# Wind of Change: Faraday Rotation in a Simulated Large Magellanic Cloud

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# ABSTRACT

Magnetic fields significantly influence the structure of galaxies' interstellar media, but our understanding of magnetic field strengths and structures in external galaxies is severely limited. The Large Magellanic Cloud (LMC) offers a unique opportunity for improvement due to its proximity and large angular size, allowing for various detailed observations, particularly rich datasets of rotation measures and dispersion measures (RM and DM). However, interpreting these measurements is challenging due to the need for assumptions about the 3D structure for which we can only access line-of-sight integrated quantities. To address this, we conduct a suite of high-resolution magnetohydrodynamic (MHD) simulations of the LMC, incorporating star formation, star-bystar feedback, and ram pressure stripping by the Milky Way's circumgalactic medium (CGM), experienced as a circumgalactic wind in the frame of the LMC. Synthetic observations of these simulations allow us to identify parameters that closely match observed RM and DM values. Our best model, which is an excellent match to the real LMC, yields magnetic field strengths of  $\sim 1.4 \,\mu\text{G}$  (ordered) and  $\sim 1.6 \,\mu\text{G}$  (turbulent). In this model, Milky Way CGM wind experienced by the LMC plays a critical role in shaping the RM data, with the bulk of the RM signal arising not from the LMC's plane, but from warm,  $\sim 10^4$  K, gas in a Reynolds layer region  $\sim 1$  kpc off the plane where relatively dense material stripped from the LMC is partially ionised by hard extragalactic radiation fields. This finding suggests that we should be cautious about generalising inferences from the LMC to other galaxies that may not be shaped by similar interactions.

Key words: ISM: magnetic fields – MHD – techniques: polarimetric – galaxies: Interactions – Magellanic Clouds – galaxies: magnetic fields

# **1 INTRODUCTION**

Magnetic fields permeate many astrophysical objects over a range of scales from planetary (~  $10^{-10} - 10^{-8}$  pc) to intergalactic (~  $10^{6}$  pc). When these fields are strong, they have a broad range of physical effects that modify the evolution of the objects that host them, for example altering the way that fluids mix and cool, and suppressing fluid instabilities such as Kelvin-Helmholtz and Rayleigh-Taylor (e.g., Chandrasekhar 1961; Ji et al. 2019; Das & Gronke 2023). In the context of galaxy formation and evolution, simulations show that magnetic fields affect galactic properties including the H I mass in the CGM, interstellar medium (ISM) disc sizes (van de Voort et al. 2021), the extents of filamentary structures (Ade et al. 2016; Federrath 2016; Das & Gronke 2023), and star formation rates and initial stellar mass distributions (Federrath & Klessen 2012; Krumholz & Federrath 2019). Magnetic fields' effects on cosmic ray transport and feedback are also critical (Salem et al. 2015; Seta et al. 2017; Farcy et al. 2022; Butsky et al. 2022).

However, magnetic fields are notoriously difficult to observe. Polarised dust emission or absorption reveals the field direction, but not (at least not directly) its intensity. Field strengths can be measured using the Zeeman effect (Crutcher 2012), but Zeeman splittings are generally too small to detect beyond the Milky Way. For extragalactic systems, perhaps our best available tool is the Faraday rotation measure (RM). This method uses bright and compact polarised background sources, such as quasars or radio galaxies, which emit linearly polarised synchrotron radiation (Duric 1988; Klein & Fletcher 2015). As this linearly polarised radiation passes through the magneto-ionic gas of a foreground galaxy, its initial polarisation angle  $\psi_0$  rotates so that the observed polarisation angle becomes (see Sec. 3.3 in Klein & Fletcher 2015)

$$\psi_{\text{obs}} = \psi_0 + \text{RM}\,\lambda^2,\tag{1}$$

where  $\lambda$  is the wavelength of the radiation and RM is the Faraday rotation measure, given by

$$RM = \frac{0.81}{(1+z)^2} \int \frac{n_e}{cm^{-3}} \frac{\vec{B}}{\mu G} \cdot \frac{ds}{pc} rad/m^2, \qquad (2)$$

where z is the redshift of the source,  $n_e$  is the thermal electron density,  $\vec{B}$  is the component of the magnetic field along the line of sight, and s measures position along the line of sight (LOS) from our location to the source. By measuring how the polarisation angle of an observed source varies with wavelength, we can back out the value of RM along the LOS, which directly probes the mean field strength in the foreground gas.

The Large Magellanic Cloud (LMC), one of the closest and largest Milky Way (MW) satellite galaxies, is an excellent target for extra-

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galactic magnetic field studies both because it is an interesting system that is undergoing an interplay of complex interactions, and because it feasible to obtain large RM-based maps of its field structure. With regard to the first of these points, the LMC is currently subject to two major interactions (Putman et al. 1998; Putman et al. 2003; Staveley-Smith et al. 2003; Kim et al. 2003; Olsen & Massey 2007; Nidever et al. 2013; Indu & Subramaniam 2015; Salem et al. 2015; Petersen et al. 2022): ram pressure stripping and tidal interactions as a result of LMC's orbit through the MW circumgalactic medium (CGM), and tidal stripping due to the Small Magellanic Cloud (SMC) orbiting around it. These interactions significantly alter LMC's gas dynamics and presumably also its magnetic field structure. With regard to feasibility, observations of the LMC are facilitated by the fact that it resides just  $\approx$  50 kpc from us (Pietrzyński et al. 2019), which makes its angular size as viewed from the Earth very large,  $\sim 10.75^{\circ} \times 9.17^{\circ}$ , so that it covers a large number of background radio sources bright enough to permit RM measurements. Moreover, its location well off the MW plane (Galactic latitude  $b \approx -33^{\circ}$ ) is fortuitous in that it lacks a significant MW foreground along the line-of-sight.

Given these attributes, it is not surprising that magnetic fields in the LMC have already been studied extensively. Gaensler et al. (2005, hereafter G2005) observed RMs along  $\approx 151$  sightlines through the LMC and concluded that the fields show an axisymmetric spiral geometry, which they attributed to the action of a large-scale dynamo. Livingston et al. (2024) followed the same observational methods and obtained similar qualitative results for the RM structure from a larger sample of sightlines. Mao et al. (2012) used the diffuse polarised synchrotron radiation arising from the LMC ISM to probe the magnetic fields in the side of the LMC halo nearer to us. Most of the RM values that Mao et al. obtained are negative, meaning the magnetic fields are directed away from the observer, consistent with the simple quadrupolar magnetic field structure expected for a large-scale dynamo (Parker 1971).

While such an interpretation is plausible, it is by no means unambiguous, because it is far from trivial to infer magnetic fields from RM observations. As can be seen from Equation 2, deriving the LOS magnetic field requires making assumptions about both the electron density and the path length through the magnetised medium. For instance, G2005's interpretation of the RM data as implying an axisymmetric field in the LMC disc relies on assuming a single electron column density for the entire LMC along with an idealised field geometry whereby halo magnetic fields are mirror-symmetric about the disc, leading their effects to cancel. Livingston et al. (2024) also assumed that RM measurements primarily probe disc fields, but adopted a slightly more complex model for position-dependent electron column densities. While adopting assumptions such as these is an understandable starting point given the difficulty of interpreting integrated LOS quantities, the LMC's complex environment renders them questionable. For example, the gas in the LMC halo should be strongly asymmetric due to tidal interactions and ram pressure stripping, and so there is no reason to believe that the magnetic geometry is symmetric either – and if there is no symmetry, then there is also no good reason to believe that RM measurements are primarily probing disc fields rather than halo magnetic fields. This complexity suggests a need to move past simple assumed geometries and instead combine realistic simulations with mock observations to facilitate more accurate inference of magnetic field structure.

With modern computers and simulation methods such simulations are possible, and indeed several authors have already simulated the LMC and its interactions with the MW and the SMC (e.g., Mastropietro et al. 2005, 2009; Besla et al. 2012; Salem et al. 2015; Pardy et al. 2018; Wang et al. 2019; Lucchini et al. 2020, 2021, 2024; Jiménez-Arranz et al. 2024; Sheng et al. 2024). These papers have examined topics including the role of tidal interactions in shaping the morphology of the LMC, the effects of ram pressure stripping on its H<sub>1</sub> gas disc, the orbital histories of the LMC-SMC system, features of the CGM surrounding the LMC, and the origin of gas in the Magellanic stream and bridge. However, none of these existing simulations have included magnetic fields, and thus they cannot be used to interpret RM measurements. Moreover, it is entirely possible that the omission of magnetic fields itself leads to substantial inaccuracies in the simulation results, since there is ample evidence that magnetic fields have important dynamical effects in local galaxies (e.g., Beck 2009; Pakmor & Springel 2013; Pakmor et al. 2017; Kim et al. 2019; Pillepich et al. 2019; Hopkins et al. 2019; van de Voort et al. 2021; Wibking & Krumholz 2023).

Here, we present the first-ever suite of high-resolution magnetohydrodynamic (MHD) simulations of the LMC and its interaction with the MW CGM. We post-process this suite to generate mock observables that permit direct comparison with measurements of the real LMC. In Section 2, we outline our simulation setup and postprocessing pipeline for generation of the mock observables. Section 3 outlines our results and presents a detailed comparison between mock and real observations, which we use to identify which of the simulations in our suite best match reality. We in turn use this information to interpret several aspects of the RM data. Finally, in Section 4 we summarise our primary results.

# 2 METHODS

Here we outline all the steps in our analysis: how we simulate the LMC (Section 2.1), the initial conditions we use for those simulations (Section 2.2), how we generate those mock observations from the simulations (Section 2.3), and the post-processing of the gas ionisation state required for the mock observations (Section 2.4).

# 2.1 Simulation

We use the GIZMO code (Hopkins 2015) to solve the equations of ideal magnetohydrodynamics (MHD) plus self-gravity for a fluid interacting with a population of collisionless star and dark matter particles; for MHD we use GIZMO's meshless finite mass (MFM) setting (Hopkins & Raives 2015) with the constrained-gradient divergence cleaning method described by Hopkins (2016). Apart from MHD, we incorporate a time-dependent chemistry network with abundances of H I, H II, He I, He II, He III, and free electrons, and gas cooing using tabulated H, He, and metal cooling rates calculated with the photoionisation code CLOUDY (Ferland et al. 1998; Chatzikos et al. 2023), included as a part of the GRACKLE chemistry and radiative cooling library (Smith et al. 2008, 2016). GRACKLE includes a UV background radiation field based on the models of Haardt & Madau (2012), which for our simulations we evaluate at redshift z = 0; it also includes an FUV background that provides a uniform photoelectric heating rate of  $8.5 \times 10^{-26} n_{\rm H}^{-1} \,{\rm erg \, cm^{-3} \, s^{-1}}$ , where  $n_{\rm H}$  is the number density of H nucleons, in gas with temperatures  $T < 2 \times 10^4$  K, consistent with the estimates of Wolfire et al. (2003) and Tasker & Bryan (2008). We use GRACKLE rather than GIZMO's built-in cooling module because the former does not correctly produce a multi-phase atomic medium (Wibking & Krumholz 2023), something that will be important for our purposes.

Our star formation model follows the approach described by Springel & Hernquist (2003), whereby gas elements with densities  $\rho > \rho_{SF}$  are probabilistically converted into star particles (e.g., Katz

et al. 1996) with a probability per unit time such that the expected star formation rate per unit volume for a fluid of density  $\rho$  is  $\dot{\rho}_* = \epsilon_{\rm ff} \rho / t_{\rm ff}$ , where  $t_{\rm ff} = \sqrt{3\pi/32G\rho}$  is the gas free-fall time. Our settings for  $\rho_{\rm SF}$ and  $\epsilon_{\rm ff}$  mirror those described by Wibking & Krumholz (2023) and Hu et al. (2023). We set  $\rho_{SF}$  to a resolution-dependent value chosen so that star formation occurs only once the gas density exceeds our ability to resolve the collapse any further. Quantitatively, we set  $\rho_{SF}$ implicitly via the condition that  $\Delta m = M_J(\rho_{\rm SF}, T_{\rm eq.SF})$ , where  $\Delta m$ is the simulation mass resolution,  $M_I$  is the Jeans mass as a function of density and temperature, and  $T_{eq,SF}$  is the equilibrium temperature for gas of density  $\rho_{\rm SF}$ . We solve this equation numerically for our chosen heating and cooling rates and mass resolution, and report the resulting value of  $ho_{\rm SF}$  for each of our simulations below. For gas with density  $\rho$  from  $\rho_{SF}$  to  $100\rho_{SF}$  we set  $\epsilon_{ff} = 0.01$ , consistent with observations (e.g., Krumholz & Tan 2007; Krumholz et al. 2012, 2019; Utomo et al. 2018; Sun et al. 2023). In gas denser than  $100\rho_{SF}$  we artificially increase  $\epsilon_{\rm ff}$  to 100% so that gas is consumed very quickly; this limits the computational resources spent following high-density structures that evolve on short dynamical times.

Our simulations include three channels of stellar feedback: stellar winds, supernovae, and photoionisation. We implement stellar wind and supernova feedback using the explicit mechanical feedback coupling algorithm described by Hopkins et al. (2014) and Hopkins et al. (2018a), which ensures momentum and energy conservation as well as statistical isotropy, and interpolates between treating SN feedback as a deposition of thermal energy and a deposition of mechanical momentum depending on whether the Sedov-Taylor radius is resolved. Our implementation of this algorithm is identical to that described in Wibking & Krumholz (2023). Our treatment of photoionisation uses a Strömgren volume method as re-implemented by Armillotta et al. (2019) based on the work of Hopkins et al. (2018b). Gas that is located within a Strömgren sphere is heated to a temperature of 10<sup>4</sup> K.

Because we will carry out simulations with significantly higher mass resolution that is typical in the cosmological applications for which GIZMO is most commonly used, we do not use the standard GIZMO method for computing the supernova, wind, and ionising photon output, which assumes stellar populations large enough to fully sample the stellar initial mass function (IMF). We instead use the stochastic star-by-star treatment outlined in Hu et al. (2023). In this treatment when a star particle of mass  $M_*$  forms, we stochastically draw a stellar population of that mass from a Chabrier IMF (Chabrier 2005) using the slug (Stochastically Lighting Up Galaxies) stellar population synthesis code (da Silva et al. 2012; Krumholz et al. 2015). We then run slug as a backend to the simulation, using it to track the evolution of the stellar population as it ages and return the instantaneous ionising luminosity and wind luminosity, and the timing of all supernovae, each of which is assumed to detonate with an energy budget of  $10^{51}$  erg. We refer readers to Hu et al. for a more detailed description of the method.

# 2.2 Initial conditions

All our simulations begin with gas, dark matter (DM) and old stellar<sup>1</sup> particles, whose masses are given in Table 1 for our different resolutions. In all cases we set the initial temperature of all gas particles

Table 1. Mass resolutions and star f	formation thresholds
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Resolution	$\Delta m_{\rm gas}$ (M <sub><math>\odot</math></sub> )	$\Delta m_{\rm DM}$ (M <sub><math>\odot</math></sub> )	$\Delta m_{*}$ (M $_{\odot}$ )	$ ho_{\mathrm{SF}}/m_{\mathrm{H}}$ (cm <sup>-3</sup> )
Low	1000	80682	1136	194
Medium	250	20170	284	1018
High	100	8068	114	2379

Columns: (1) resolution type; (2) gas particle mass; (3) dark matter particle
mass; (4) old stellar particle mass; (5) star formation density threshold
normalised to the hydrogen mass.

to  $10^4$  K, but except in very rarefied regions the gas cools from this temperature rapidly. Similarly, we set the metallicity of all gas particles to  $Z = 0.5Z_{\odot}$ , the observed metallicity of the LMC. We run all simulations for 500 Myr, roughly 5 rotation periods for an LMC-like galaxy, which we find is long enough for the structure of the galaxy to reach statistical steady state.

All other aspects of our initial conditions vary from one simulation to another. This variation is characterised by four parameters: the mass resolution  $\Delta m$ , the initial strengths of the smooth azimuthal and turbulent components of the magnetic field  $B_0$  and  $B_{turb}$ , and whether we simulate an isolated galaxy or one that is traversing, and subject to ram pressure stripping by, the MW CGM. We list the full set of simulations we run in Table 2, and report resolutiondependent properties of the simulations in Table 1. For convenience, from this point forward we refer to simulations by names of the form I-A-T-r or W-A-T-r; I or W indicates whether the simulation uses an isolated (I) galaxy or one experiencing a wind (W) from the MW CGM, A and T give the strength of the initial smooth azimuthal and turbulent fields, respectively, in units of  $\mu$ G, and R is L, M, or H, indicating low ( $\Delta m = 1000 \text{ M}_{\odot}$  for gas), medium ( $\Delta m = 250 \text{ M}_{\odot}$ ), or high ( $\Delta m = 100 \text{ M}_{\odot}$ ) resolution. Thus for example I-2-6-L indicates a low-resolution simulation of an isolated galaxy with an initial magnetic field of 2  $\mu$ G in a smooth azimuthal component and 6  $\mu$ G in a turbulent component, while W-O-12-M indicates a medium-resolution simulation of an LMC experiencing a wind, and initialised with a 12  $\mu$ G turbulent field and no smooth field. We describe the details of how we implement each of these aspects of the initial conditions below.

# 2.2.1 Isolated galaxy simulations

For our simulations of an isolated LMC-analogue, we use open boundary conditions and initialise a galactic disc with its centre of mass at the origin and zero net momentum. We initialise the dark matter and old stellar disc particles for simulations in this class using the GALIC code (Yurin & Springel 2014). This code uses elements of Schwarzchild's technique, whereby one starts with some initial assignment of particle velocities and evolves it to optimise a merit function characterised by the difference between the target density field and the actual density response created by the N-body realisation associated with the initial velocities. Rather than optimising a global merit function as in a traditional Schwarzchild's method, this algorithm optimises the velocities of each particle directly, avoiding the need for an explicit orbit library. We set the parameters for GALIC to the same values adopted by Lucchini et al. (2020) for their simulations of the LMC. These are a DM halo with mass  $M_{200} = 1.775 \times 10^{11} \,\mathrm{M_{\odot}}$  and a concentration parameter c = 10, and a stellar disc with mass  $2.5\times 10^9\,M_\odot$  and scale length and

<sup>&</sup>lt;sup>1</sup> We use the term old stellar particles to indicate stars that are present at the start of a simulation, rather than forming during it. Old stellar particles differ from those formed in the course of the simulation in that they do not supply any feedback.

Table 2. Summary of simulations

Simulation name		Initial conditions			Outcomes					
	Туре	<i>B</i> <sub>0</sub> (μG)	$B_{turb}$ ( $\mu$ G)	Resolution	$\langle B_{\phi} \rangle$ ( $\mu$ G)	$\sigma_B$ ( $\mu$ G)	$\sigma_{\rm RM}$ (rad m <sup>-2</sup> )	$\mathcal{I}_{\rm RM}$ (rad m <sup>-2</sup> )	$p_{\rm RM}^+$	$p_{\rm RM}^-$
I-0-2-L	Isolated	0	2	Low	0.04	0.34	$25.47 \pm 1.01$	$26.29 \pm 1.3$	$0.52 \pm 0.03$	$0.52 \pm 0.02$
I-2-0-L	Isolated	2	0	Low	3.16	1.73	$66.12 \pm 1.88$	$82.09 \pm 3.93$	$0.86 \pm 0.02$	$0.85 \pm 0.02$
I-2-2-L	Isolated	2	2	Low	2.99	1.59	$49.41 \pm 1.53$	$57.2 \pm 3.04$	$0.78 \pm 0.02$	$0.77 \pm 0.0$
I-2-6-L	Isolated	2	6	Low	2.83	1.57	$48.01 \pm 1.66$	$52.6 \pm 2.82$	$0.75 \pm 0.02$	$0.7 \pm 0.02$
W-2-0-L	Wind	2	0	Low	4.89	1.79	$100.84 \pm 3.1$	$139.43 \pm 6.35$	$0.9 \pm 0.02$	$0.88 \pm 0.0$
W-2-2-L	Wind	2	2	Low	3.21	1.77	$62.46 \pm 1.89$	$74.43 \pm 3.35$	$0.84 \pm 0.02$	$0.79 \pm 0.0$
W-2-6-L	Wind	2	6	Low	3.26	1.78	$55.2 \pm 1.55$	$69.45 \pm 2.98$	$0.84 \pm 0.02$	$0.78 \pm 0.0$
I-0-12-M	Isolated	0	12	Medium	-0.10	0.66	$27.55 \pm 1.0$	$29.79 \pm 1.33$	$0.52 \pm 0.02$	$0.52 \pm 0.0$
I-2-6-M	Isolated	2	6	Medium	1.20	1.73	$33.17 \pm 1.25$	$36.84 \pm 1.64$	$0.68 \pm 0.02$	$0.65 \pm 0.0$
W-2-6-M	Wind	2	6	Medium	1.98	1.94	$40.48 \pm 1.33$	$47.32 \pm 2.23$	$0.71 \pm 0.02$	$0.67 \pm 0.0$
I-2-6-H	Isolated	2	6	High	0.99	1.61	$31.58 \pm 1.09$	$35.0 \pm 1.56$	$0.65 \pm 0.02$	$0.6 \pm 0.0$

Columns: (1): name of simulation; (2): isolated or wind simulation; (3): initial smooth azimuthal field strength; (4): initial turbulent field strength; (5) resolution (see Table 1; (6) final mean azimuthal field at two stellar scale lengths; (7) final turbulent field strength at two stellar scale lengths; (8) dispersion of RM; (9) Interquartile (25<sup>th</sup>-75<sup>th</sup> percentile) range (10) and (11): RM alignment fraction on the positive and negative RM sides of the galaxy.

height 1.8 kpc and 0.3 kpc, respectively. We use these parameters in GALIC's model D1 (see Table 1 in Yurin & Springel 2014), which assumes a spherical dark halo, thin stellar disc, and axisymmetric velocity structure.

To initialise the gas disc, we set the total gas mass to  $2.2 \times 10^9 \text{ M}_{\odot}$ and the disc scale length ( $R_0$ ) and height ( $Z_0$ ) are 4.8 kpc and 0.48 kpc, respectively; we again take these parameters from Lucchini et al. (2020). The gas density distribution is doubly-exponential, with the form

$$\rho = \rho_0 \exp\left(-\frac{r}{R_0}\right) \exp\left(-\frac{|z|}{Z_0}\right),\tag{3}$$

where  $(r, \phi, z)$  are the standard cylindrical coordinates. In practice we implement this density distribution by drawing the initial positions of gas particles from a probability distribution function  $p(r, \phi, z) \propto \rho$ . Once we have drawn positions for all gas particles, we initialise their velocities by first computing the gravitational potential  $\psi$  of the combined gas, stars, and dark matter using the PYTREEGRAV package<sup>2</sup>, and then setting particle velocities in the azimuthal direction  $v_{\phi}$  such that all gas particles are in centrifugal equilibrium against gravity, i.e.,

$$\frac{v_{\phi}^2}{r} = -\frac{\partial\psi}{\partial r}.$$
(4)

We initialise the gas magnetic field with a combination of ordered and turbulent components. The ordered component is purely azimuthal, and follows the same functional form and scale length and height as the gas density:

$$B_{\phi} = B_0 \exp\left(-\frac{r}{R_0}\right) \exp\left(-\frac{|z|}{Z_0}\right).$$
<sup>(5)</sup>

Here  $B_0$  is the field strength, which varies from simulation to simulation as indicated in Table 2. While this field is analytically divergencefree, its discretisation onto particles introduces numerical divergence; we remove this by carrying out an initial divergence cleaning and local approximate Hodge projection step prior to starting the simulation (Hopkins 2016). We generate the turbulent component of the field as a divergence-free Gaussian random field with a Kolmogorov spectrum of slope -5/3 (Minter & Spangler 1996) and a standard deviation  $B_{turb}$ , which like  $B_0$  varies between simulations as indicated in Table 2. The largest and smallest scales in our field are 1 kpc and the resolution limit, respectively. We enforce zero divergence on this field using the projection method, whereby we set the radial component in Fourier space to zero.

#### 2.2.2 Simulations with ram pressure stripping

We make several modifications to our initialisation procedure to simulate the LMC interacting with the MW CGM in our W simulations. First, we use a periodic domain of size 200 kpc × 200 kpc × 400 kpc rather than open boundary conditions as in the isolated simulations; the purpose of this change is to contain a background gas representing the MW CGM through which our LMC can move.

Our second major change is to the LMC's initial position and orientation, and is illustrated in Figure 1. We first initialise the LMC in exactly as in the I simulations; at this point the disc of the LMC lies in the xy-plane, and the angular momentum vector of the LMC is in the z direction. We then translate the positions of all LMC gas, old stellar, and dark matter particles so that the centre of the LMC is at position (x, y, z) = (100, 100, 100) kpc in our periodic domain, where the lower left corner of the domain is at the origin. We next rotate the particle positions and velocities by an angle of  $\theta = 53.57^{\circ}$  counterclockwise in the xz plane around the LMC centre, so that the angular momentum vector now points in a direction  $\hat{n} = (-0.805, 0, 0.593),$ and add to each particle a velocity  $V_{LMC}\hat{z}$ , where  $V_{LMC} = 320.7$  km s<sup>-1</sup>. The values of  $V_{\rm LMC}$  and  $\theta$  are, respectively, the velocity of the LMC relative to the MW's centre and the angle between the LMC's velocity and angular momentum vectors (Salem et al. 2015, their Table 3). Note that, over the 500 Myr of our simulation, the LMC will move 160 kpc, from (100, 100, 100) kpc to (100, 100, 260) kpc, and thus will remain far from the walls of our periodic domain.

Finally, we fill the simulation domain with a background gas whose density as a function of z-position  $\rho(z)$  is chosen such that, as the LMC moves, the gas it encounters will have the same density as a function of time as the real LMC has encountered. We take this density as a function of time from the MW halo model of Salem

<sup>&</sup>lt;sup>2</sup> https://github.com/mikegrudic/pytreegrav

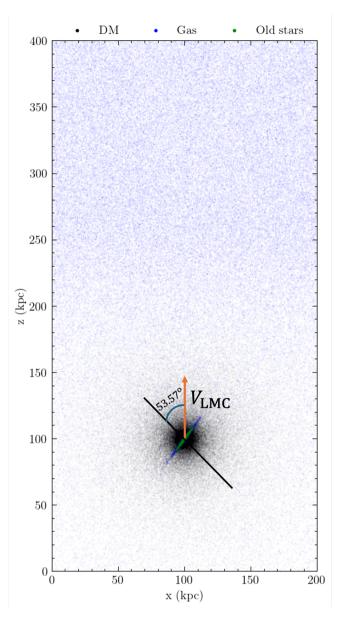
et al. (2015), who use a combination of models of the LMC's orbit and comparisons between H I 21 cm observations and simulations of ram pressure-stripped galaxies in order to estimate the density of the MW halo gas through which the LMC has passed over the last ~Gyr. They find that this density reached a maximum  $n_{\rm H} = 1.1 \times 10^{-4}$ cm<sup>-3</sup> during the LMC's pericentric approach ~ 50 Myr ago, but was significantly lower in the past when the LMC was further from the MW, and that as a result ram pressure stripping only became dynamically significant in the last ~ 100 – 200 Myr, significantly shorter than our simulation duration. To capture this change in density over time, we extract the background density as a function of time experienced by the LMC,  $\rho_{\rm LMC}(t)$ , from Salem et al.'s Figure 4. We then set the density of the background gas in our simulation domain as  $\rho(z) = \rho_{\rm LMC}(t(z))$ , where

$$t(z) = \begin{cases} (z - z_0)/V_{\text{LMC}} - t_0, & -z_0 < z - z_0 < V_{\text{LMC}} t_0 \\ 0 & z - z_0 > V_{\text{LMC}} t_0 \end{cases},$$
(6)

and  $z_0 = 100$  kpc and  $t_0 = 500$  Myr are the initial LMC *z*-position and run duration, respectively. The density variation  $\rho(z)$  is visible in Figure 1. The background gas has zero initial velocity, and in order to ensure that it remains static prior to the passage of the LMC through it, we set the background temperature T(z) such that  $\rho(z)T(z)$  is constant and there is no pressure gradient; we normalise this relation such that  $T = 5 \times 10^6$  K at  $z < z_0$ , and given the density profile we take from Salem et al. this implies a temperature range from  $\approx 5 \times 10^5 - 5 \times 10^6$  K, reasonable CGM gas temperatures. However, Salem et al. also find that the CGM temperature has little effect on the process of ram pressure stripping. Finally, we initialise the magnetic field in the background gas using a Gaussian-random field with the same spectral shape as the turbulent disc field, but with a standard deviation of  $0.6 \,\mu$ G (Pakmor et al. 2020; Shah & Seta 2021; Heesen et al. 2023) and an outer scale of 30 kpc (Pakmor et al. 2020).

The final minor differences in initialisation from the I case are intended to maintain continuity across the disc-halo interface. For densities, we define the disc-halo interface as the location where the gas disc density is the same as the gas halo density. We remove all the gas particles from the halo (disc) inside (outside) this interface to make densities continuous.

For magnetic fields, the disc-halo interface is defined to be the location where the magnitude of the decaying, ordered component of disc magnetic field (Equation 5) is equal to the RMS strength of the halo magnetic field  $(0.6 \,\mu\text{G})$ . We set the disc field to zero outside this boundary and the halo field to zero inside it; note that this procedure does not guarantee that the magnetic field remains divergence-free at the disc-halo interface, but the initial divergence cleaning step carried out at simulation startup (Section 2.2.1) removes any divergence that it introduces.



**Figure 1.** Edge-on projection of initial particle positions in our  $\mathbb{W}$  simulations. We show gas (blue), DM (black), and old stellar (green) particles; note that gas is present both in the LMC disc and in the background, and that the background has a density gradient chosen such that, as the simulated LMC moves, the density of material it encounters will reproduce the history of the real LMC. The angle of 53.57° between the LMC velocity vector ( $V_{LMC}\hat{z}$ ) and angular momentum vector (direction illustrated by the black line) ensures that our simulated LMC experiences a wind with the same angle of attack as the real LMC.

(EMs). These three quantities are defined as

$$DM = \int n_e \, ds \tag{7}$$

$$RM = 0.81 \frac{\text{rad } \text{m}^{-2}}{\text{cm}^{-3} \ \mu\text{G pc}} \int n_{\text{e}}(\vec{B} \cdot \hat{s}) \, ds \tag{8}$$

$$EM = \int n_e^2 \, ds \tag{9}$$

# 2.3 Creating mock observables

#### 2.3.1 Definitions of the quantities

The three main observable diagnostics to which we have access when studying the LMC's magnetic field structure are dispersion measures (DMs), Faraday rotation measures (RMs), and emission measures where  $n_e$  and  $\vec{B}$  are the electron density and magnetic field, s is a coordinate that measures position along the line of sight, and the integrals are thus evaluated along a path from the emitting source to the observer. Observations of DM come primarily from sightlines to pulsars in the LMC, which are corrected for the contribution to the DM arising from the ISM of the MW (McCulloch et al. 1983; Seward et al. 1984; McConnell et al. 1991; Marshall et al. 1998; Crawford et al. 2001; Manchester et al. 2006; Ridley et al. 2013; Johnston et al. 2021), while RMs are most often measured using linearly polarised synchrotron emission from background quasars. Emission measures are observed using the H $\alpha$  brightness. Note that, while the EM and DM are not directly sensitive to the magnetic field, they are useful for interpreting RMs, which mix together magnetic field and electron density; a common practice is to use DMs to infer typical electron densities, which are then in turn combined with RMs to yield magnetic field strengths.

# 2.3.2 Geometry

In order to generate mock observations, we must evaluate the integrals appearing in Equation 7 - Equation 9 through our simulation. To facilitate this exercise, we first transform our simulated LMC into a frame such that our line of sight is aligned with the *z*-axis. For Wsimulations this requires two steps: we first align the angular momentum vector of the LMC with the *z* axis of the simulation by applying the rotation matrix

$$R_{\rm z} = \begin{bmatrix} -0.42 & 0.71 & -0.57\\ -0.42 & -0.71 & -0.57\\ -0.8 & 0 & 0.6 \end{bmatrix}$$
(10)

to the position of every gas particle, using positions measured relative to the centre of the simulated LMC. This rotation corresponds to  $\alpha = 0^\circ$ ,  $\beta = 53.57^\circ$ , and  $\gamma = 225^\circ$ , where  $\alpha, \beta, \gamma$  are the Euler angles assuming extrinsic rotation. While  $\gamma = 225^\circ$  is not necessary to align the angular momentum vector of the LMC with *z*-axis, it is necessary to align the wind direction in the observer's frame when the second rotation is performed. We then rotate again to place the LMC into a frame where the observer is located at  $z = +\infty$  (or outside the simulation domain) using the rotation matrix

$$R_{\rm obs} = \begin{bmatrix} 0.64 & 0.63 & -0.44 \\ -0.76 & -0.53 & 0.37 \\ 0 & -0.57 & -0.82 \end{bmatrix}.$$
 (11)

The procedure for the I simulations simply uses the second step. We validate these transformations by comparing the wind velocity and angular momentum vectors with those documented by Salem et al. (2015) in their observer's frame.

#### 2.3.3 Dispersion measures

Now that we have our observer's line of sight aligned to the  $\hat{z}$  direction, we can evaluate integrals through the simulation domain to generate mock DMs, RMs, and EMs. For DMs, since the observations to which we are comparing target pulsars within the LMC, we place in the simulations 200 synthetic pulsars, approximately equal to the steady-state number of sLUG clusters in the age range 5 – 10 Myr expected for young pulsars. We choose the locations for these pulsars by starting from the positions of sLUG clusters (chosen at random if there are more clusters than pulsars) and adding a random displacement drawn from a 3d Gaussian distribution with a standard deviation of 500 pc. This displacement scale emerges from typical

pulsar characteristics: spin-down times of 5-10 Myr (Alvarez & Carramiñana 2004) and kick velocities of approximately 100 km s<sup>-1</sup> for the slower group of pulsars (Verbunt et al. 2017). Once we have our set of mock pulsar positions, we calculate DMs to them by evaluating the integral in Equation 7 from the location of pulsar towards the observer along the line of sight.<sup>3</sup>

#### 2.3.4 Rotation and emission measures

Since RMs are most often measured toward background quasars whose positions are random, we generate mock RM measurements by placing sightlines uniformly in a  $10 \text{ kpc} \times 10 \text{ kpc}$  region around the LMC centre in the observer's frame and integrating Equation 8 through the full domain. We pick 200 such sightlines as this is approximately equal to the number of RM sightlines available from the observations to which we will be comparing below, which come from G2005. We discuss the rationale for choosing this data set in more detail in Section 3.2. We find that choosing a different number of sightlines (100, 300, 400, 500) changes the outcome statistics by ~ 10%.

We also calculate EMs along the same lines of sight (Equation 9), which is important so that we can replicate the selection procedure used by G2005. These authors discard any RM measurements along lines of sight with EM > 100 pc / cm<sup>6</sup> to avoid observational errors due to depolarisation along lines of sight that pass through dense ionised regions. So that we can compare fairly with the observations, we replicate this cut by removing from our sample any RM measured along a line of with for which the EM is above this threshold.

Finally, in order to allow unbiased comparison with observations we also add realistic observational errors to our mock observables, and derive statistics from the real and mock observations using the same bootstrapping method to marginalise over those errors. We describe our procedure for doing so in Appendix A.

# 2.4 Estimating electron densities in the LMC

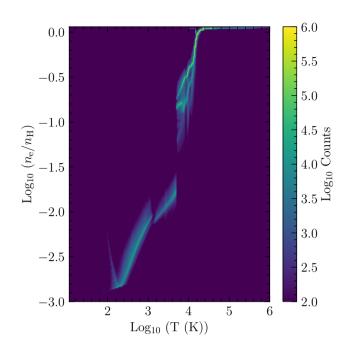
Our mock observables depend on the electron number density  $n_{\rm e}$ , and therefore generating realistic predictions requires careful consideration of the gas ionisation state, at a level beyond that provided by the "quick and dirty" model used in the on-the-fly simulation chemistry network. This first-order determination of the abundances of the various H and He ionisation states relies on the GRACKLE tables, which assume a uniform UV background characteristic of intergalactic space (Haardt & Madau 2012). This simple treatment overlooks the role of the Reynolds layer - a dense ISM region that shields galaxies from background radiation emitted by distant AGN that pervades extragalactic space (Reynolds 1993). Because of the presence of the Reynolds layer, the interstellar radiation field that prevails within galaxies is significantly softer than the field experienced by gas in the CGM. Our simulation includes both regions that are shielded by the Reynolds layer and regions outside it, and while the resulting spatial variation of the radiation field matters relatively little for the

<sup>3</sup> Note that our W simulation domain includes some contribution from the medium we have placed in the box to represent the MW CGM, which in principle we should remove from the DM (and the RM) since the observations are corrected for the MW foreground. In practice, however, we find that the contribution of material far from the LMC is minimal because it represents only the local CGM environment experienced by the LMC during its orbit, rather than the complete MW CGM intervening between us and the LMC. We therefore omit this correction for simplicity.

gas *temperature* – which is what is important for hydrodynamics, and thus why it is reasonable to use the simplifying assumption of a single radiation field when running the simulation – it matters a great deal for the ionisation fractions of predominantly neutral gas, and thus in turn for the RM and DM signatures that this gas produces. Quantitatively, we find that for gas at the densities ~  $0.1 - 1 \text{ cm}^{-3}$  typical of the warm neutral medium, switching between a Haardt & Madau radiation field and one more appropriate for ISM conditions only produces ~ 10% differences in the equilibrium temperature, but can yield almost order of magnitude differences in the ionisation fraction, enough to strongly alter synthetic DM and RM signals.<sup>4</sup> We must therefore post-process the simulation data to take into account these effects and obtain a more realistic model of the gas ionisation state.

Our procedure for doing so is as follows. We first generate a set of tables for equilibrium ionisation states as a function of gas density and temperature using CLOUDY (Chatzikos et al. 2023), following exactly the same procedure as for the GRACKLE library (Smith et al. 2016), but replacing the Haardt & Madau (2012) radiation field used by GRACKLE with a background radiation field with a spectral energy distribution (SED) following Black (1987), subject to extinction by a cold neutral slab with column density  $10^{21}$  cm<sup>-2</sup>, typical for the ISM (Stil & Israel 2002; Draine 2011; Saha et al. 2018). In this calculation we also set a cosmic ray ionisation rate of  $4.6 \times 10^{-16}$  s<sup>-1</sup> (Indriolo et al. 2007). This radiation and cosmic ray field are typical of ISM conditions, as opposed to the CGM and IGM conditions assumed in GRACKLE. The output of this calculation is a set of ionisation states as a function of density and temperature in exactly the same format as the GRACKLE tables, but for an ISM radiation field.

We then assume that ionisation conditions switch from CGM-like to ISM-like at some characteristic transition temperature  $T_{\rm Re}$  that characterises the Reynolds layer; we also experimented with placing the transition at a characteristic density and column density, and found that the results are nearly identical. We will calibrate the value of  $T_{\rm Re}$  below, but for the moment we simply assume we have a known value. Given this known value we now assign the ionisation state of each GIZMO gas particle to the equilibrium value specified in the CGM-like or ISM-like table based on its temperature. Our final step is then to add in the effects of photionisation feedback. As noted above, we implement this in the simulations using a Strömgren volume method, as described by Armillotta et al. (2019), following an earlier implementation from Hopkins et al. (2018b). To ensure that our post-processed electron fractions are consistent with this treatment of photoionisation, we implement a post-processing algorithm to apply a similar Strömgren volume calculation to our outputs. The steps in this algorithm are as follows: (1) sort all the slug clusters from largest to smallest ionising luminosity; (2) sort all predominantly neutral  $(n_e/n_{\rm H} < 0.5)$  gas particles from smallest to largest distance to the most luminous star, with ionising photon production rate  $\dot{N}_{\text{ion},*}$ ; (3) calculate the rate at which ionising photons must be supplied to maintain the nearest gas particle in a fully ionised state,  $\Delta \dot{N}_{ion,g} = \alpha_B n_e n_{H^+} V$ , where  $\alpha_B$  is the case B recombination coefficient evaluated at  $T = 10^4$  K,  $n_e$  and  $n_{H^+}$  are the number densities of electrons and protons assuming the particle is fully ionised, and V is the particle volume; (4) if  $\Delta \dot{N}_{ion,g} < \dot{N}_{ion,*}$ , then (4a) change the chemical composition of the particle to fully ionised and remove it



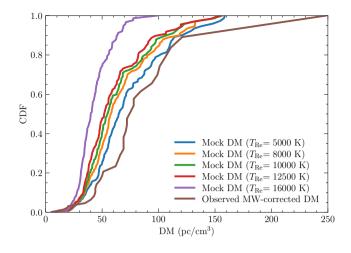
**Figure 2.** Example 2D histogram of the distribution of gas particles in the plane defined by gas temperature and number of free electrons per H nucleon, computed using the procedure described in Section 2.4. This example is for the final time snapshot of simulation W-2-6-M computed using  $T_{\text{Re}} = 5000$  K.

from the neutral particle list, deduct the photons available for the ionisation from the stellar budget (i.e., set  $\dot{N}_{\text{ion},*} - \Delta \dot{N}_{\text{ion},g} \mapsto \dot{N}_{\text{ion},*}$ ), and go back to step (4); otherwise (4b) remove the sLUG cluster from the list of clusters and proceed to the next most luminous one, until none are left. At the end of this procedure, we have a description of the ionisation state that self-consistently accounts for both the background and local massive stellar radiation fields.

Figure 2 shows an example of the joint distribution of free electrons per H nucleon,  $n_e/n_H$ , and temperature we compute via this procedure for the final snapshot of simulation W-2-6-M, using  $T_{Re} = 5000$ K. As expected, we see a clear break in the electron fraction at  $T_{Re}$ due to the change in radiation field at that temperature. Other features are essentially as expected: we see a band of high ionisation at T = 10000 - 15000 K driven by stellar photoionisation, and a transition to nearly complete ionisation above  $\approx 20000$  K due to collisional ionisation. The small break at  $\approx 3000$  K is due to the transition between the cold and warm neutral phases.

We now seek to calibrate our choice of  $T_{\text{Re}}$  by matching our synthetic DMs to the distribution observed for LMC pulsars; we use DMs rather than RMs for this purpose because the DMs depend only on  $n_e$  and not on  $\vec{B}$ . We therefore repeat the calculation illustrated in Figure 2 for a grid of values  $T_{\text{Re}}/\text{K} = (5000, 8000, 10000, 12500, 16000)$ , again using simulation W-2-6-M; we choose this run because it is the most high-resolution case we have with wind. For each calculation, we generate synthetic DMs to the same set of synthetic pulsar positions following the procedure described in Section 2.3, and then plot the cumulative distribution function (CDF) or DMs, which we compare to the observed distribution taken from Johnston et al. (2021). We show this comparison in Figure 3. As the plot shows, we obtain the best

<sup>&</sup>lt;sup>4</sup> The EM is much less sensitive to this effect, because its  $n_e^2$  dependence means that the signal is dominated by gas that is almost completely ionised, and the choice of background radiation field only leads to substantial differences in gas that is mostly neutral.



**Figure 3.** CDF of observed MW-corrected DM (green) and the corresponding distribution of mock DMs generated from W-2-6-M at several different values of  $T_{\rm Re}$ , as indicated in the legend – see text of Section 2.4 for details. We see that, while the difference between the simulated CDFs is not strongly dependent of  $T_{\rm Re}$ , agreement is best for  $T_{\rm Re} = 5000$  K.

agreement for  $T_{\text{Re}} = 5000$  K, and we therefore adopt this value for the remainder of our analysis in this paper.

# **3 RESULTS**

Here we report the results of our simulations. We first present a qualitative overview of the outcome to orient the reader in Section 3.1. We then carry out a detailed comparison of RM statistics between simulations and observations in Section 3.2. We explore the effects of ram pressure on gas properties and the 3D magnetic field structure, and the corresponding RM signatures, in Section 3.3. Finally, in Section 3.4 we address the question of which gas phase is being probed by the RM observations.

# 3.1 Overview of simulation outcomes

All our simulations undergo an initial burst of star formation before settling to a relatively steady-state regime after  $\approx 150$  Myr. We show examples of the star formation history for two example simulations in Figure 4, but the results for all simulations are qualitatively similar, with no strong dependence on the initial magnetic field configuration or presence or absence of a wind from the MW CGM. In steady-state, the SFRs in our simulations are  $\approx 0.1 - 0.2 \text{ M}_{\odot} \text{ yr}^{-1}$ , in good agreement with observational estimates for the LMC (e.g., Maschberger & Kroupa 2010; Jameson et al. 2016).

Figure 5 shows the mass-weighted mean density averaged in faceon and edge-on projection through the simulated LMC after 500 Myr of evolution, comparing two example simulations, one isolated (I-2-6-M) and with a wind (W-2-6-M); we select these two because their overall outcomes are reasonably typical of other isolated and wind cases. For the purpose of making this plot for the W simulations, we rotate particle position about the LMC centre by the rotation matrix

$$R = \begin{bmatrix} 0.59 & 0 & 0.8\\ 0 & 1 & 0\\ -0.8 & 0 & 59 \end{bmatrix},$$
(12)

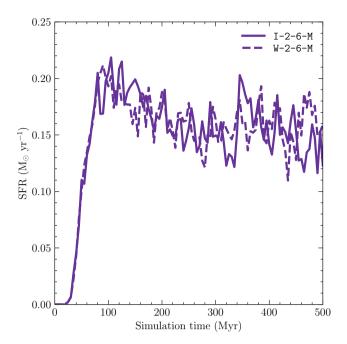
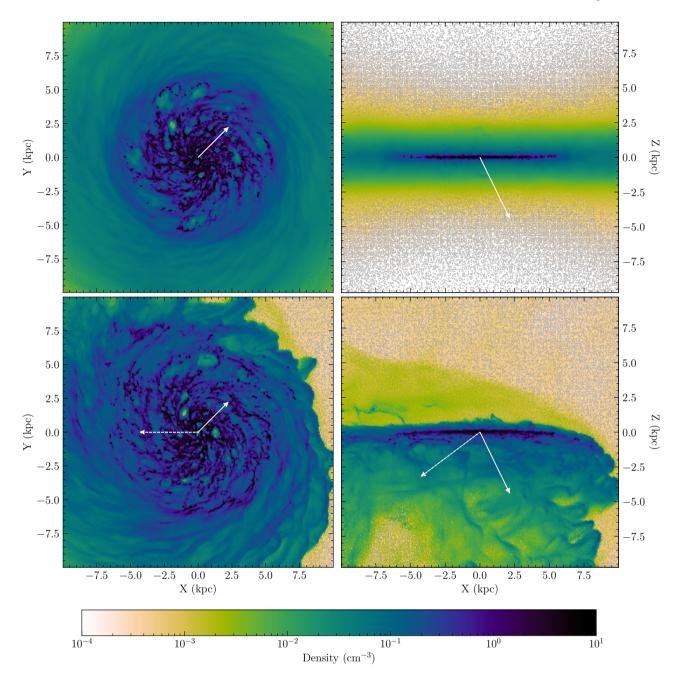


Figure 4. Star formation rate (SFR) as a function of time in simulations I-2-6-M (solid) and W-2-6-M (dashed). We do not see any significant differences between the two cases, and the steady-state SFR of  $0.1-0.2~M_{\odot}~yr^{-1}$  is close to that of the observed LMC.

which is the inverse of the rotation by  $53.57^{\circ}$  we apply to the initial conditions; this serves to rotate the LMC back to an orientation where its angular momentum vector lies in the  $\hat{z}$  direction. In terms of Euler angles, this is equivalent to  $\alpha = 0^{\circ}$ ,  $\beta = 53.57^{\circ}$ , and  $\gamma = 0^{\circ}$ .<sup>5</sup>

We see from Figure 5 that the dense interstellar medium of our simulated LMC extends approximately 5 kpc from the galactic centre, consistent with HI observations (Kim et al. 1998; Staveley-Smith et al. 2003). Supernova feedback introduces turbulence that creates a flocculent structure throughout the ISM. The isolated case contains low-density material extending to larger radii, but in the W case ram pressure stripping has removed much of the diffuse material. Removal begins with the hot, diffuse gas that is more weakly gravitationally bound (Balogh & Morris 2000), and then advances outside-in as the simulation progresses, consistent with observational inferences from truncated discs (Warmels 1988; Cavatte et al. 1990; Vollmer et al. 2001; Lee et al. 2022). The ram pressure, however, is insufficient to remove the denser ISM components, due to the LMC's substantial mass, relatively modest velocity through the MW CGM, and the relatively low ambient CGM density. In the W case, the edge-on projection reveals a dense tail extending  $\sim 15$  kpc below and to the left of the LMC (in the orientation of the projection shown), marking the trajectory of the stripped material and giving it a jellyfish-like appearance; as shown in the Figure, our line of sight to the LMC intersects this tail of material, which means that it can contribute to the line-of-sight integrated EM, DM, and RM. There is a corresponding bow shock above and to the right (Bekki 2009; Ebeling et al. 2014;

<sup>5</sup> Note that this is slightly different from the rotation used in Equation 10, which has  $\gamma = 255^{\circ}$ ; both rotations align the angular momentum vector with the *z* axis, but the one given in Equation 10 also applies an additional rotation about the *z* axis so that the wind velocity vector is properly aligned relative to the line of sight from the Milky Way to the LMC.



**Figure 5.** Mass-weighted mean density along a LOS of 30 kpc for simulations I-2-6-M (top) and W-2-6-M (bottom) after 500 Myr of evolution. The left column shows a face-on projection, while the right column shows an edge-on projection; positions shown are relative to the LMC centre. We see that the presence of a wind in the W run adds dense turbulent eddies in the outskirts of the disc (face-on plots) and stripped material extending ~ 15 kpc off-plane (edge-on plots). These plots are in a frame where the LMC angular momentum vector is aligned with the +z direction, and the wind direction is  $-0.8\hat{x} - 0.6\hat{z}$ , as indicated by the dashed white arrows. In the reference frame of the plot, the vector pointing from the LMC centre to the observer is  $0.4\hat{x} - 0.4\hat{y} - 0.82\hat{z}$ , and we show the projection of this vector onto the planes of the plot with the solid white arrow.

McPartland et al. 2015; Rohr et al. 2023). Ram pressure can compress the gas, especially on the leading edge, and we see marginal evidence for this towards the leading edge in the off-plane direction.

Figure 6 shows the time evolution of the magnetic fields for the same two runs as shown in Figure 5 at intervals of 125 Myr. Since the initial turbulent field  $(6 \mu G)$  is 3 times stronger than the initial smooth field  $(2 \mu G)$ , the leftmost panels showing the initial conditions contain mostly randomly oriented magnetic field vectors, as

expected. However, the rotation of the galaxy quickly orders this into predominantly azimuthal fields. Field strengths in the galactic centre rise rapidly due to strong compression caused by cooling, so that in steady state the magnetic field and density structures are strongly correlated.

The magnetic field evolution in our isolated (I-2-6-M) and wind (W-2-6-M) runs remain similar until 125 Myr, after which significant differences emerge in the outer regions ( $r \gtrsim 5$  kpc). At 500 Myr,

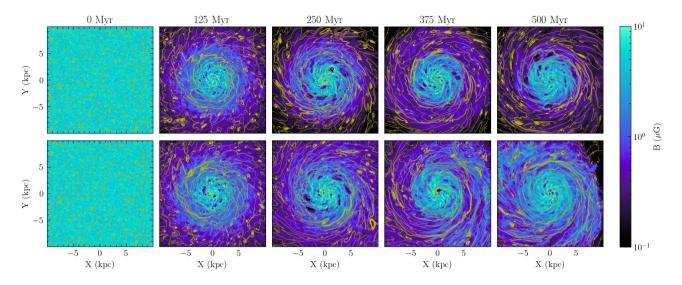


Figure 6. Density-weighted mean magnetic field as a function of time in the simulation (columns from left to right) for example isolated I-2-6-M (top) and wind W-2-6-M (bottom) simulations. The yellow overlaid curves show the direction of magnetic field lines while the background colour shows field magnitude. We see that the simulation evolves from predominantly turbulent initial fields to relatively ordered final fields. At late times we observe major differences in both the morphology and the strength of fields between the isolated and the wind cases.

while the isolated case shows weak magnetisation in the outskirts, the wind case exhibits stronger fields both in the outer regions and central 5 kpc. This enhancement stems from two effects: ram pressure compression leading to density and magnetic field amplification in central regions, and the LMC sweeping up outflows and magnetised circungalactic medium (CGM) material in the outer regions. The effect intensifies over time as the LMC traverses increasingly dense CGM regions (see Figure 1), leading to disc truncation on the leading edge while maintaining overall stronger magnetic fields. The magnetic field magnitude shows a strong correlation with gas density, as can be seen by comparing the bottom left panel of Figure 5 with the bottom right panel of Figure 6. Thus, a dense magnetised tail exists towards the trailing edge of the LMC. These features suggest that ram pressure stripping should leave observable signatures in RM maps of the LMC.

#### 3.2 Comparison with RM observations

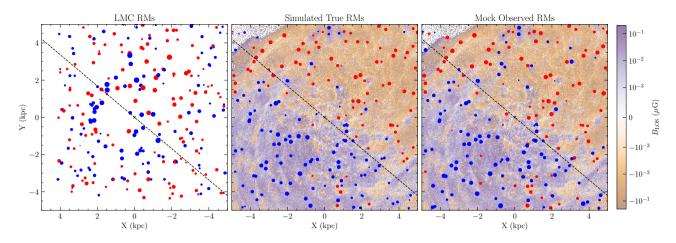
Having given a general overview of the outcome of our simulations, we now proceed with our primary goal, which is a quantitative comparison between our mock RM data for all simulations and real observations. For the latter, there have been two major studies of interest that report large samples of RM measurements through the LMC to polarised extragalactic background sources: G2005 and Livingston et al. (2024). Both use 1.4 GHz data from the Australia Telescope Compact Array (ATCA). While the more recent measurements from Livingston et al. offer a larger number of sources and thus higher spatial resolution, for the purposes of a statistical comparison we prefer to use the G2005 data. The reason is that these data, which were collected as part of the hydrogen line survey (Kim et al. 1998) and include 291 background sources across a 130 square degree field (of which roughly 100 cover the LMC), are randomly selected and thus offer a statistically-unbiased sampling of the LMC's magnetic field<sup>6</sup>.

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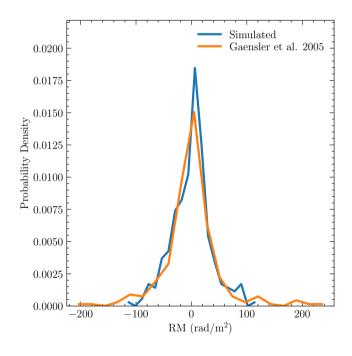
By contrast, Livingston et al. specifically chose sightlines toward regions of high H I column density, with the primary goal of detecting H I absorption. Since this selection was done by hand, there is no easy way for us to reproduce it in mock observations, and we therefore focus our statistical comparison of simulations and observations on the uniformly-sampled G2005 map despite its lower resolution. We will make use of the foreground-subtracted RM measurements from this data set for the remainder of this section.

The left panel of Figure 7 shows the G2005 RM map of the LMC, while the middle and right panels show mock RM maps from the final time snapshot of our simulations (computed as described in Section 2.3) for comparison. The middle panel shows the central RM values, and the right panel shows one of our realisations with our treatment of observational errors in the mock data (see Appendix A for details). In comparing our simulations to these measurements, we focus on three statistical quantities. The first two are the interquartile (25th - 75th percentile) range and the dispersion of RM values,  $I_{\rm RM}$  and  $\sigma_{\rm RM}$ , which characterise the typical strength of the LMC's magnetic field (along with the electron density). The IQR is more robust against outliers and thus we will give slightly more weight to it in our analysis, but we will report both  $I_{\rm RM}$  and  $\sigma_{\rm RM}$  in what follows. Our third statistic is an alignment fraction metric, which we use to characterise the fraction of RMs that have the "wrong" sign. In Figure 7, the dashed lines shown in each panel are drawn to be perpendicular to the LMC's line-of-nodes as determined from the rotation parameters of van der Marel (2004). If the LMC's magnetic field were purely azimuthal, the direction of the line-of-sight magnetic field would change sign across this line; if the magnetic field direction were parallel to the LMC's direction of rotation, given its orientation on the plane of the sky, we would expect regions to the left of the dashed line to show purely positive RM values, while regions to the right would have negative values. In fact, as Figure 7 shows, while there is a trend in this direction, it is clearly noisy, with significant numbers of RM measurements showing a sign opposite to the one we would expect for a simple azimuthal field geometry; the extent of this misalignment therefore characterises the extent to which the magnetic field displays turbulent structure that deviates from a

<sup>&</sup>lt;sup>6</sup> There remain biases in *detection* of polarisation, as opposed to target selection, but these are easier to model, and we will do so below.



**Figure 7.** The G2005 RM map (left), a sample mock RM with central RM values map from run W-2-6-M (middle), and a sample mock RM map in a realisation where we include simulated observational errors from run W-2-6-M (right). In the leftmost panel, blue (red) circles show positive (negative) RMs, with the size of the circle is  $\propto$  |RM|<sup>0.5</sup>, with the largest circle having a magnitude of  $\sim$  250 rad/m<sup>2</sup>. The dashed lines show the magnetic line of nodes, which is perpendicular to the line of nodes of the LMC's rotation as seen from the Sun, computed using the LMC geometry and kinematic model of van der Marel (2004). If the LMC's magnetic field were purely azimuthal, RMs should flip signs from positive to negative across this line. The mock RM maps in the rightmost two panels are overlaid on a background showing the true volume-weighted mean LOS (10 kpc depth) magnetic field. Comparing the middle and the right panel shows that the inclusion of simulated observational error in the treatment of mock RM data can change the value and alignment fractions of the dataset.



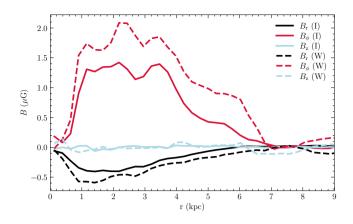
**Figure 8.** PDFs of RMs from the two leftmost maps shown in Figure 7. The comparison of observed and mock PDFs demonstrates that the simulation W-2-6-M does a good job of reproducing the observed LMC RM distribution.

simple ordered, azimuthal geometry. We quantify this by defining the alignment fractions  $p_{\rm RM}^+$  and  $p_{\rm RM}^-$  as the fraction of positive and negative RMs on their expected sides, i.e.,  $p_{\rm RM}^+$  represents the fraction of measurements to the right of the line of nodes shown in the left panel of Figure 7 that do in fact show positive RM, and similarly for  $p_{\rm RM}^-$ . A completely random RM distribution would have 50% alignment fraction, while a purely azimuthal field would have 100%.

We compute our three statistics from the mock and real observa-

tions using the analysis method outlined in Appendix A to properly marginalise over the uncertainties. The effect of these uncertainties is clear from the middle and right panels of Figure 7, where we see different RM values with more misalignment in the realisation that accounts for the observational errors. For the observations, this analysis yields  $\sigma_{\rm RM} = 55.54 \pm 1.98 \text{ rad/m}^2$ ,  $I_{\rm RM} = 48.5 \pm 2.13$ rad/m<sup>2</sup>,  $p_{\rm RM}^+ = 0.52 \pm 0.02$ , and  $p_{\rm RM}^- = 0.54 \pm 0.02$ ; for the mock observations, we analyse the final time snapshot of each run, and report the resulting values in Table 1. Here we can start to see the effects of different initial magnetic fields on the observables like the RM: when we initialise the simulation with purely turbulent magnetic fields (as is the case for runs I-0-2-L and I-0-12-M), the alignment fractions are close to 0.5, meaning a randomly distributed RM map. However, the typical magnetic field strengths we find at the ends of these runs are too small due to efficient cancellation of RM contributions from regions in which the field is oppositely-directed, leading to  $\sigma_{\rm RM}$  and  $I_{\rm RM}$  values that are too small compared to what we observe. When we initialise the magnetic fields to be purely azimuthal (I-2-0-L, W-2-0-L), the alignment fractions (~ 0.85, 0.89),  $\sigma_{\rm RM}$  (~ 66, 101 rad/m<sup>2</sup>), and  $I_{\rm RM}$  (~ 82, 139 rad/m<sup>2</sup>) are too high compared to the observations; the high  $\sigma_{\rm RM}$  and  $\mathcal{I}_{\rm RM}$  values occur because the ordered field amplifies significantly as the simulation runs, yielding high RM magnitudes in both the positive and negative directions. This makes it clear that recreating the observed alignment fractions,  $\sigma_{RM}$ , and  $I_{RM}$  will require a mix of turbulent and ordered fields.

Examining the various mixed-field values we have tried, we find that the case with a wind where the turbulent fields are 3 times stronger than the ordered fields in the initial conditions – run W-2-6-M – reproduces the dispersion of RMs, interquartile range of RMs, and the alignment fraction reasonably well. We show the distribution of RM values for this run in Figure 8, demonstrating that this run provides a very good match to the observations. There is an excellent match between the observed  $I_{\rm RM} = 48.5 \pm 2.13 \text{ rad/m}^2$  and W-2-6-M  $I_{\rm RM} = 47.32 \pm 2.23 \text{ rad/m}^2$ ; agreement is slightly less good for  $\sigma_{\rm RM}$ (40.48±1.33 rad/m<sup>2</sup> simulated versus 55.54±1.98 rad/m<sup>2</sup> observed), but since this quantity is not as robust as  $I_{\rm RM}$  against outliers, and



**Figure 9.** Volume-weighted mean magnetic fields averaged over thin cylindrical shells with thickness 0.25 kpc and height 0.5 kpc in runs I-2-6-M (solid lines) and W-2-6-M (dashed lines), which are identical except that the latter includes the wind due to the MW halo and the former does not. Different colours show the three components of the field in a cylindrical coordinate system where the angular momentum axis of the simulated LMC is oriented in the  $\hat{z}$  direction. There is an evident increase of almost 50% in the azimuthal ( $B_{\phi}$ ) and radial ( $B_{r}$ ) magnetic field strengths in the presence of wind.

we can be seen in Figure 8 that a number of outliers with very high RM are present in the data, we consider this run a good match overall to the observations. Most of the subsequent scientific discussion will therefore revolve around this case unless otherwise stated.

# 3.3 On the importance of ram pressure for LMC rotation measures

Now that we have identified a simulation that reasonably reproduces observations of the LMC, we can use it to understand the physical origins of features of those observations. We first do so with respect to the effects of ram pressure from the MW halo on the LMC, which we assess by comparing our wind simulation that best matches the data (W-2-6-M) with the corresponding simulation with identical initial conditions in the LMC disc but without the MW halo (I-2-6-M), which matches the data less well.

Figure 9 shows the volume-weighted mean magnetic fields in cylindrical shells of height 0.5 kpc and thickness 0.25 kpc as a function of cylindrical radius in these two cases. The vertical  $(B_z)$ component of the magnetic field is negligible in both cases, meaning that in both, the field largely lies in the plane of the disc. Interestingly, the radial and azimuthal magnetic field components are  $\sim$  50% larger in the run including the MW halo wind, despite the field strength starting at identical values in the two simulations. One might be tempted to attribute this to gas compression leading to magnetic field amplification in the wind run, but we find that the relative increase in density in the wind run is significantly smaller than the amplification in magnetic field strength, i.e.,  $\rho_W/\rho_I < B_W/B_I$  at all radii, particularly in the outskirts (r > 4 kpc). Since even if the compression due to the wind is purely orthogonal to the field (the most favourable orientation) the field amplification is only linear in density, i.e.,  $B \propto \rho$ , this implies that compression alone cannot explain the magnetic field enhancement we measure.

Instead a more likely explanation for the enhanced field in W-2-6-M compared to I-2-6-M is that when the LMC traverses the magnetised MW CGM, it sweeps up material which gets deposited in its ISM

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and increases the field strength there. This effect becomes particularly evident past ~ 200 Myr in our simulation. This time is special for the following reason: the LMC is at all times travelling supersonically with respect to gas in the halo and thus drives a bow shock, but prior to this time, the halo material through which the LMC passes is sufficiently low density that the LMC is supersonic but not super-Alfvénic. In this state, the passage of the LMC through the halo is mediated by fast magnetosonic waves that run ahead of the galaxy and create a standoff between the galaxy and the bow shock. As the LMC traverses denser and denser material over time, however, the halo Alfvén speed drops and the standoff distance decreases, until eventually, around 200 Myr the LMC catches up with the strongly magnetised bow shock and accretes the swept-up material and the magnetic field associated with it.

Figure 10 shows slices through the magnetic field structure of the LMC and illustrates this phenomenon. The left panels show run I-2-6-M, and demonstrate that, in the absence of a wind, the galaxy has a mostly symmetric magnetic field structure across the disc plane. The top left panel shows that the field strength falls rapidly away from the midplane, and the bottom left panel shows that, in the disc plane where the field is strongest, the field is oriented mostly horizontally, residing in the disc plane. Immediately above and below the plane  $(|z| \ge 200 \text{ pc})$ , the field is turbulent, with no strong preference for a particular vertical component.

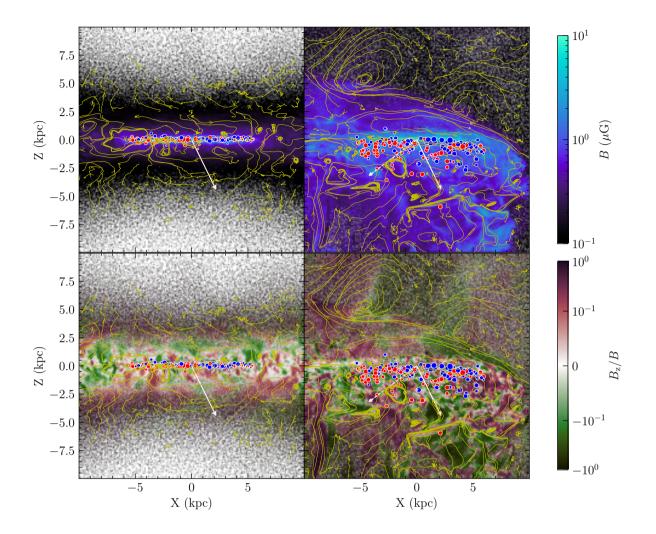
In contrast, the right panels of the figure show W-2-6-M, which has starkly different features, particularly away from the disc plane. First, there is a very strong asymmetry above and below the disc due to the wind being directed towards the bottom left of the figure (as shown by the white dashed arrow). As discussed above, this motion creates a bow shock above the disc with enhanced magnetic fields parallel to the interface between the background CGM and LMC material. The relative increase in the magnetic field magnitude and its alignment along the boundary is due to magnetic draping, a phenomenon where the magnetic fields are swept up and slip along the surface of a moving object such as a galaxy or a cloud as it interacts with the surrounding medium (e.g., see Figure 3 of Pfrommer & Dursi 2010, among many other examples - Lyutikov 2006; Ruszkowski et al. 2007; Dursi & Pfrommer 2008; Ruszkowski et al. 2014; Sparre et al. 2020; Jung et al. 2023). The region below the disc consists of a magnetised gas tail, extending  $\sim 15$  kpc off-plane, created by the material stripped from the LMC ISM. As a result of these effects, we see that the magnetic field in W-2-6-M is both stronger and more organised than in I-2-6-M.

These changes in the magnetic configuration have dramatic effects on the observed rotation measures. To quantify these effects, we begin by defining the RM-weighted mean position along any given line of sight i through the LMC as

$$\langle s \rangle_{\rm RM,i} = \frac{\int s n_{\rm e} |\vec{B} \cdot \hat{s}| \, ds}{\int n_{\rm e} |\vec{B} \cdot \hat{s}| \, ds},\tag{13}$$

where *s* is a coordinate measuring the position along the line of sight (c.f. Section 2.3.1), and we place s = 0 at the position where the LOS passes through the LMC plane and  $s = \infty$  at the location of the observer. The factor  $n_e |\vec{B} \cdot \hat{s}|$  appearing in this expression is simply the absolute value of the differential contribution made by the material at any given point *s* to the RM, and  $\langle s \rangle_{\text{RM},i}$  can therefore be used to characterise the average position along this line of sight from which the RM signal comes.

We show the (projected) mean positions defined by  $\langle s \rangle_{\text{RM},i}$  for each sightline as blue and red points in Figure 10. These are the same points shown for the mock observations in Figure 7 with blue and red colours for positive and negative RMs, respectively, and the



**Figure 10.** The top two panels show the density-weighted mean magnetic field strength averaged over a 30 kpc thick slab centred on the LMC centre for runs I-2-6-M (isolated case, left) and W-2-6-M (wind case, right) at the end of the simulation, in a frame where the LMC angular momentum vector is aligned with the +*z* direction and the wind direction is  $-0.8\hat{x} - 0.6\hat{z}$ , as indicated by the dashed white arrow. The bottom two panels show the ratio of vertical to total magnetic fields over the same region in the two runs. Yellow lines, which are the same in both panels, show magnetic field lines in the plane of the plot. In the reference frame of the plot, the vector pointing from the LMC centre to the observer is  $0.4\hat{x} - 0.4\hat{y} - 0.82\hat{z}$ , and we show the projection of this vector onto the plane of the plot with the solid white arrow. Blue (positive RM) and red (negative RM) circles mark the RM-weighted mean position along each of our 200 sample lines of sight (Equation 13) projected onto the plane of the plot. The sizes of the circles are scaled by  $|RM|^{0.5}$ . We see that, in the run including a wind from the LMC's passage through the MW CGM (right panels), the wind drags out the RM signature from the plane of the LMC to ~ 1 kpc off-plane in the direction of the tailwind and the observer.

size corresponding to the RM magnitude.<sup>7</sup> We see that the presence of wind causes a significant shift in the location of maximum RM contribution along the LOS towards the observer. A considerable fraction (> 40%) of sightlines have  $\langle s \rangle_{\text{RM},i} > 1$  kpc, while no sightlines have  $\langle s \rangle_{\text{RM},i} > 1$  kpc in the run without the wind. In the presence of wind along the observer LOS, the electron density decays much more slowly than in its absence, leading to an order of magnitude higher  $n_e$  at 1 kpc from the plane in the wind run, with correspondingly stronger magnetic fields. The combined effects of increasing electron density and magnetic field strength in the tailwind cause the mean location of the RM signature to shift towards the observer. We can see that this shift is a general phenomenon in Table 3, which reports the values of  $\langle s \rangle_{\rm RM}$  and  $\sigma_{s,\rm RM}$  for all our simulations, defined mathematically as

$$\langle s \rangle_{\rm RM} = \frac{\sum_i \int sn_e |\vec{B} \cdot \hat{s}| \, ds}{\sum_i \int n_e |\vec{B} \cdot \hat{s}| \, ds},\tag{14}$$

$$\sigma_{s,\text{RM}}^2 = \frac{1}{N_{\text{LOS}}} \sum_i \langle s \rangle_{\text{RM},i}^2,$$
(15)

<sup>&</sup>lt;sup>7</sup> Note that, in the projection shown in the plot, the LMC's line of nodes is tilted with respect to the normal to the plane of the figure. This tilt is the reason that the degree of separation between the positive RM (blue) and negative RM (red) sides of the galaxy is less visible here than it is, for example, in Figure 7.

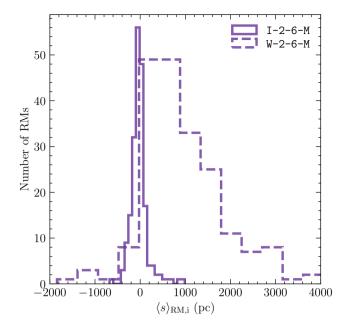


Figure 11. Histogram of RMs in isolated (solid) and wind (dashed) runs with respect to RM-weighted mean distance from the LMC plane. The distribution is symmetric around the plane in the isolated case, while it is skewed towards the observer in the wind case.

where the sums run over our  $N_{\text{LOS}} = 200$  sightlines.

Figure 11 shows a histogram of  $\langle s \rangle_{RM,i}$  values from I-2-6-M and W-2-6-M simulations, representing isolated and wind cases, respectively. Generally, for isolated cases,  $\langle s \rangle_{\text{RM},i} \approx 0$ ,  $\sigma_{s,\text{RM}} < 200$ pc, and Figure 11 shows that the distribution of  $\langle s \rangle_{RM,i}$  is narrowlypeaked near and symmetric about s = 0 in the isolated case I-2-6-M. This means that RMs in the absence of a wind are entirely set by material close to the galactic plane, and that the signal comes equally from above and below the plane (as would be expected, since there is nothing to break the symmetry). By contrast, runs including the Milky Way CGM wind have  $\langle s \rangle_{\rm RM}$  from ~ 0.2 – 1 kpc,  $\sigma_{s,\rm RM}$  ~ 1 kpc, and distributions of  $\langle s \rangle_{RM,i}$  that are highly skewed to positive values as can be seen for the example of run W-2-6-M from Figure 11. This implies that when an observer looks at rotation measure from the LMC, the dominant signature arises from the tailwind on the near side rather than from the plane of the disc as has been conjectured by G2005 and Livingston et al. (2024). Since the alignment fractions do not change significantly between the isolated and the wind cases, it also means that the magnetic field structure present in the disc is retained well out into the halo ( $\sim 1 \text{ kpc}$ ).

#### 3.4 Which gas phase is responsible for the RM?

Now that we have identified where along the LOS the RM signature arises, we can further identify which gas phase is responsible for the RM signature. For this analysis, we again use simulation W-2-6-M, which best matches the observations. For this purpose we will divide the gas into different phases – below we consider defining phases by temperature and ionisation fraction, and show that they all yield qualitatively-similar conclusions – and generate RM maps for each phase where we manually set the RM contribution of all other phases to zero; this lets us isolate the contribution of each phase to the total RM. We complement these maps with statistics to characterise the

 Table 3. Mean and dispersion of RM-weighted mean distance from the LMC plane.

Simulation name	$\langle s \rangle_{\rm RM}$ (kpc)	$\sigma_{s,\mathrm{RM}}~(\mathrm{kpc})$	
I-0-2-L	0.03	0.17	
I-2-0-L	0.03	0.09	
I-2-2-L	0.03	0.13	
I-2-6-L	0.02	0.16	
W-2-0-L	0.22	0.70	
W-2-2-L	0.44	0.88	
W-2-6-L	0.49	0.94	
I-0-12-M	-0.01	0.17	
I-2-6-M	-0.03	0.19	
W-2-6-M	0.94	1.41	
I-2-6-H	-0.01	0.17	

Columns: (1) name of simulation; (2) mean RM-weighted mean distance
along LOS from the galactic plane over all sightlines; (3) dispersion of
RM-weighted mean distances over all sightlines.

fractional contribution of each phase; we define these first of these statistics as

$$f_{\mathrm{RM},i,k} = \frac{|\mathrm{RM}|_{i,k}}{\sum_{k} |\mathrm{RM}|_{i,k}},\tag{16}$$

where the first index, i, indicates a particular LOS, and second index represents a particular phase of interest; the quantity in the denominator is the total RM along a given LOS. Thus Equation 16 quantifies the fractional contribution of some particular gas phase k to the total RM signal measured along some sightline i. We further define

$$\langle f_{\mathrm{RM},k} \rangle = \frac{\sum_{i} f_{\mathrm{RM},i,k} |\mathrm{RM}_{i}|}{\sum_{i} |\mathrm{RM}_{i}|},\tag{17}$$

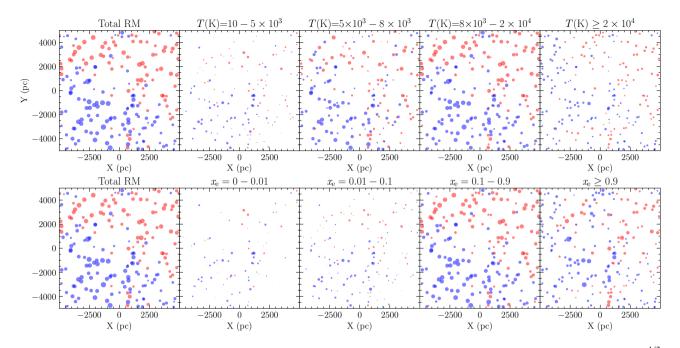
as the average contribution of each phase to the RM over all sightlines i, weighted by the RM magnitudes of all phases along each LOS,  $|\text{RM}_i|$ . Our final statistic is the "same sign fraction"  $f_{\text{RM-same}}$ , which we define as the fraction of sightlines for which the sign of the RM produced by a given phase matches the sign of the net RM over all phases along that sightline. In formal mathematical terms, we define this quantity as

$$f_{\text{RM-same},k} = \frac{1}{N_{\text{LOS}}} \sum_{i} \Theta \left( \text{RM}_{i,k} \, \text{RM}_{i} \right), \tag{18}$$

where RM<sub>i</sub> is the total RM along sightline *i* summing over all phases, and  $\Theta(x)$  is the Heaviside step function, which returns 1 when the argument is positive and zero when it is negative. Thus, a low value of  $f_{\text{RM-same},k}$  implies that the RM from gas in phase *k* is opposite in sign to the overall RM on a large fraction of sightlines.

We show RM maps generated using two different ways of dividing up gas phases in Figure 12; the maps in this figure follow the same convention as in previous RM maps, with blue (red) indicating positive (negative) RM values, and with the sizes of the circles scaled to  $\propto |\text{RM}|^{1/2}$ . We also report the corresponding summary statistics for these phase divisions in Table 4.

In the top row of the figure, the gas is categorised based on its temperature. The leftmost panel shows the overall RM without any categorisation, and is thus identical to the RM plot shown in the middle panel of Figure 7. The remaining panels show, from left to right, RM maps from gas with temperatures 10-5000 K, 5000-8000



**Figure 12.** RM maps due to gas with certain gas properties where blue (red) show positive (negative) RM values with the magnitude scaled to  $\propto |\text{RM}|^{1/2}$  and the largest circle corresponds to  $\sim 130 \text{ rad/m}^2$ . The top row panels show gas categorisation based on its temperature. The leftmost panel is the overall RM map while the second, third, fourth, and fifth panels show RM maps from gas with temperatures between 10 - 5000 K, 5000 - 8000 K, 8000 - 20000 K, and  $\geq 20000 \text{ K}$ , respectively. The bottom row panels show gas categorisation based on its ionisation fractions ( $x_e = n_e/n_H$ ) where the leftmost panel is overall RM map again while the second, third, fourth, and fifth panels correspond to ionisation fractions between  $0 - 0.01, 0.01 - 0.1, 0.1 - 0.9, \text{ and } \geq 0.9$ , respectively. These categories are carefully chosen to represent different ISM phases like the cold neutral medium, warm neutral medium, warm partially ionised medium, warm ionised medium. In general, we find that the RM signature dominates from the warm ionised medium irradiated by the hard-UV photons from the extragalactic background.

Temperature (K)	All T	$10 \le T < 5000$	$5000 \le T < 8000$	$8000 \le T < 20000$	$T \ge 20000$
$\langle f_{\mathrm{RM},k} \rangle \%$ $f_{\mathrm{RM-same},k} \%$	96.69 100.0	1.9 56.0	28.21 75.0	64.85 93.5	5.04 75.5
$x_{\rm e} \left( n_{\rm e}/n_{\rm H}  ight)$	All <i>x</i> <sub>e</sub>	$0 \le x_{\rm e} < 0.01$	$0.01 \le x_{\rm e} < 0.1$	$0.1 \le x_e < 0.9$	$x_{\rm e} \ge 0.9$
$\langle f_{\mathrm{RM},k} angle$ % $f_{\mathrm{RM-same},k}$ %			1.83 56.5	72.81 93.5	24.57 74.5

The top part of the table shows gas divided into phases by temperature *T*, the bottom by electron abundance  $x_e = n_e/n_{\rm H}$ . The first row in each section reports the fractional contribution  $\langle f_{\rm RM,k} \rangle$  for a given phase averaged over all sightlines (Equation 17), and the second row shows the same-sign fraction  $f_{\rm RM-same,k}$  (Equation 18), which indicates the fraction of sightlines for which the sign of the RM for that phase matches the sign of the total RM. Columns show, from left to right, these quantities summed over all phases, and then for gas that lies in the indicated range of *T* or  $x_e$ . Note that fractional contribution  $\langle f_{\rm RM,k} \rangle$  over all phases need not be exactly unity, because  $\langle f_{\rm RM,k} \rangle$  is normalised by the total RM, which is only equal to the sum of the individual phase RMs if all phases have the same sign (c.f. Equation 16).

K, 8000 – 20000 K, and  $\geq$  20000 K. We choose these temperature ranges to roughly divide the ISM into cold and unstable neutral medium (CNM and UNM), warm neutral medium (WNM), warm ionised medium (WIM), and hot ionised medium (HIM), respectively (Begelman 1990; Heiles & Troland 2003; Kanekar et al. 2003; Cox 2005; Roy et al. 2013; Murray et al. 2015, 2018; Bhattacharjee et al. 2023).

From both visual inspection and their low  $\langle f_{\text{RM},k} \rangle$  and  $f_{\text{RM}-\text{same},k}$ values (Table 4), it is clear that the CNM / UNM and HIM temperature ranges contribute negligibly to the overall RM. This is expected: in the cold medium the ionisation fraction is low, leading to a low electron density, while in the HIM the gas is fully ionised but the overall density is very low. By contrast, the WNM temperature regime contributes non-negligibly,  $\langle f_{\text{RM},k} \rangle \approx 28\%$ . Gas in this temperature range is too cool to have significant thermal ionisation, but is assumed to form part of the Reynolds layer in our treatment (c.f. Section 2.4 and Figure 2), and thus to be irradiated by the harder extragalactic background radiation field rather than the softer ISRF. This leads to non-thermal ionisation levels high enough to produce a notable RM contribution. However, the majority of the RM,  $f_{\rm RM} \approx 65\%$ , comes from WIM gas with temperatures in the range 8000 - 20000 K. This temperature regime sees high ionisation levels due to the hard-UV radiation, photoionisation due to massive stars, and, at the very upper end of the temperature range, collisional ionisation.

The bottom row categorises gas based on its electron fraction  $x_e = n_e/n_H$ , where  $n_H$  is the number density of H nuclei; this quantity ranges from 0 to  $\approx$  1.2, with the latter case corresponding to full ionisation of both H and He. As in the top row, the leftmost panel shows the total RM over all phases, and in the remaining panels we break the gas into bins, from left to right, with  $x_{e} = 0 - 0.01$  (mostly CNM and UNM), 0.01-0.1 (mostly WNM), 0.1-0.9 (warm gas that is partially ionised by the extragalactic background rather than strong local sources), and > 0.9 (WIM produced by strong stellar ionisation, together with thermally-ionised hot gas). We see that the dominant RM signature comes from partially-ionised gas with  $x_e = 0.1 - 0.9$ ; this phase has  $\langle f_{\text{RM},k} \rangle \approx 73\%$ , and  $f_{\text{RM-same},k} \approx 94\%$ . The fully ionised bin,  $x_e > 0.9$ , is the second-largest contributor, and the remaining weakly-ionised phases are negligible. This result indicates that the bulk of the RM signature arises from gas where temperatures are not high enough for full ionisation, nor low enough to be part of the neutral medium, but instead exist in a regime of partial ionisation driven by the hard-UV photons of the extragalactic background rather than from softer local stellar sources (which produce  $x_e \ge 1$ ). This points to an important result that the RM signature, at least for the LMC, arises from the Reynolds layer.

# **4 CONCLUSIONS**

In this study, we perform GIZMO-MHD simulations of an LMCanalogue galaxy in two distinct environments - isolated and with ram pressure stripping due to wind experienced as a result of its motion through the density varying MW CGM. We consider a range of field magnetic strengths and configurations, and carry out detailed post-processing of our simulation results – calibrated against DM data from pulsars – in order to determine what magnetic conditions best reproduce RM observations from the present-day LMC. Below, we summarise the main results.

(i) We succeed in identifying a configuration that shows very good agreement with the statistical properties of the observed LMC RM map; in particular, our simulation is able to reproduce the observed interquartile range, dispersion, and fraction of RM points which have

a sign opposite that which would be expected for a purely azimuthal field. In this simulation, the star-forming disc of the present-day LMC is characterised by a field that can reasonably be described as the sum of an ordered azimuthal component and a randomly-oriented turbulent component, with each component having a strength of  $\approx 2 \mu$ G.

(ii) The simulation that best reproduces the observations includes the effects of the LMC's interaction with the MW CGM, which in the frame comoving with the LMC manifests as a wind that ram pressure-strips the galaxy. We compare our simulation including this wind to a simulation of an otherwise-identical but isolated LMC to deduce the effect of the wind on the galaxy's physical properties and RM statistics. We find that the wind produces a substantial, ~ 50%, enhancement in the azimuthal and the radial polar components of the magnetic field, and that this, in turn, leads to a ~ 25% increase in the magnitude of dispersion of RM. Only a minority of this enhancement is due to ram pressure compression; instead, it primarily arises because the magnetised MW CGM is deposited onto the LMC ISM as the LMC moves through the MW halo.

(iii) The presence of wind also substantially modifies the physical location of the region responsible for producing the bulk of the RM signal. In the isolated case RMs probe a region very close to the LMC plane, but in the interacting case the region that drives the RM is shifted towards the observer by ~ 1 kpc, so that it lies in a region dominated by a tail of highly magnetised, warm ( $T \sim 10^4$  K), partially ionised (electron abundance  $x_e \sim 0.1 - 0.9$ ) material stripped from the LMC by the MW wind, and then partially ionised by exposure to the hard extragalactic radiation field that exists outside the LMC's Reynolds layer. This implies that RM measurements from background quasars through the LMC are probing magnetic fields in the tailwind of the LMC rather than the galactic plane as previously thought (e.g., G2005, Livingston et al. 2024).

This study represents a new approach to the problem of deriving accurate magnetic field strengths and geometries from RM observations: forward modelling via simulations and mock observations rather than backward modelling that attempts to reconstruct field data from projected quantities. This new approach will become increasingly important as newer, higher-resolution RM data arrive from ongoing radio surveys such as ASKAP POSSUM (Anderson et al. 2021; Vanderwoude et al. 2024). It is clear from our work that analysing these data using traditional backward modelling techniques may lead to significant misinterpretations as a result of the assumptions one is inevitably forced to adopt with this method. Forward modelling as we have performed here offers us the opportunity for more robust results.

That said, we would be remiss not to mention some caveats to our results that we plan to address in future work. One clear one is the absence in our simulations both of the SMC and of a prominent stellar bar in the LMC (which is likely at least in part due to tidal forcing by the SMC). These features can potentially alter the gas dynamics and thus the magnetic field configuration, and including an SMC will obviously become necessary if we seek to model RM measurements of the Magellanic Bridge as well as in the body of the LMC. And as always in numerical work, resolution is a concern; while our mass resolution of 250  $M_{\odot}$  in the simulation that best reproduces the data is extremely high by the standards of most cosmological or even isolated galaxy simulations, it is not sufficient to allow us to forego the use of subgrid models to handle supernova and photoionisation feedback, and offers only marginal resolution of the dense molecular phase of the ISM. While it is unknown to what extent these resolution limitations influence magnetic structure, future simulations should strive for higher resolution to allay any concerns. We will pursue such higher-resolution models in future work.

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# DATA AVAILABILITY

Data related to this work will be shared upon reasonable request to the corresponding author.

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# APPENDIX A: BOOTSTRAPPING PROCEDURE

This appendix outlines our bootstrapping method for analysing RM data from both observations and simulations, ensuring that we can compute statistics (e.g., outcome statistics mentioned in Table 2) on RM data sets properly marginalising over uncertainties, and do so in a manner that is consistent between real and mock observations.

Our first step when processing mock data is to generate realistic observational errors. To do so we first construct a kernel density estimate (KDE) of the distribution of  $1\sigma$  uncertainties using the set of uncertainties reported by G2005; we use SciPx<sup>8</sup> for this purpose. For each realisation (see below), we then draw a value from that KDE for each sightline in our mock RM map. At this point our mock and observed maps both consist of a series of  $N_{\text{LOS}}$  sightlines for which we have both a central estimate of the rotation measure and an associated uncertainty {RM<sub>i</sub>,  $\sigma_i$ }.

Our next task is, given data in this format, to derive central estimates and uncertainties for any statistic  $f(\{RM_i\})$  that can be computed on a set of RM measurements; for example, we can take the function f to be the variance function if we wish to compute the variance of RM, or the median function if we want to compute the median. Our bootstrapping method is the same regardless of the statistic we wish to evaluate, and it proceeds as follows. At each iteration, we generate a new realisation of the RM map in two steps:

<sup>&</sup>lt;sup>8</sup> https://docs.scipy.org/doc/scipy/reference/generated/ scipy.stats.gaussian\_kde.html

(i) Generate a new set of  $N_{\text{LOS}}$  {RM<sub>i</sub>,  $\sigma_i$ } pairs by drawing from the original sample *with replacement*.

(ii) For this new set of pairs, generate a new set of RM measurements  $\{RM'_i\}$  by, for each LOS produced in the previous step, drawing from a Gaussian distribution with mean  $RM_i$  and dispersion  $\sigma_i$ .

This first step accounts for uncertainties induced by the finite number of sightlines to which we have access, while the second accounts for the uncertainties induced by the measurement errors on each sightline. We then calculate our target statistic on this realisation of the RM map as  $f(\{RM'_i\})$ .

We repeat the above process N times, yielding N values of the statistic that we denote  $f(\{RM'_i\})_n$ . We then compute the mean and standard deviation of these N values,  $\langle f(\{RM'_i\})_n \rangle_N$  and  $\operatorname{std}(f(\{\operatorname{RM}'_i\})_n)_N$ . In order to ensure that the number of iterations N is large enough to yield an accurate estimate of the mean and standard deviation, we proceed by sample doubling. We first carry out this procedure with N = 32 trials, then repeat it for N = 64 trials, and compare the values of  $\langle f(\{\mathbf{RM}'_i\})_n \rangle_{32}$  and  $\langle f(\{\mathbf{RM}'_i\})_n \rangle_{64}$ . If these differ by less than 1% we consider the procedure converged and accept  $\langle f(\{\mathbf{RM}'_i\})_n \rangle_{64}$  and std $(f(\{\mathbf{RM}'_i\})_n)_{64}$  as our final estimates of the mean and variance of the statistic f. If they differ by more than 1%, we generate a sample of N = 128 iterations and check if  $\langle f(\{\mathbf{RM}'_i\})_n \rangle_{64}$  and  $\langle f(\{\mathbf{RM}'_i\})_n \rangle_{128}$  differ by less than 1%, and so forth, repeating the doubling procedure until two successive iterations differ by less than our 1% tolerance, at which point we accept the largest N values as our final estimates for the mean and standard deviation. In practice we find that most of our statistics reach convergence within 64-512 iterations.

For the simulated data, we must also marginalise over the first step of assigning error values to lines of sight by drawing from the KDE of observed errors. We do so by creating 100 different error realisations, i.e., 100 different {RM<sub>i</sub>,  $\sigma_i$ } data sets. We apply the full bootstrapping procedure to each realisation and average the resulting statistics to produce our final values. For observations this step is not necessary, since we have only a single uncertainty  $\sigma$  to go with each RM, and we therefore simply apply the bootstrapping process once with the actual measured errors.