales)  $\sim 0.1$  (SMC) to 300 (MW centre)  $M_{\odot} \text{ pc}^{-2}$
  - Relatively large dwarfs (SMC) through medium spirals (MW, M31)
  - NO mergers, starbursts, ULIRGs, wimpy dwarfs, very metal poor systems — these can ONLY be studied using unresolved stellar populations

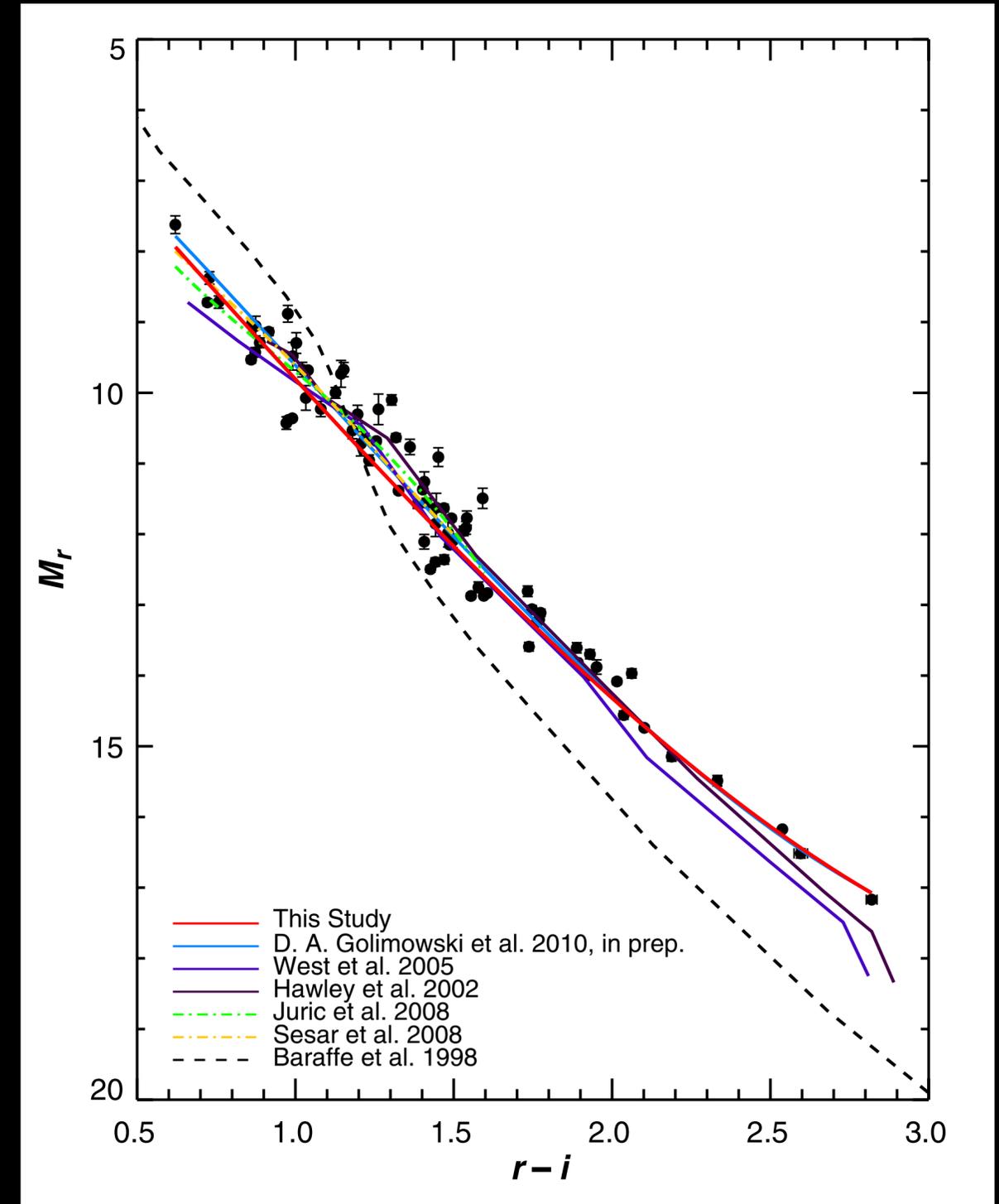
# The IMF in the Galactic Field

- For stars with mass low enough that lifetime  $\approx$  10 Gyr age of the Galaxy (mass  $\lesssim 1 M_{\odot}$ ), best statistics come from using whole galactic field — samples of  $>10^6$  possible
- Spectroscopy of large samples is expensive, particularly for dim targets, so biggest samples are photometric only
- Basic steps in a field IMF measurement
  - Measure apparent luminosity function (LF) and colour distribution
  - Use distance estimates / colours to convert to intrinsic LF
  - Correct for biases (extinction, Malmquist, metallicity)
  - Correct for unresolved binaries
  - Convert corrected LF to mass distribution

# LFs and distances

## Sources and methods

- Apparent LFs are relatively easy to obtain from large sky surveys (e.g. SDSS)
- Distances are bigger challenge:
  - Pre-*Gaia*, parallax distances only available for bright, nearby stars → studies used CMD for sample with parallax distances to convert colour to absolute magnitude for all other stars
  - Post-*Gaia*, parallax sample  $\sim 10^5$ , can get distances directly (though still smaller sample than colour-based studies)



Colour-magnitude diagram for stars with parallax distances (c. 2010 data) — Bochanski+ 2010

# Bias mitigation

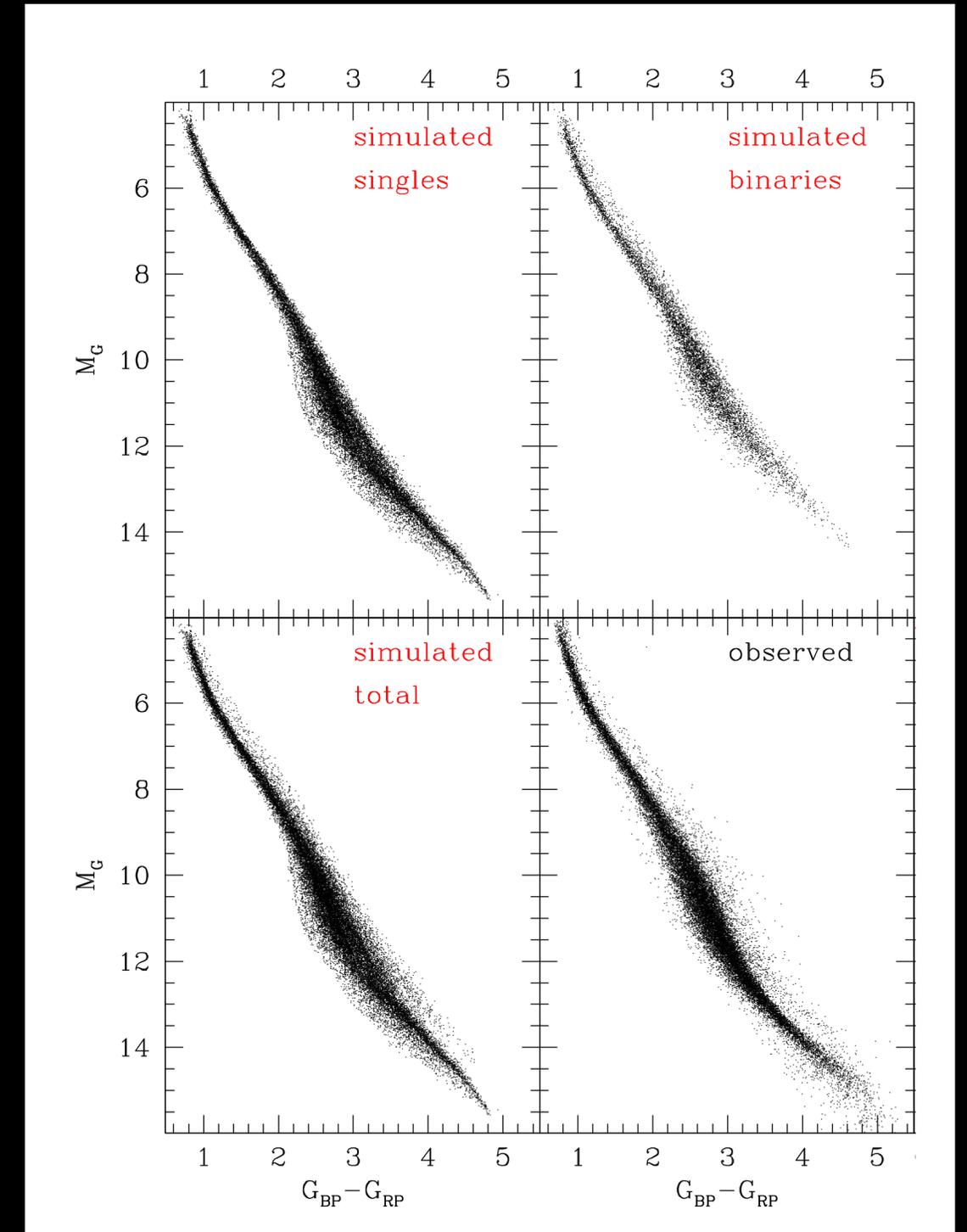
## For both photometric and parallax studies

- Extinction bias: distant objects are both reddened and dimmed, so stars assigned artificially low luminosities → mass is underestimated
- Malmquist bias: near magnitude limit of sample, errors are asymmetric: stars more likely to be kept if error is positive (makes star look brighter) than negative (makes star look dimmer) → mass on average overestimated
- Metallicity bias (for photometric method): empirical CMD used to assign luminosities is based on nearby stars, which have higher mean metallicity than full sample (since metal-poor stars more common at large scale height) → metal-poor stars are bluer, so magnitude assigned is too bright, mass is overestimated

# Binarity correction

## The biggest bias of all

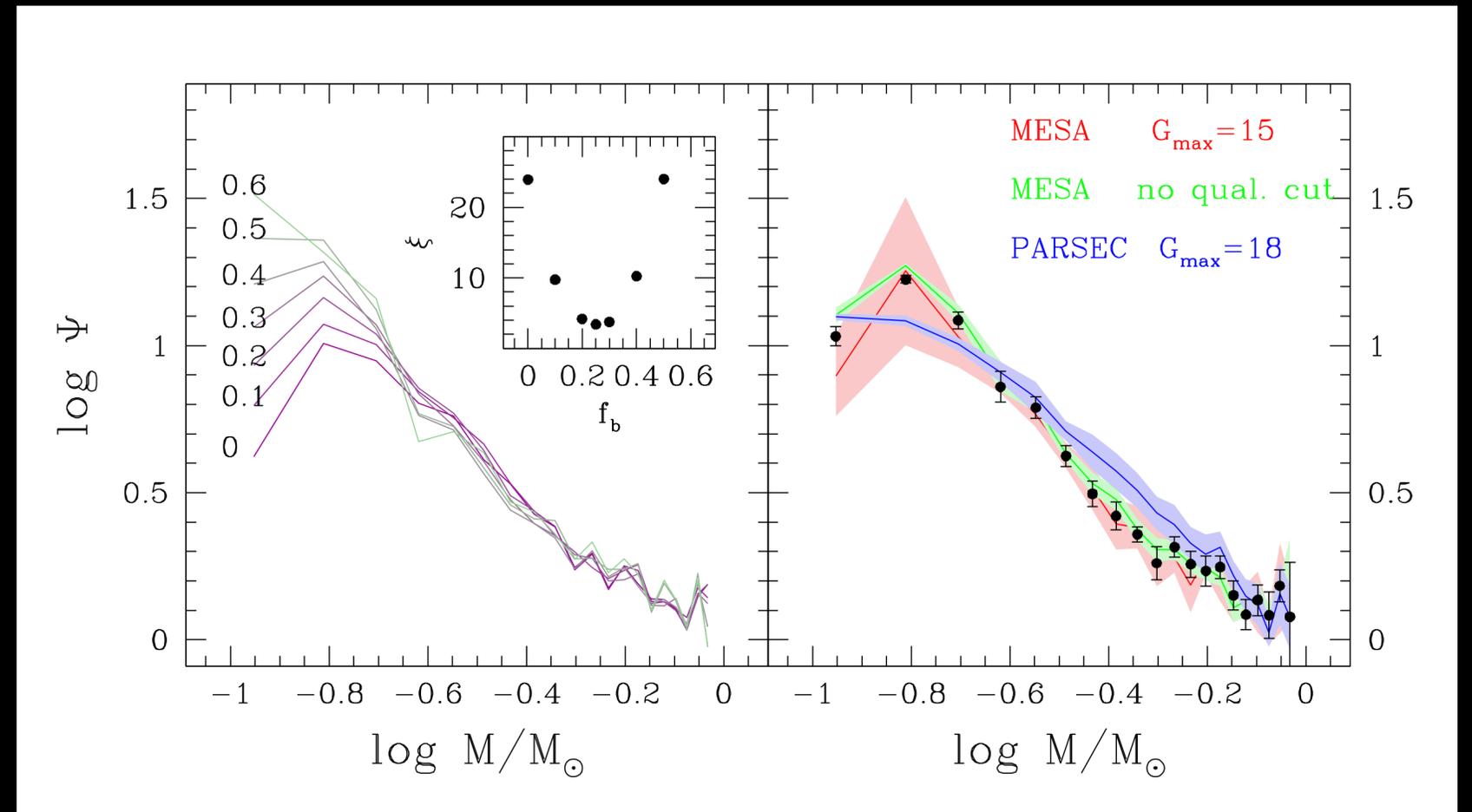
- Some fraction of stars are unresolved binaries
- Complex effects; depends on mass ratio  $q$ :
  - If  $q \lesssim 0.3$ , primary much brighter, secondary not seen at all  $\rightarrow$  properties of primary recovered correctly, but secondary missed
  - If  $q \approx 1$ , colour unaffected, but true luminosity =  $2 \times$  value of single star  $\rightarrow$  error in distance or mass, depending on how luminosity is used
- Must be modelled based on *a priori* knowledge of binary fraction, mass ratio distribution



Simulated CMD including the effects of binaries, being matched to observed CMD from *Gaia* (Sollima 2019)

# From luminosity to mass functions

- Convert corrected LF to mass function using empirical or theoretical mass-magnitude relation (MMR)
- Empirical MMRs come from binary star dynamical mass measurements; also subject to metallicity bias
- Theoretical MMRs uncertain, particularly for low-mass stars at red colours, where molecular opacities in stellar atmospheres are complex



Mass functions derived using different assumed unresolved binary fractions (left) three different theoretical MMRs (right) — Sollima 2019

# IMFs in young clusters

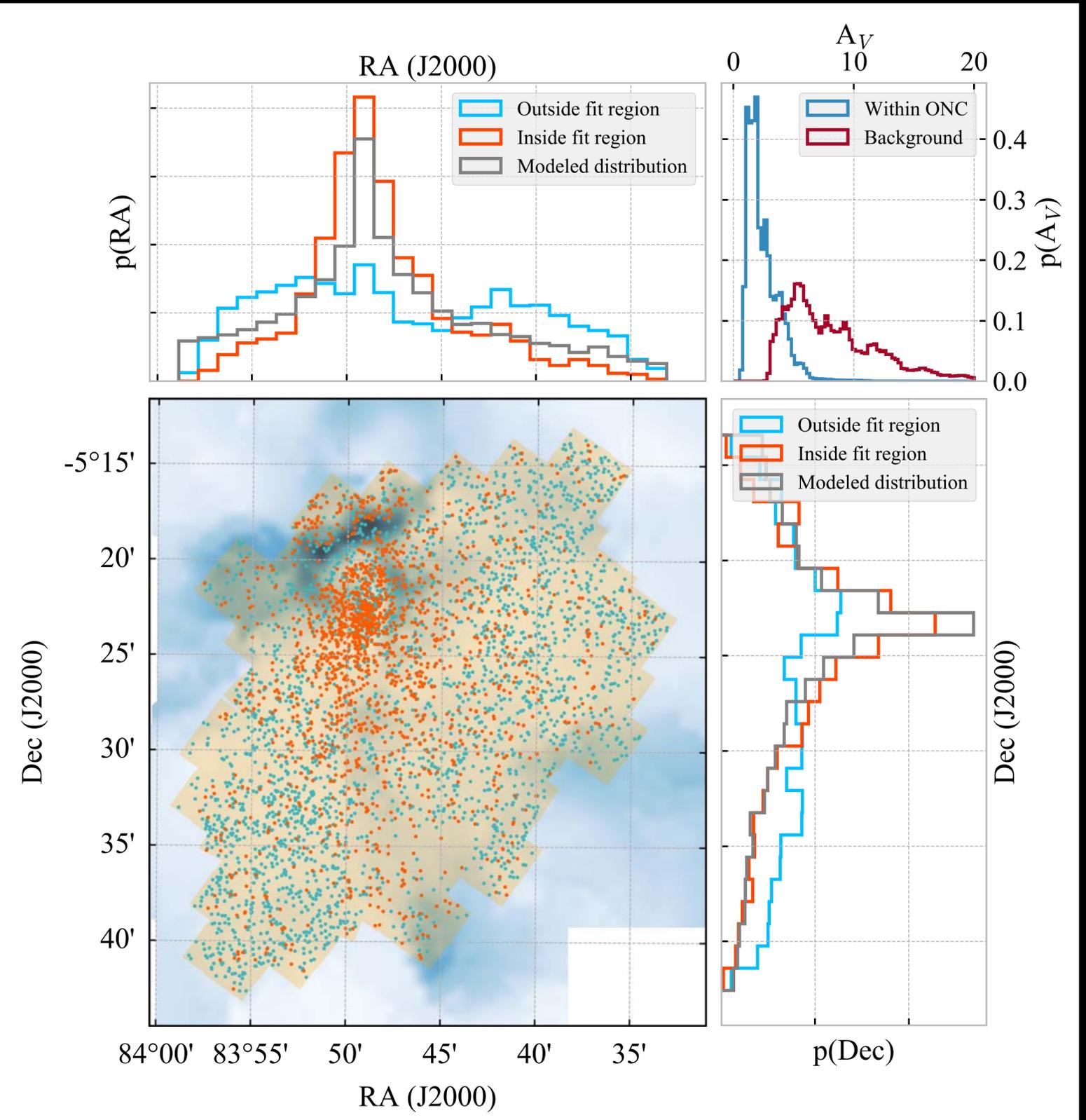
## General considerations

- Advantages:
  - Only way to probe IMF of stars  $\gtrsim$  few  $M_{\odot}$
  - Near-uniform metallicity, distance, foreground dust  $\rightarrow$  greatly reduced bias
  - Low-mass stars / brown dwarfs brighter when young, can go to lower mass
- Disadvantages:
  - Much worse statistics ( $\sim 10^3 - 10^4$  stars instead of  $\sim 10^5 - 10^6$ )
  - Low-mass stars will be pre-main sequence  $\rightarrow$  much more uncertain MMR
  - Need to separate cluster members from foreground / background objects
  - Differential extinction due to dust within the cluster
  - Dynamical ejections / mass segregation may be a concern

# Example: the ONC

## Best Galactic case

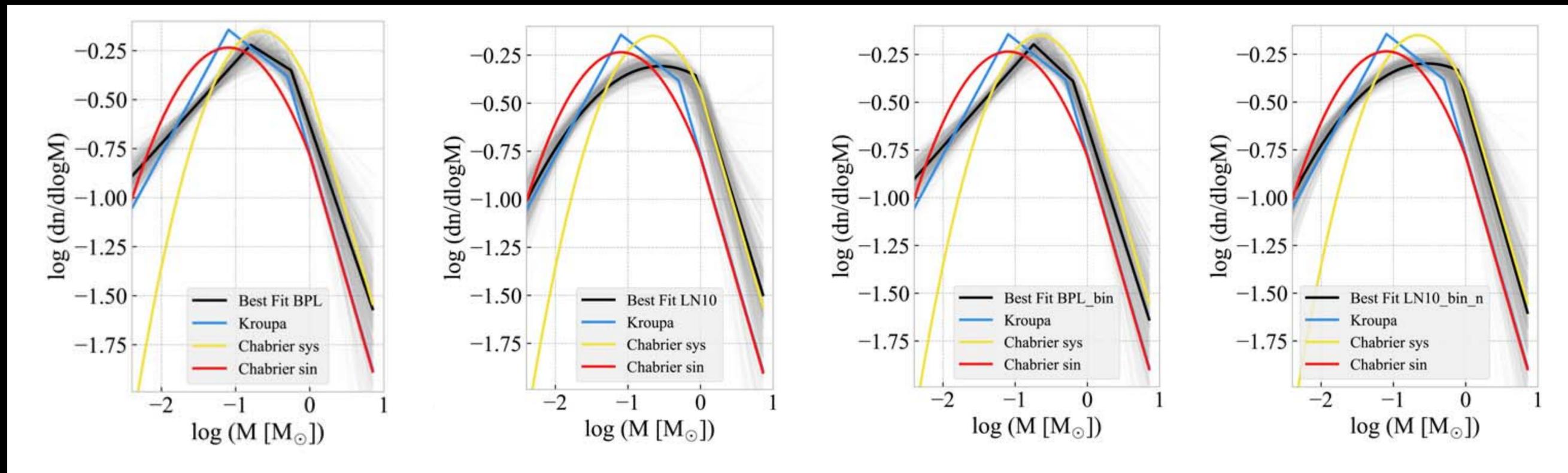
- LF in Orion Nebula Cluster (ONC) measured using HST down into the brown dwarf / planet regime
- $d = 400$  pc from parallax, extinction well-mapped
- Can separate background based on colours
- Age distribution roughly known — reduces MMR uncertainty



Blue dots = background objects, orange = ONC stars; background shading = dust extinction map; Gennaro & Roberto 2020

# ONC results

- ONC IMF roughly consistent, with errors, with measured field IMF
- Exact details depend on assumed age distribution, binary corrections
- Clearly detected turnover of  $\sim \text{few} \times 0.1 M_{\odot}$

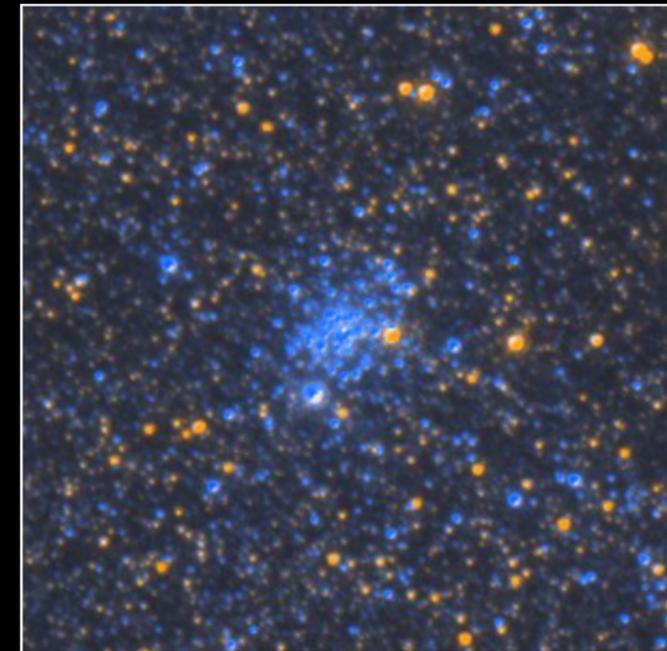


ONC IMFs for different assumed star formation histories and different functional forms — Gennaro & Robberto 2020

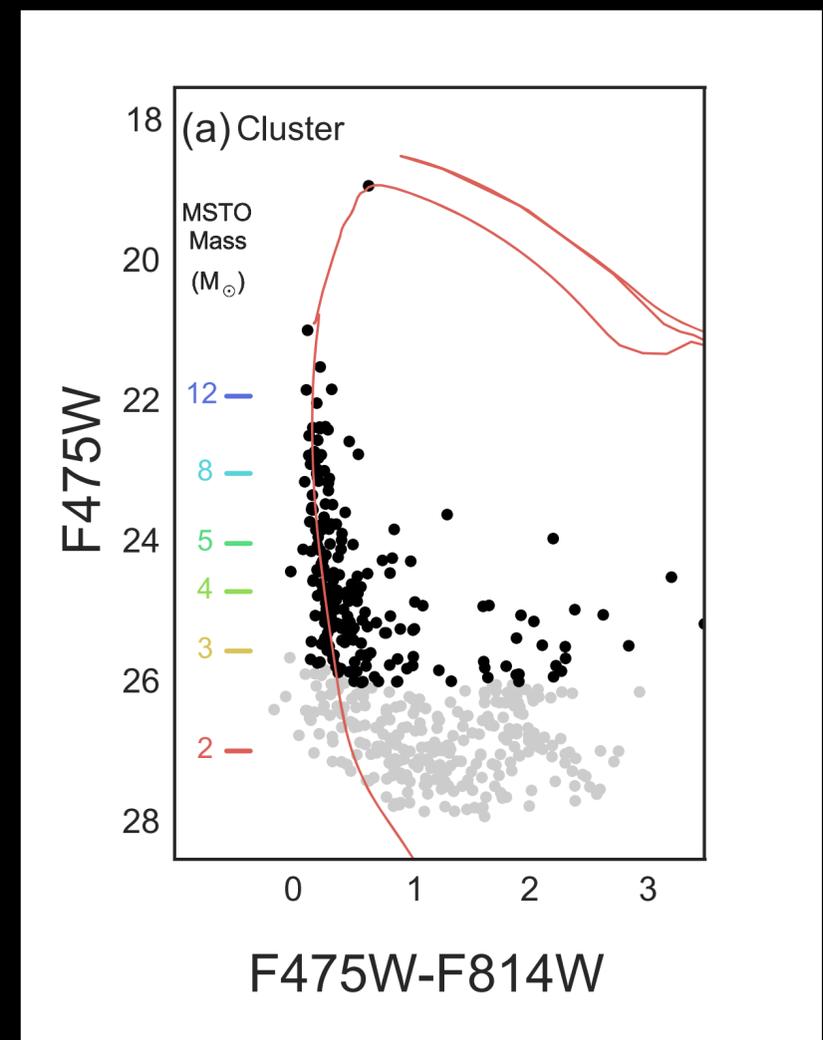
# Example: M31 / PHAT

## Best extragalactic case

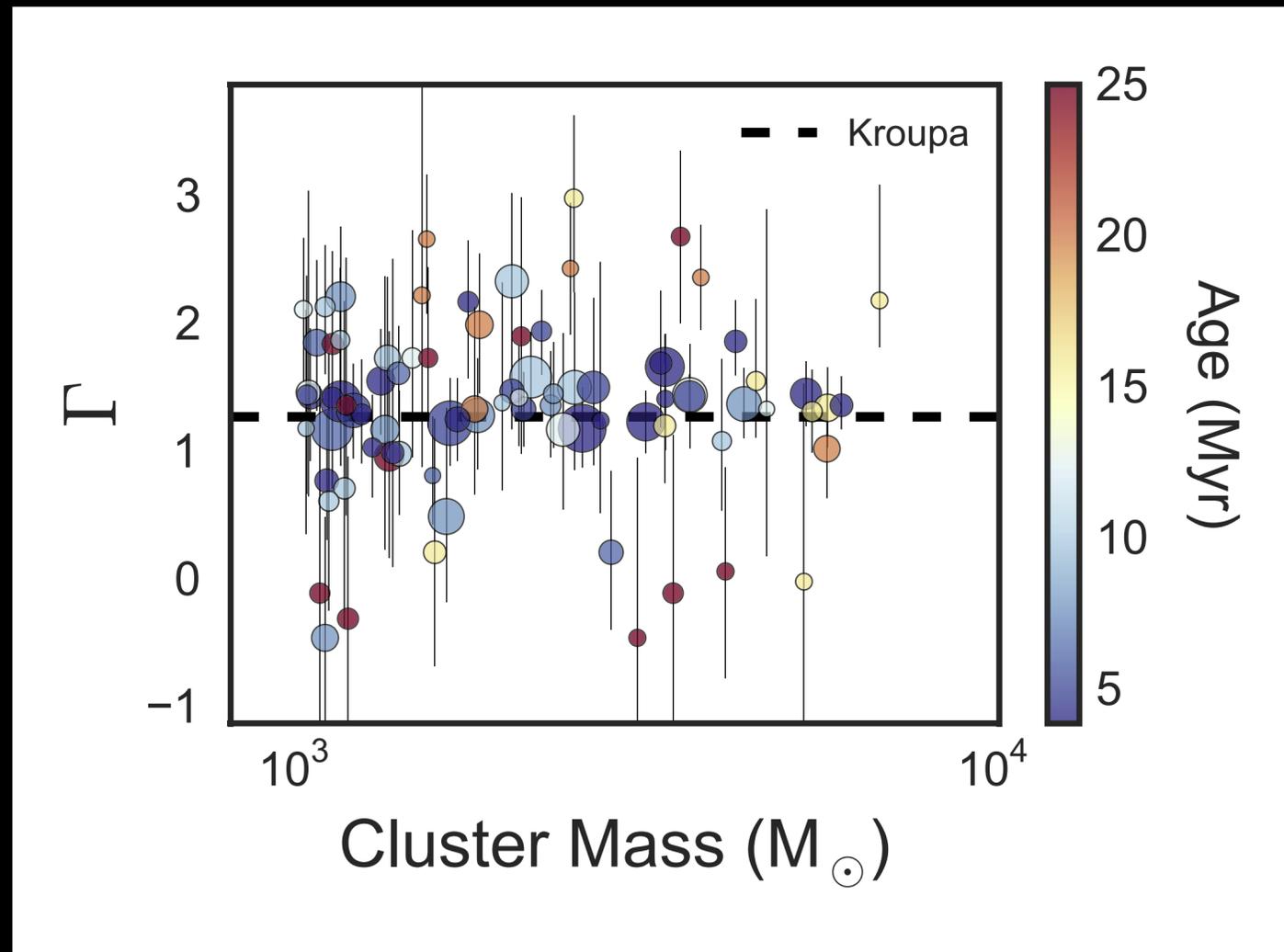
- In M31 using HST, can see individual stars down to  $\sim 2 - 3 M_{\odot}$  in  $\sim 100$  clusters 5 - 25 Myr old — probably best measurement of high mass IMF in resolved stars
- High mass slope in individual clusters has big uncertainties due to small number of stars, but large number of clusters provide strong constraint on IMF in galaxy as a whole
- No distance uncertainty, minimal extinction uncertainty



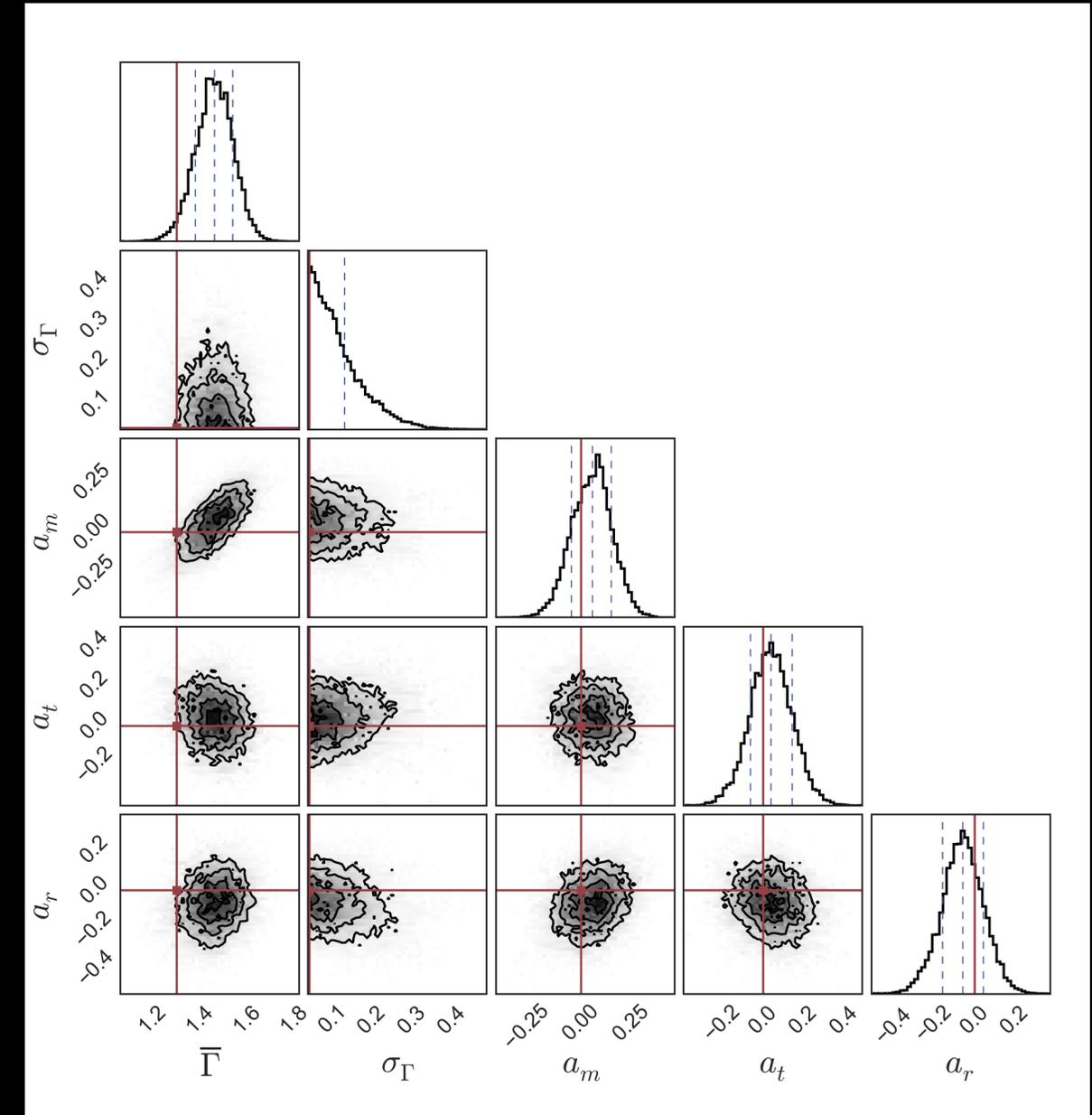
Weisz+  
2015



# PHAT result



High mass slopes  $\Gamma$  of individual clusters



Posterior PDF for mean high mass slope in galaxy  $\Gamma$ , cluster-to-cluster scatter in high mass slope  $\sigma_{\Gamma}$ , and scaling of slope with cluster mass, age, radius ( $a_m$ ,  $a_t$ ,  $a_r$ )

# Summary of resolved observations

## For most local star-forming environments

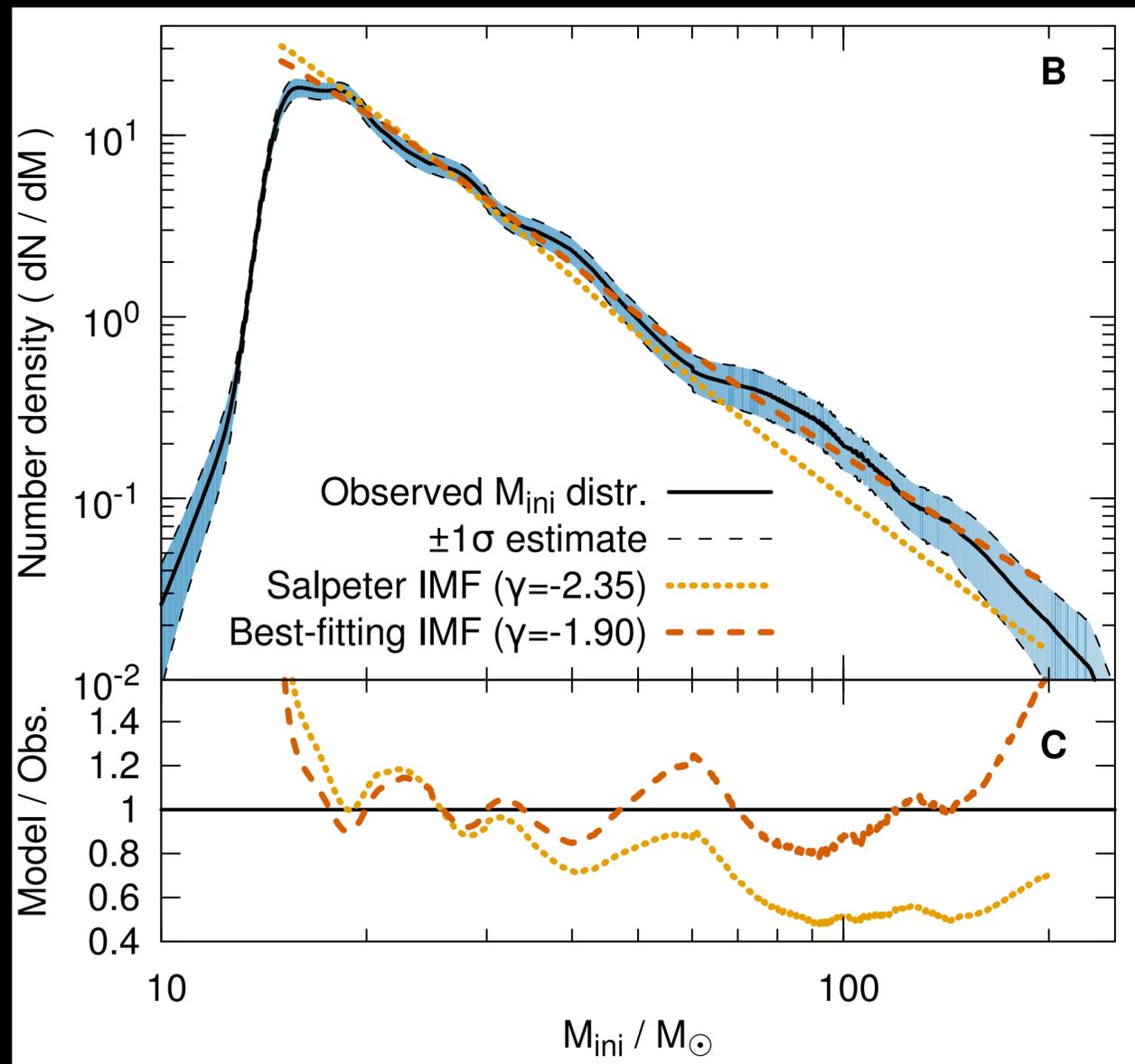
- Low-mass IMF in clusters similar to that inferred for the field — flattens to peak at  $\sim \text{few} \times 0.1 M_{\odot}$
- High mass IMF shows little scatter between clusters — slope similar to Salpeter value ( $dn / dm \sim m^{-2.3}$ ) with perhaps  $\sim 0.1$  dex variation
- No evidence for systematic variation in either peak or slope with environment (cluster mass or age, field vs. cluster) within the disc of the MW or M31
- Best evidence for a “universal” IMF

# The most massive clusters

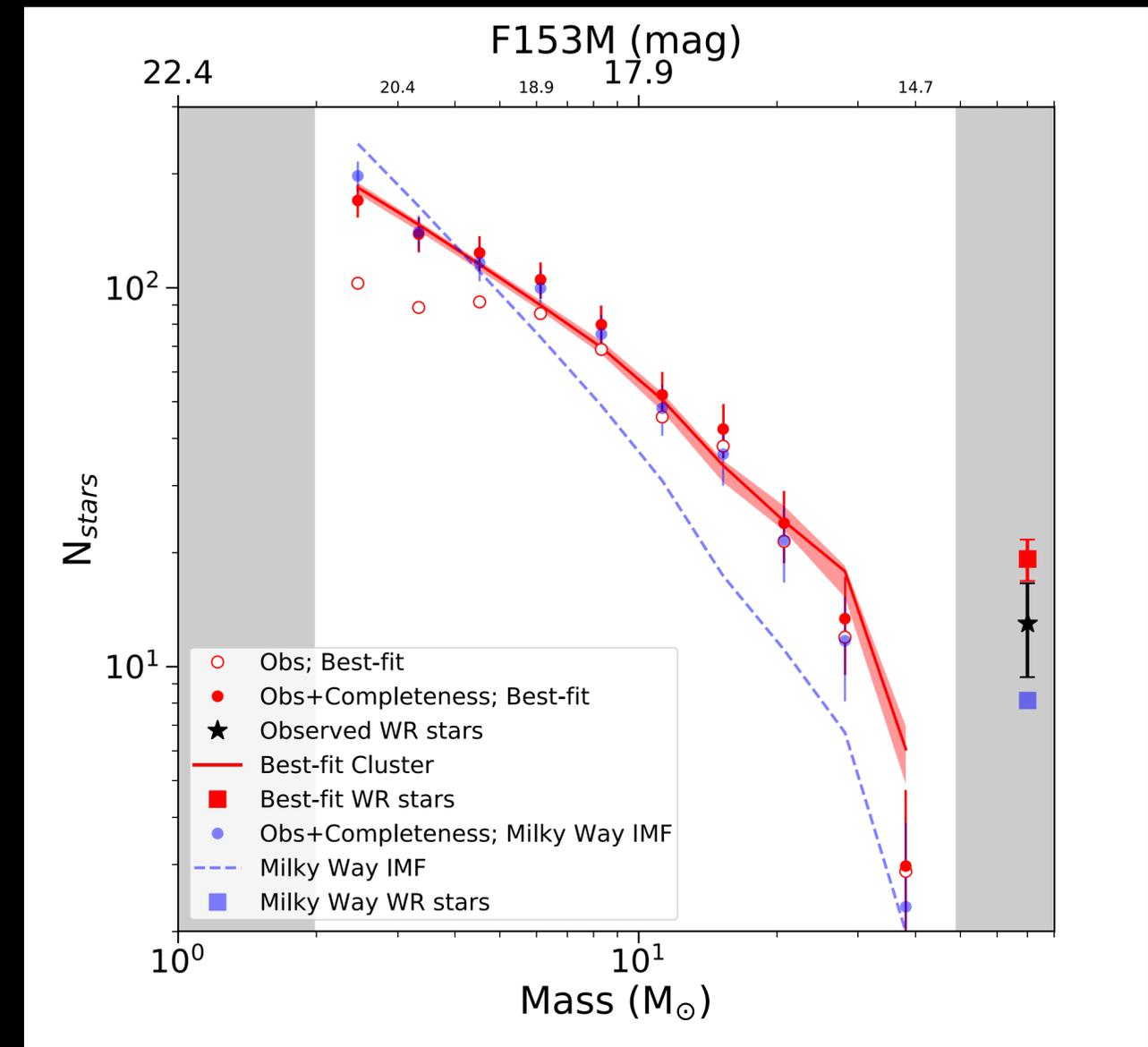
## Pushing toward a broader range of environment

- Most extreme environments available for resolved star IMFs are massive clusters near Galactic Centre in Milky Way (Arches, Quintuplet, Wd 1) and 30 Doradus cluster in LMC
- Characteristics: cluster mass  $> 10^5 M_{\odot}$ , density  $> 10^5$  stars  $\text{pc}^{-3}$
- Can only see relatively massive stars due to confusion
- Despite caveats: tentative evidence for slightly shallower slope

# IMFs in Arches and 30 Doradus



Schneider+ 2018



Hosek+ 2018

**Class exercise: what are some potential problems / biases that could potentially produce a shallower IMF measurement? That is, what should we be worried about before we trust these measurements?**

# Unresolved stellar populations

## General considerations

- IMF measurements for unresolved populations use spectral synthesis:

$$L_\nu = \int_0^\infty \dot{M}_*(t) \int_0^\infty \frac{dn}{dm} L_\nu(m, t) dm dt$$

- General problem is degeneracy between IMF and SF history — output light depends on both, so need a way to disentangle to constrain IMF
- Basic approaches:
  - Choose  $\nu$  where  $L_\nu \rightarrow 0$  at small  $t$ , so we can assume constant SFR
  - Use some proxy to calibrate out dependence on SF history
  - Choose systems where SFR has been 0 for a long time ( $\sim 10$  Gyr), so range of stellar ages  $t$  is small

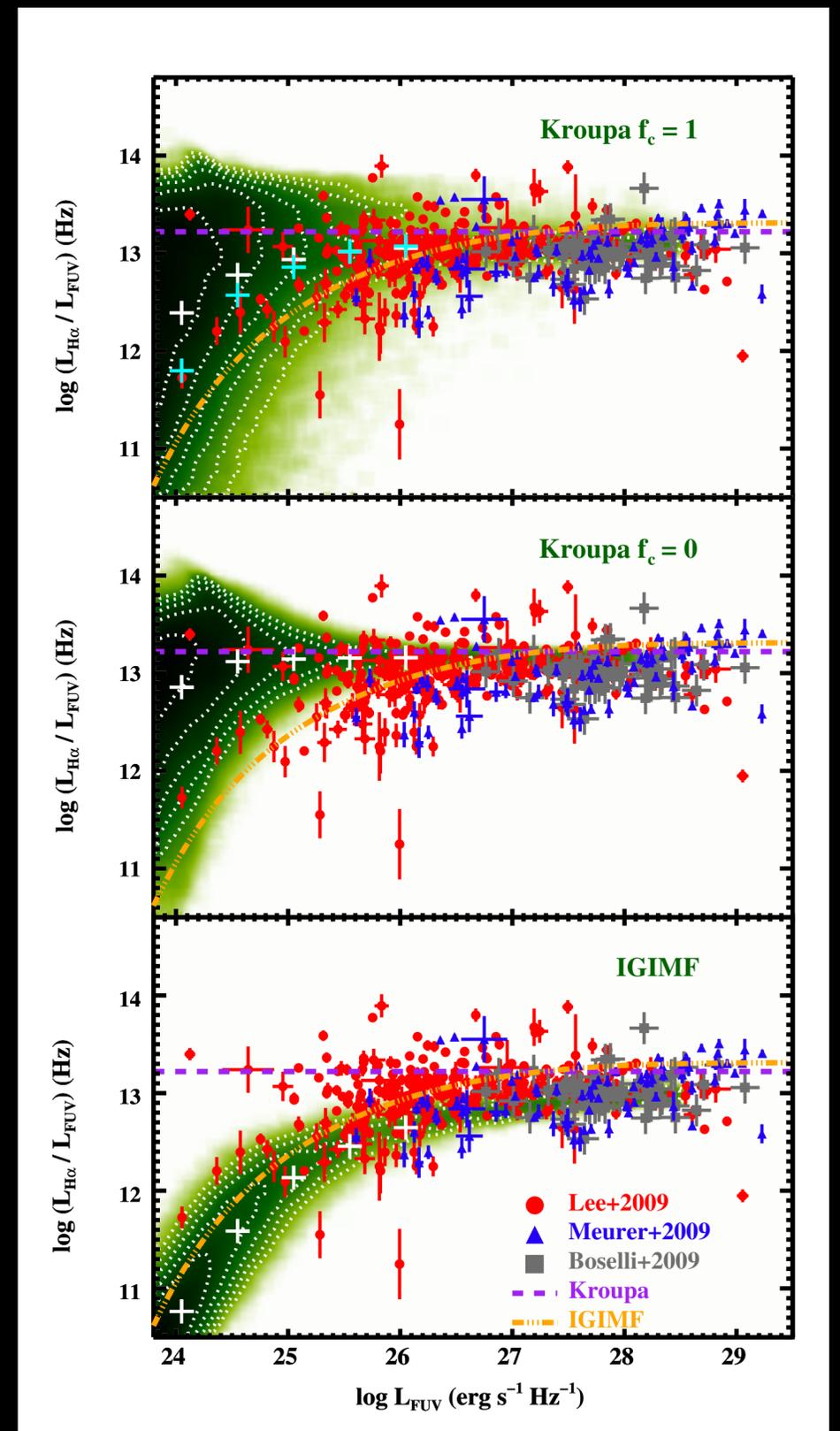
# H $\alpha$ -based methods

## Basic idea

- H $\alpha$  comes from recombination, and thus ultimately from ionising photons
- Ionising photons are predominantly produced by the most massive stars in the IMF — for a Chabrier IMF at zero age, half of ionising photons come from stars  $> 50 - 60 M_{\odot}$
- Ratio of ionising photons to tracers of lower mass stars is sensitive to the IMF
- Timescale of H $\alpha$  emission is short —  $\sim 5$  Myr
- Main challenge is the tracer to which to compare H $\alpha$ , since tracers of lower mass star usually integrate over longer timescale

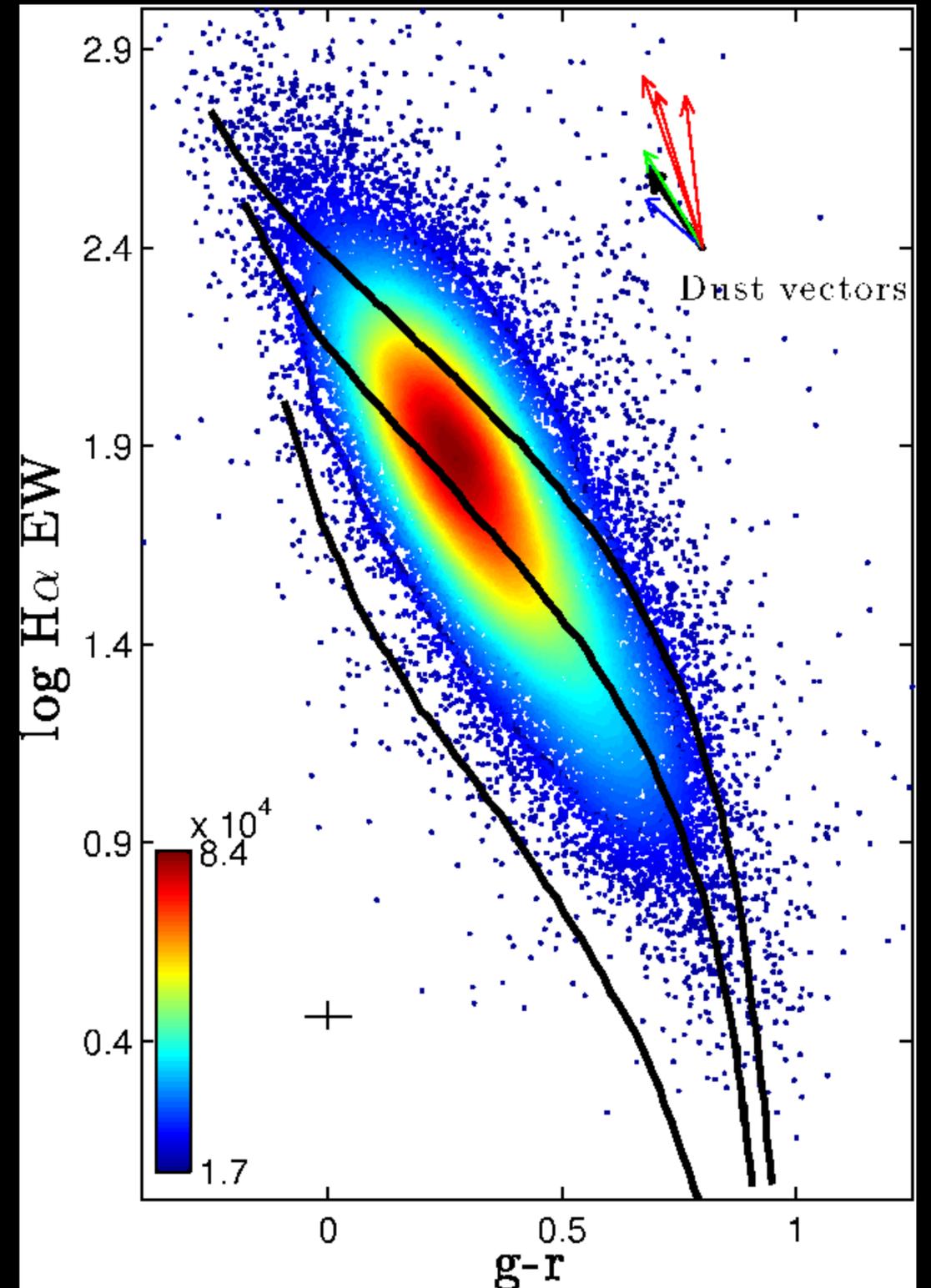
# H $\alpha$ -FUV ratio method

- FUV comes mainly from  $\sim 10$ - $20 M_{\odot}$  stars, so timescale is  $\sim 30$  Myr — probably safe to assume constant SFR in most galaxies
- H $\alpha$  / FUV therefore a proxy for ratio of  $> 60 M_{\odot}$  stars to  $\sim 10$ - $20 M_{\odot}$  stars  $\rightarrow$  IMF slope
- H $\alpha$  / FUV  $\sim$  constant in spirals, but falls in dwarfs with SFR  $\lesssim 0.1 M_{\odot} / \text{yr}$ : IMF variation?
- No! At low SFR, H $\alpha$  is highly stochastic due to rarity of massive stars and clustering of stars in time, so spectral synthesis needs to account for this. When it does, normal IMF fits data!



# H $\alpha$ -colour method

- FUV only accessible from space; from ground, can use colour as a proxy for SF history
- H $\alpha$  equivalent width versus colour depends on slope of IMF *or* location of low-mass turnover — position on track depends on age of stellar population
- Published claims suggest shallower IMF or higher turnover mass for higher SFR; however, major uncertainties not yet checked:
  - Stochasticity
  - Ionising photon escape
  - Dust absorption of ionising photons



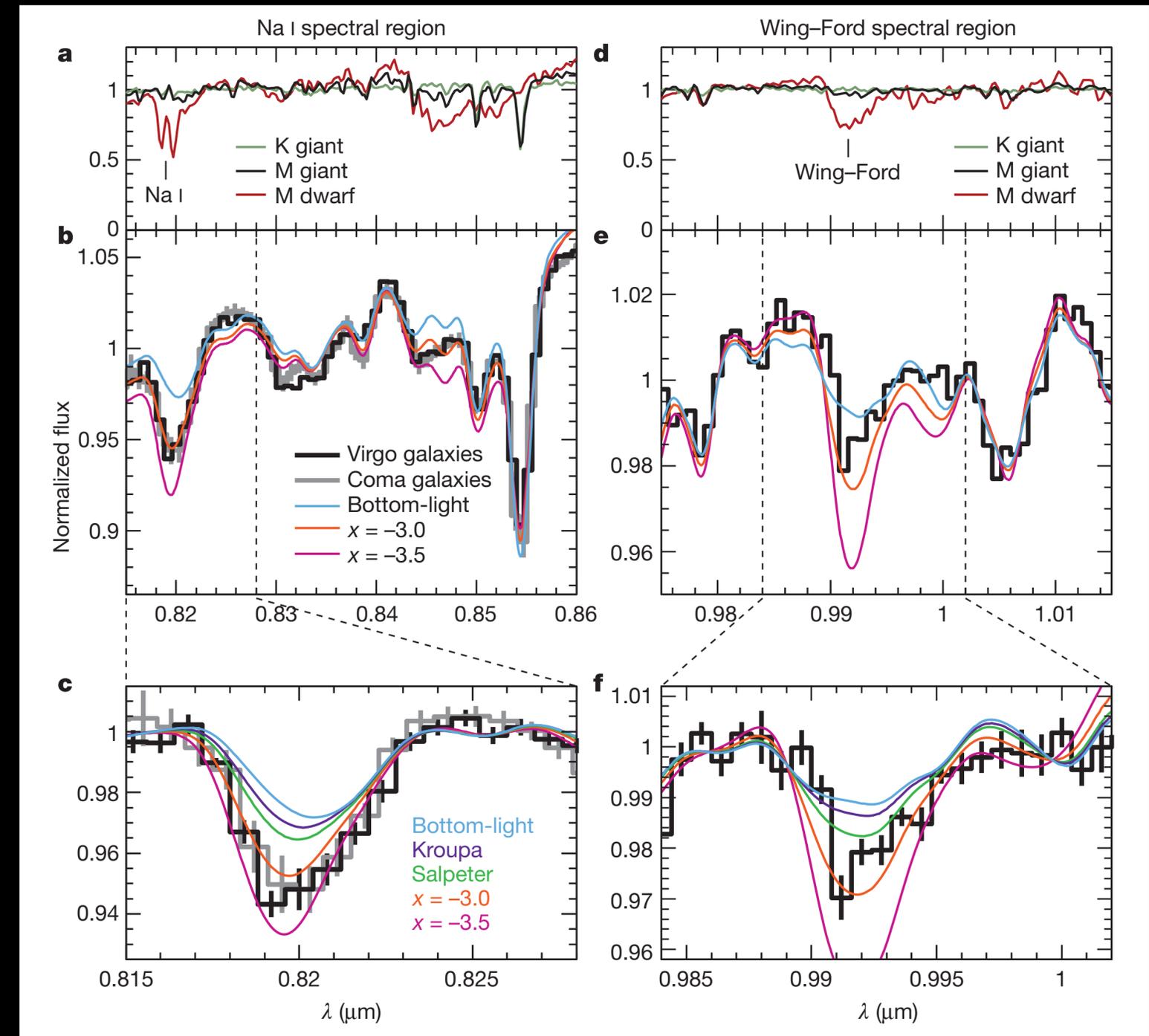
# Spectral feature methods

## General considerations

- Stochasticity, and SF history in general, is a problem for star-forming galaxies
- To avoid this, can look at massive elliptical galaxies instead — these have little gas, and mostly stopped forming stars very early ( $z > 2$ )
- Since stars are all old, can only study low-mass part of IMF
- Light output dominated by giant stars that have left the main sequence; subject major uncertainties in spectral synthesis
- Basic idea: use gravity-sensitive features to separate dwarfs from giants, focus on dwarfs, look for IMF-sensitive features in them

# M vs. K dwarfs

- Na I, Fe-H, Ca II, TiO<sub>2</sub> features separate dwarfs and giants
- Features appear in M dwarfs ( $\sim 0.1 M_{\odot}$ ) but not K dwarfs ( $\sim 0.3 - 0.5 M_{\odot}$ ), so depth of feature in integrated spectrum measures position of IMF peak / slope in region of peak
- Observations favour IMF peak at lower masses / steeper slope in ellipticals with higher velocity dispersion
- Caveat: spectral features calibrated from MW sample, but abundances in MW do not match ellipticals



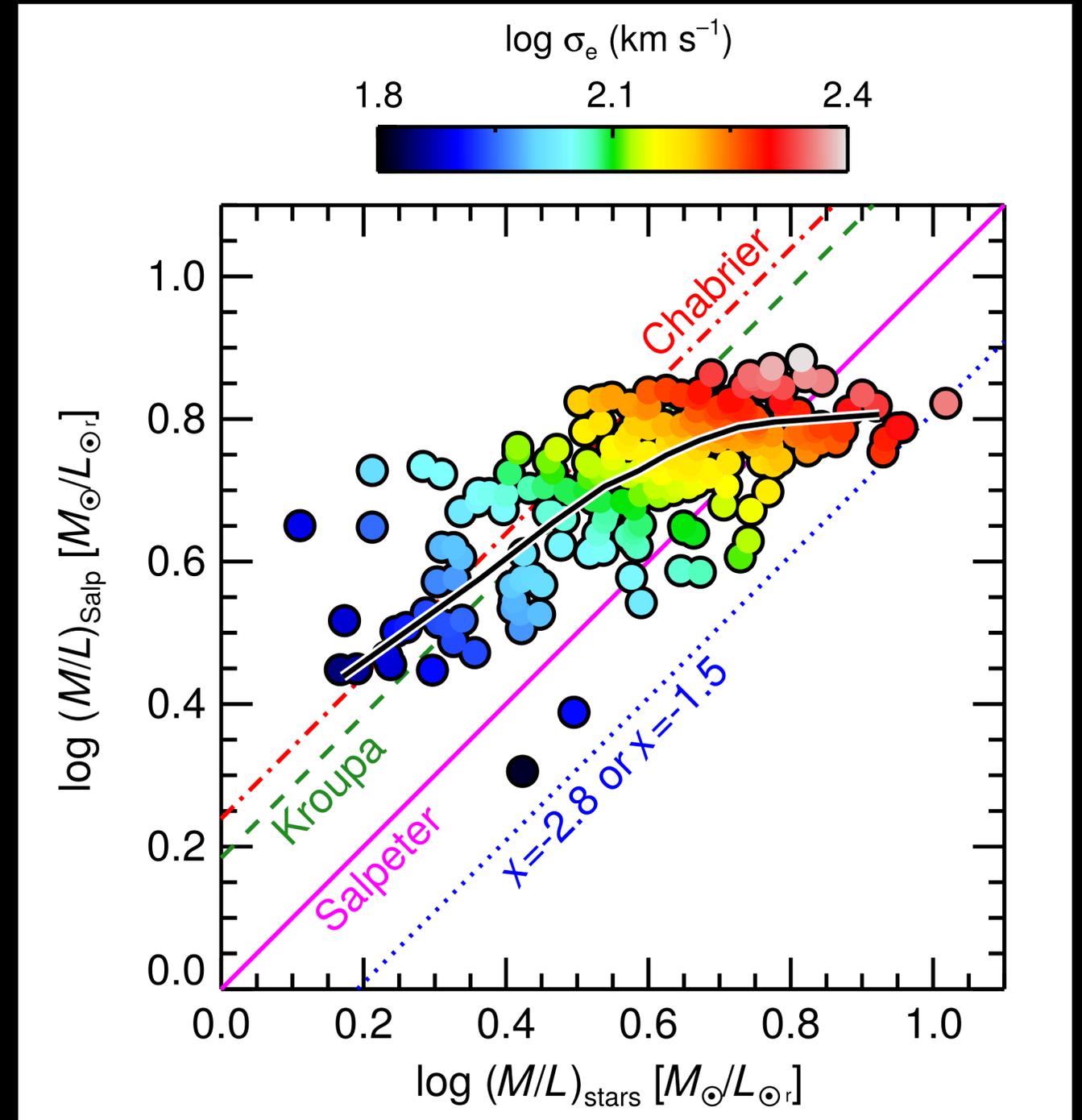
# M/L methods

## General idea

- Measure ratio of mass to luminosity in some broad band, compare to predicted value for a given IMF
- Luminosity is easy to measure; M/L in a broad band for a given IMF is easy to predict, much fewer uncertainties than spectral features
- Hard part is measuring mass. Two basic approaches:
  - Jeans (orbit) modelling
  - Gravitational lensing
- Target centres of ellipticals, where mass is dominated by stars, to avoid uncertainties on dark matter

# IMF from M/L

- Results from lensing + Jeans analysis both suggest higher M/L in ellipticals with higher velocity dispersion
- Broadly consistent with spectral result, since higher M/L  $\rightarrow$  lower IMF turnover mass
- However, poor agreement on a galaxy-by-galaxy basis — two methods sensitive to somewhat different radii in galaxy
- Effect is fairly small: factor of  $\sim 2$  in M/L



# Final notes

- There is some tension between the elliptical results and the massive cluster / high-SFR results:
  - Stars we see in ellipticals today formed at very high SFR, probably formed massive clusters — so if these environments lead to an IMF with more massive stars, why do ellipticals seem to have fewer massive stars?
- In general, history of the field suggests that claims of IMF variation should be treated with extensive skepticism: number of abandoned / retracted claims » number of still-viable claims
- Editorial viewpoint: I consider the elliptical work much more credible than the star-forming galaxy work, with the cluster work in between

**Exercise: consider two stellar populations, one with IMF slope  $-2.3$  from  $0.1 - 1 M_{\odot}$ , one with slope  $-1.3$  from  $0.1 - 0.5 M_{\odot}$  and  $-2.3$  from  $0.5 - 1 M_{\odot}$ . By what factor do their M/L ratios differ (approximately)?**