

# Astrophysical Gas Dynamics

*TODAY:*

- *Sedov solution ( $\rightarrow$  recap)*
- *Magnetohydrodynamics (MHD)*



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# Supernova phases

## Energy-driven expansion

Shock speeds of about 1000 km/s

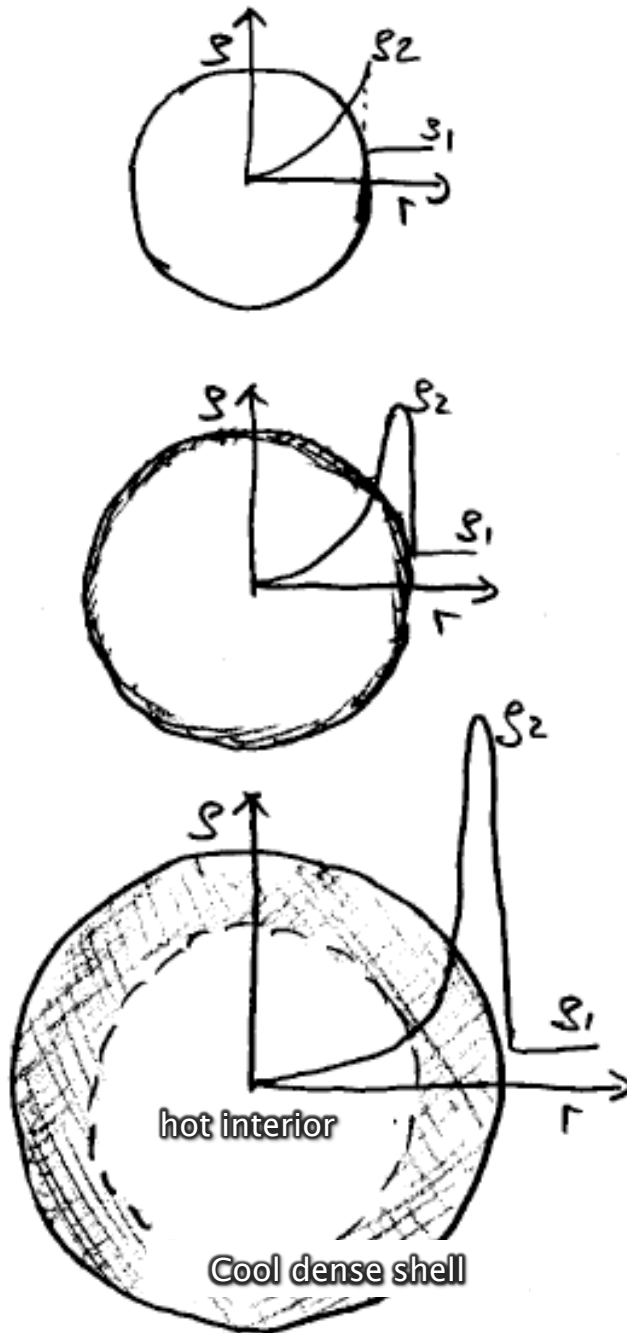
## “Snow-plow phase”

Cooling  $\rightarrow$  dense, thin shell forms and sweeps up more material;  
Thickness of shell  $\sim 1$  pc with  
density  $n \sim 1\text{--}100\text{ cm}^{-3}$

## Momentum-driven phase

Expansion eventually comes to a halt after about 30,000 yr, when momentum of swept-up material equals the initial momentum of the shell

Evolutionary sequence



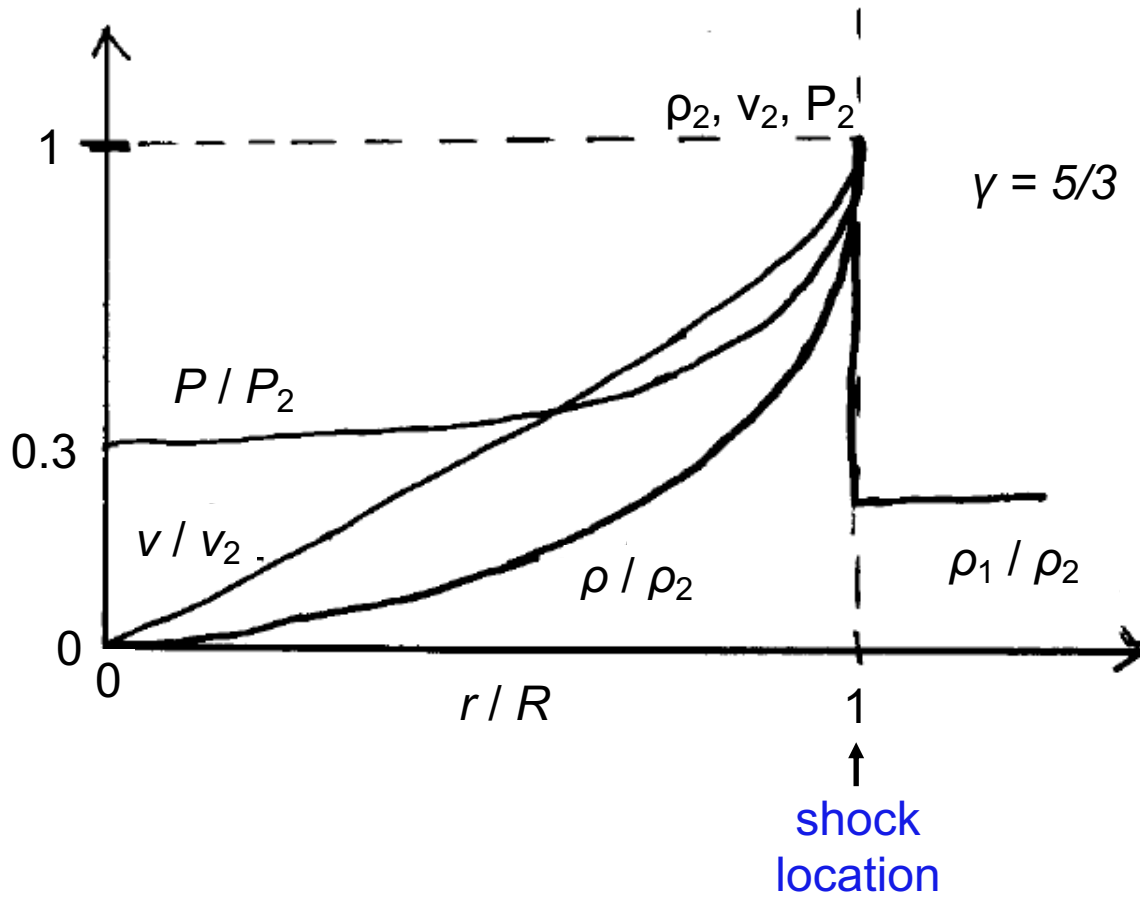


# Astrophysical Gas Dynamics

*TODAY:*

- *Supernova explosions (scalings  $\rightarrow$  recap)*
- *Sedov solution*

Self-similar Sedov solution for density, velocity, and pressure  
(shock wave expanding into uniform medium of density  $\rho_1$ )



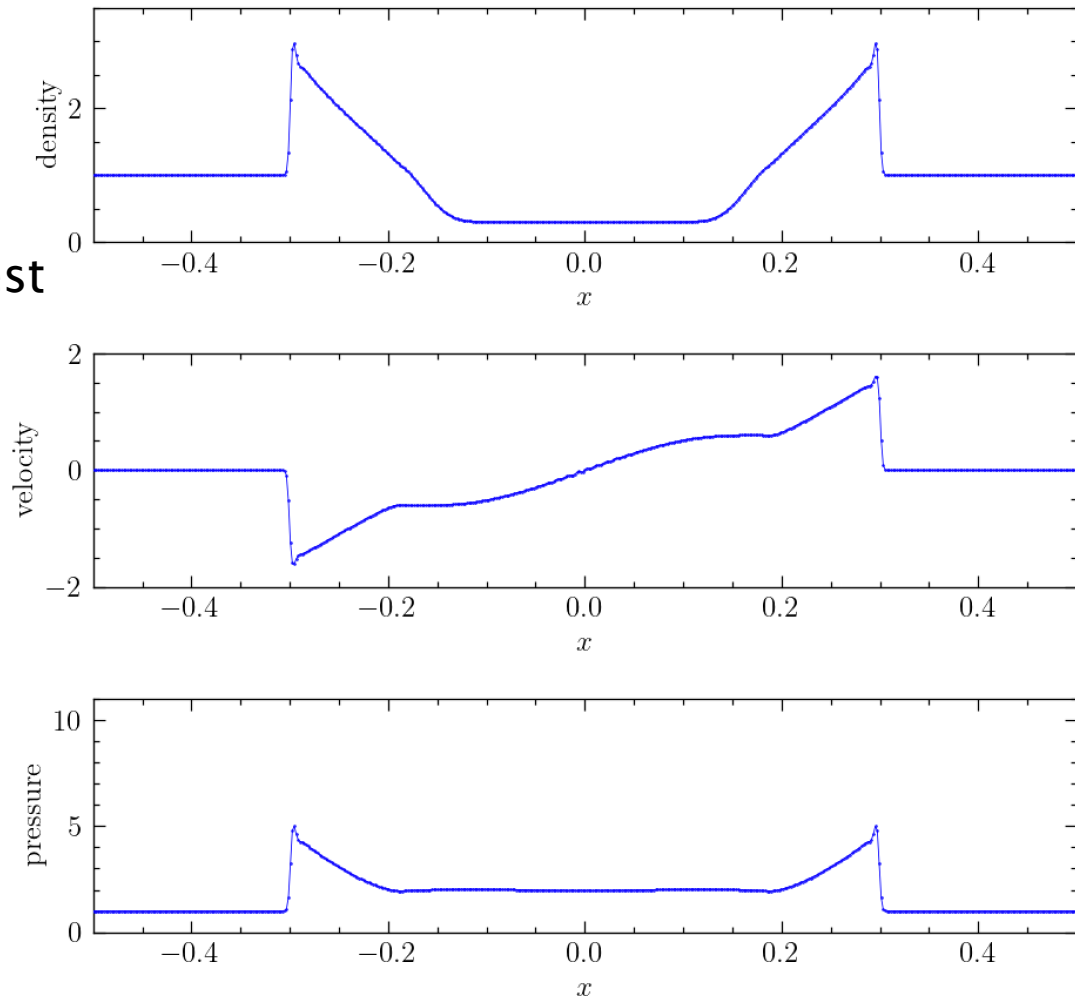
# Sedov explosion

- Python program to solve 1D/2D hydro equations:

[hydro.py](#)

- > ./hydro.py -h
- > ./hydro.py -sim sedov\_test

**Suggested: Modify the code to change the initial conditions, e.g., energy injection zone, grid resolution, etc.; compare to analytic solution**

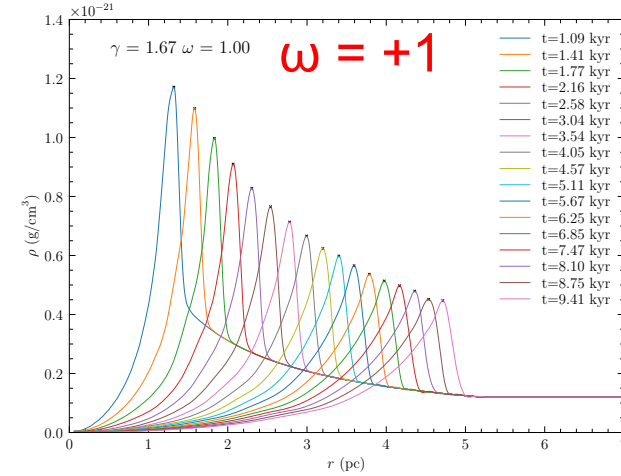
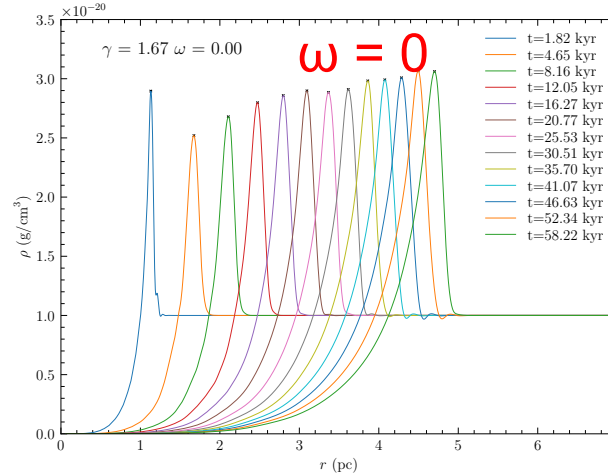
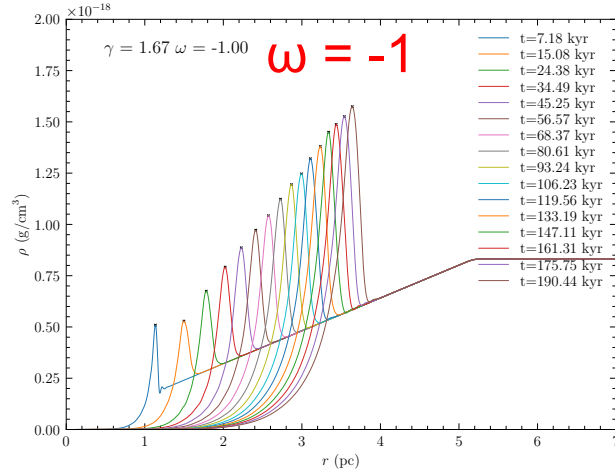


This code uses cfpack; you can simply do “[pip install cfpack](#)”

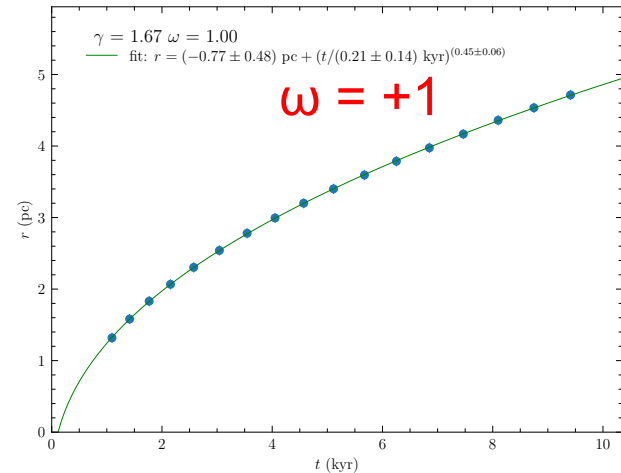
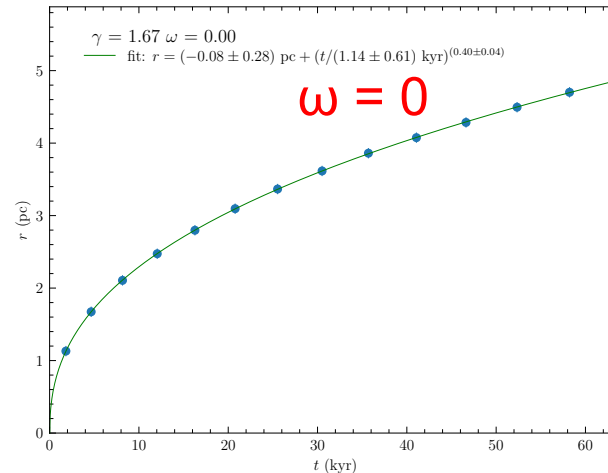
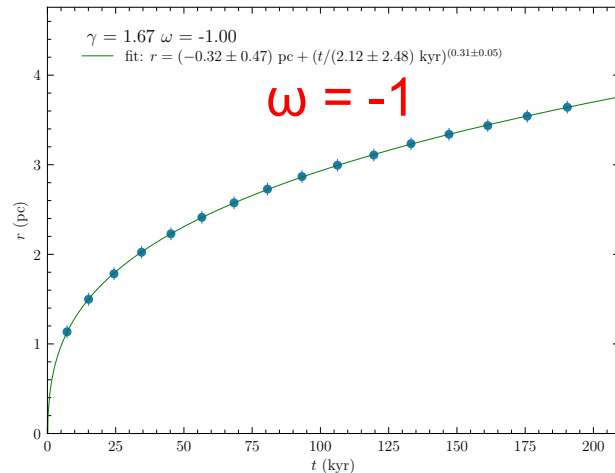
# Sedov solution for non-uniform medium with $\rho_{\text{amb}}(r) \sim r^{-\omega}$

(see Book 1994, for a summary and discussion of the analytic solutions)

## Density profiles $\rho(r)$

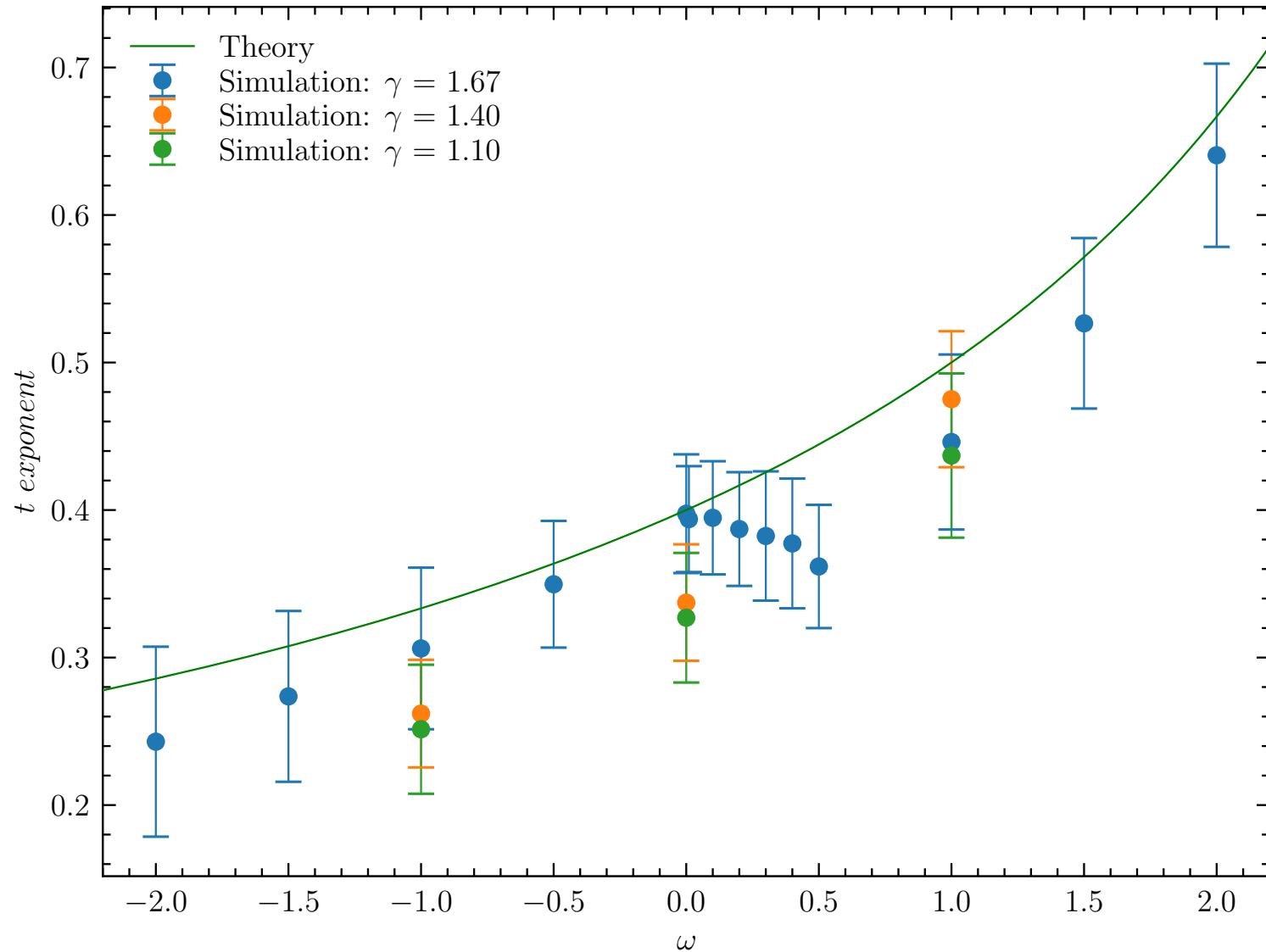


## Evolution of shell expansion radius $r(t)$



# Sedov solution for non-uniform medium with $\rho_{\text{amb}}(r) \sim r^{-\omega}$

(see Book 1994, for a summary and discussion of the analytic solutions)

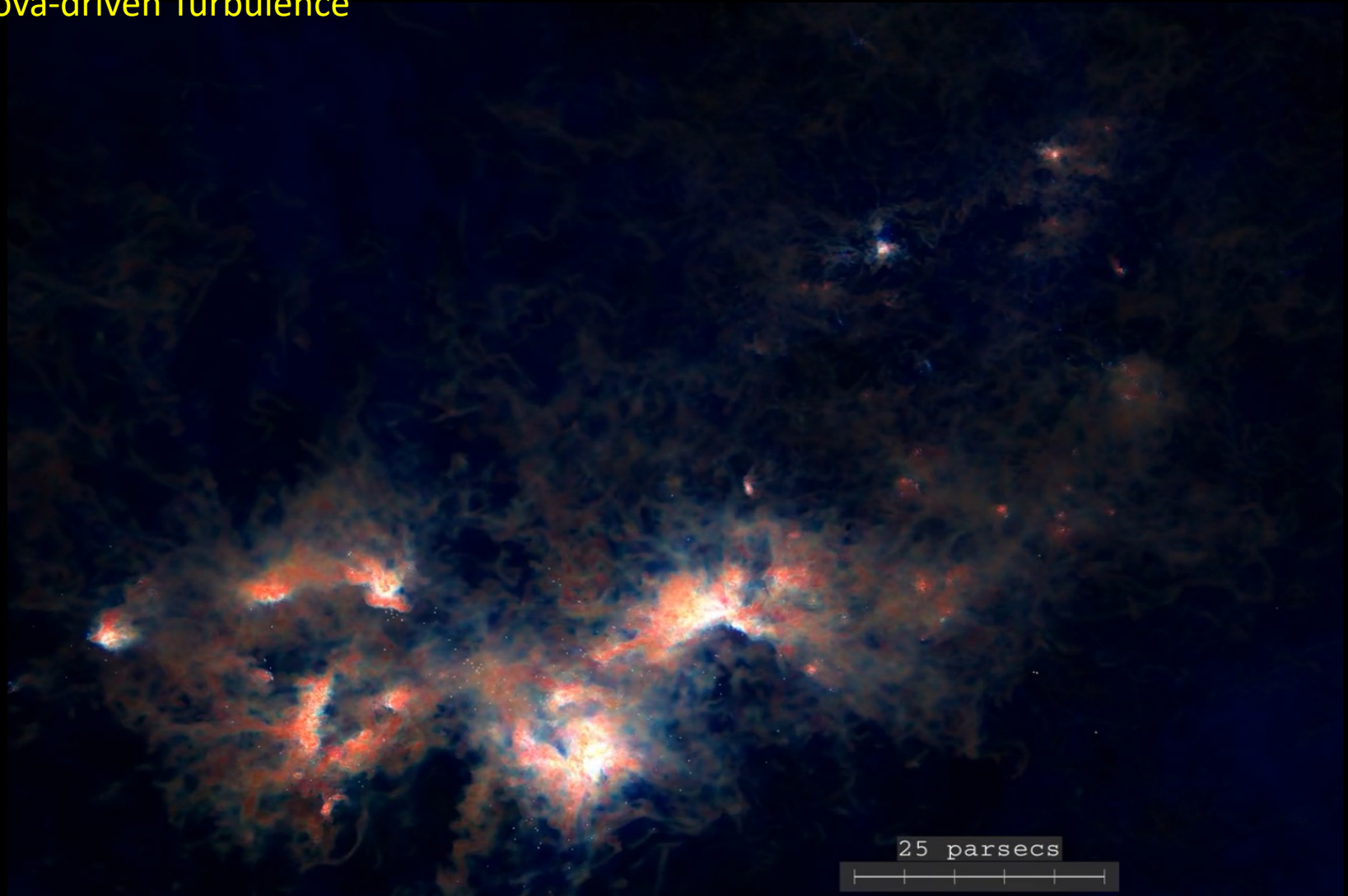


(Monica Bapna et al., in prep.)



# Supernova-driving of turbulence

## Supernova-driven Turbulence



(Padoan et al. 2016, 2017)

# Driving of turbulence by supernova explosions

## Comparison of Milky Way turbulence dissipation and SN injection rates

Turbulence energy dissipation rate:

$$\dot{e} \simeq -(1/2)\rho v_{\text{rms}}^3 / L_d = -(3 \times 10^{-27} \text{ erg cm}^{-3} \text{ s}^{-1}) \left( \frac{n}{1 \text{ cm}^{-3}} \right) \left( \frac{v_{\text{rms}}}{10 \text{ km s}^{-1}} \right)^3 \left( \frac{L_d}{100 \text{ pc}} \right)^{-1}$$

Supernova energy injection rate:

$$\begin{aligned} \dot{e} &= \frac{\sigma_{SN} \eta_{SN} E_{SN}}{\pi R_{sf}^2 H_c} \\ &= (3 \times 10^{-26} \text{ erg s}^{-1} \text{ cm}^{-3}) \left( \frac{\eta_{SN}}{0.1} \right) \left( \frac{\sigma_{SN}}{1 \text{ SNU}} \right) \left( \frac{H_c}{100 \text{ pc}} \right)^{-1} \left( \frac{R_{sf}}{15 \text{ kpc}} \right)^{-2} \left( \frac{E_{SN}}{10^{51} \text{ erg}} \right) \end{aligned}$$

( $\eta_{\text{SN}}$  is the fraction of kinetic energy per SN)

(1 SNU is about 1 SN per 50 years for the Milky Way)



# **Turbulence is key for Star Formation**

(Federrath & Klessen 2012; Federrath et al. 2016)

**Turbulence** → **Stars** → **Feedback**

**Magnetic Fields**

**Dynamics**  
(shear)

**Turbulence driven by**

- Shear
- Jets / Outflows
- Cloud-cloud collisions
- Winds / Ionization fronts
- Spiral-arm compression
- Supernova explosions
- Gravity / Accretion

**Solenoidal**

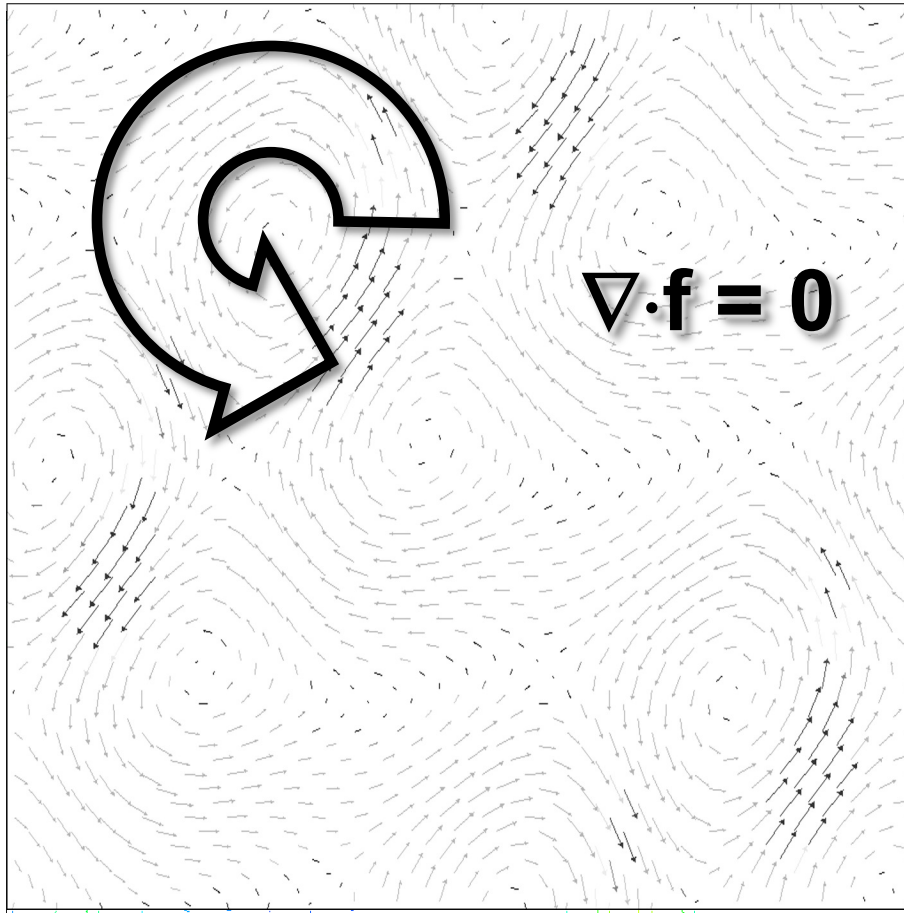
**Compressive**



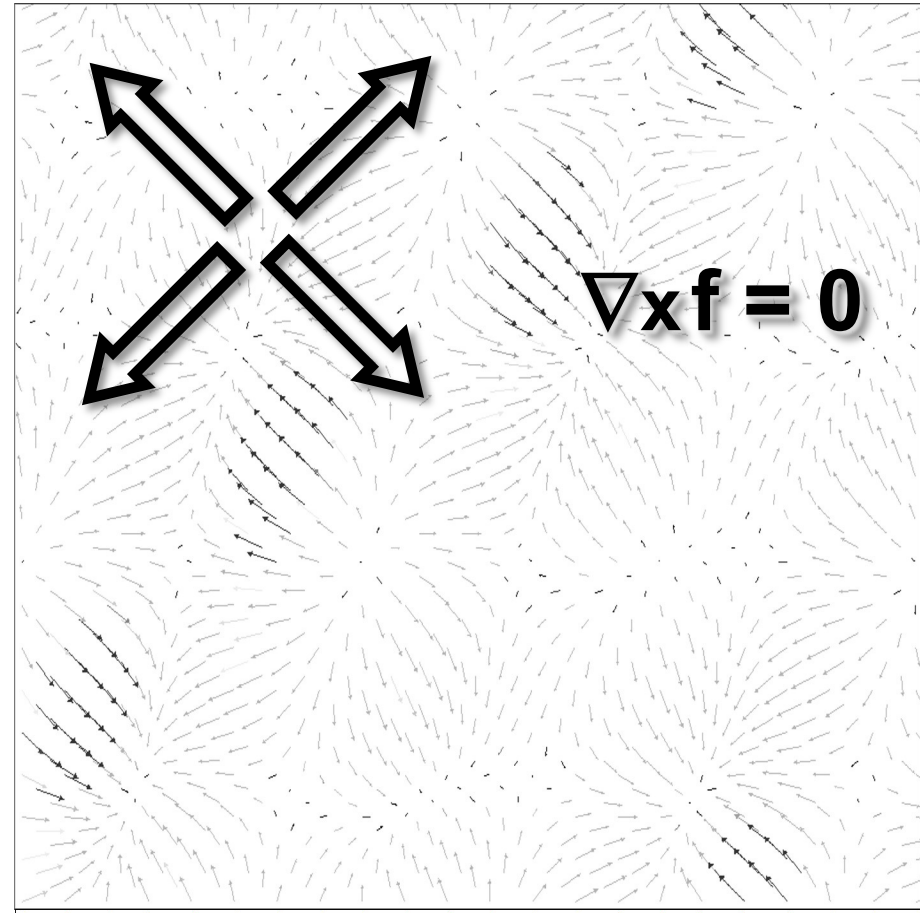
# Turbulence driving – solenoidal versus compressive

Ornstein-Uhlenbeck process (stochastic process with autocorrelation time)  
→ **forcing varies smoothly in space and time,**  
**following a well-defined random process**

**Solenoidal forcing**



**Compressive forcing**

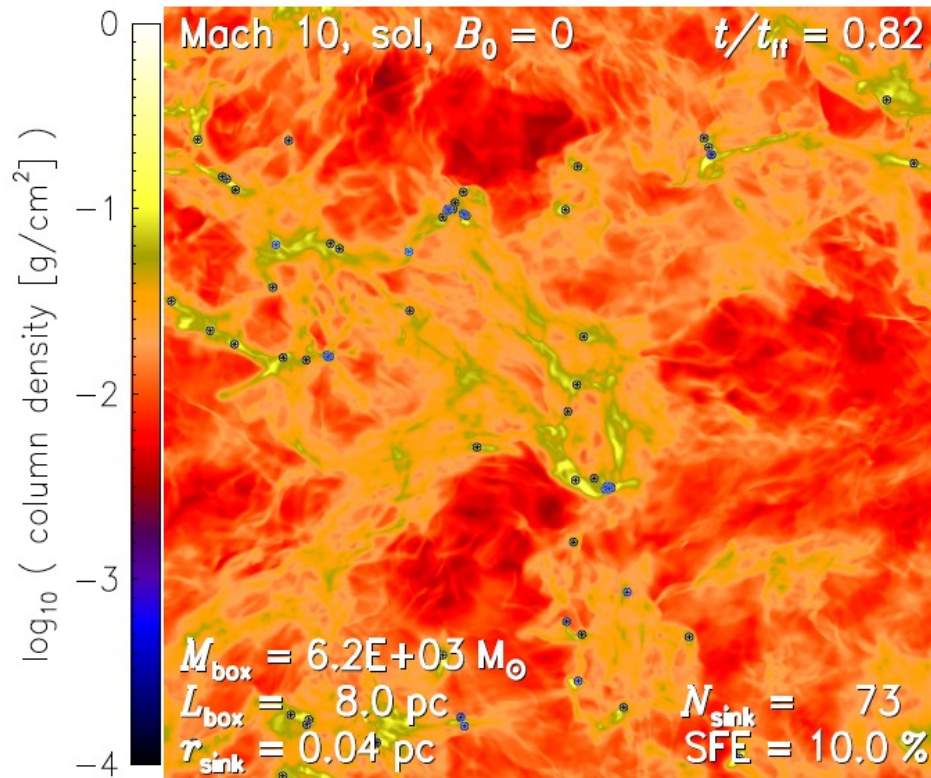


# Density Distribution → Star Formation Rate

## Numerical experiment for Mach 10

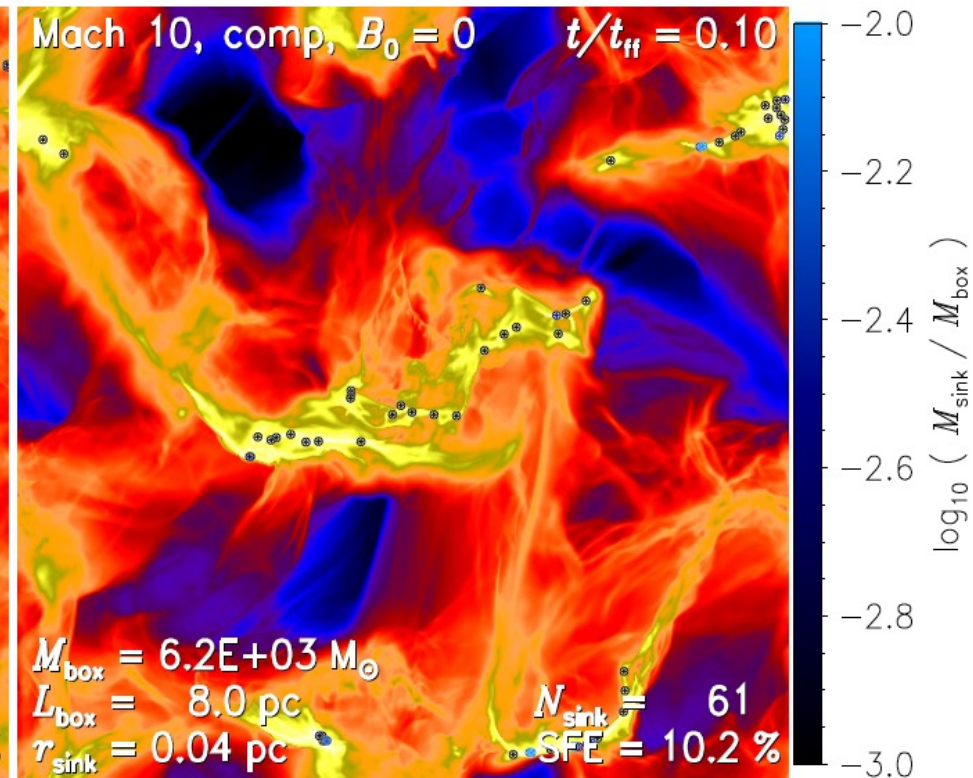
Movies available: <http://www.mso.anu.edu.au/~chfeder/pubs/sfr/sfr.html>

### Solenoidal Driving ( $b=1/3$ )



$SFR_{\text{ff}}$  (simulation) = 0.14  
 $SFR_{\text{ff}}$  (theory) = 0.15

### Compressive Driving ( $b=1$ )



x20  
x15

$SFR_{\text{ff}}$  (simulation) = 2.8  
 $SFR_{\text{ff}}$  (theory) = 2.3

**Turbulence driving is a key parameter for star formation!**



# Astrophysical Gas Dynamics

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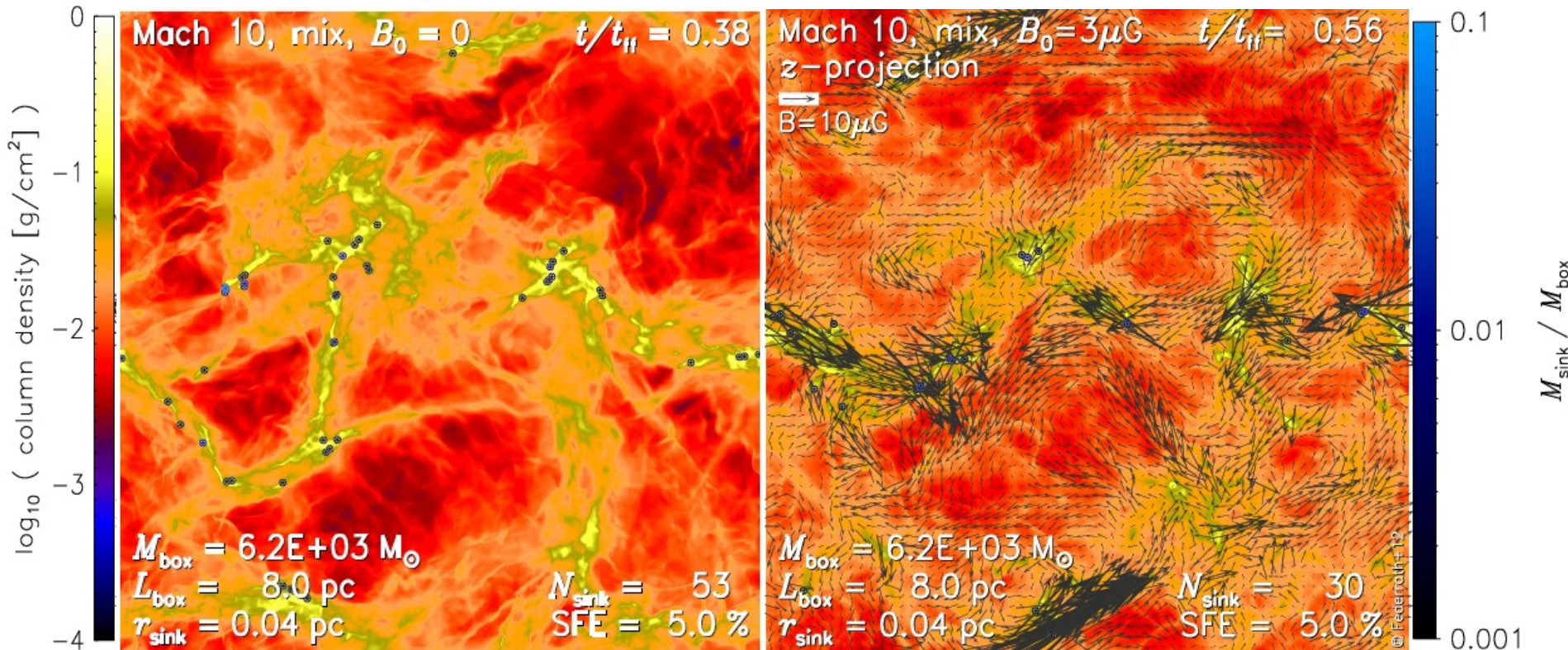
# The Star Formation Rate – Magnetic fields

## Numerical experiment for Mach 10 and $\alpha_{\text{vir}} \sim 1$

Movies available: <http://www.mso.anu.edu.au/~chfeder/pubs/sfr/sfr.html>

$B=0$  ( $M_A=\infty$ ,  $\beta=\infty$ )

$B=3\mu\text{G}$  ( $M_A=2.7$ ,  $\beta=0.2$ )



$\text{SFR}_{\text{ff}}$  (simulation) = **0.46**

**x0.63**

$\text{SFR}_{\text{ff}}$  (simulation) = **0.29**

$\text{SFR}_{\text{ff}}$  (theory) = **0.45**

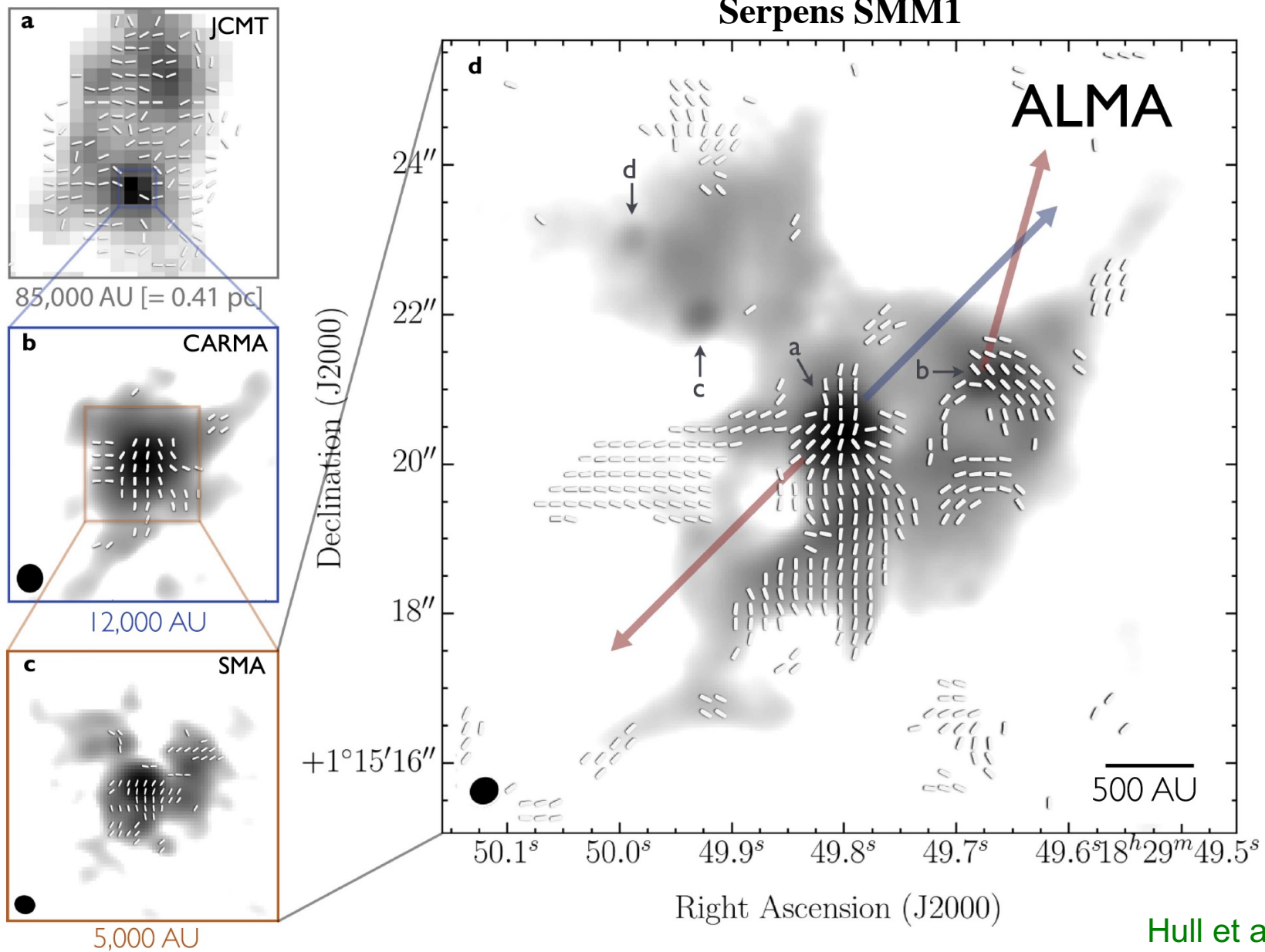
**x0.40**

$\text{SFR}_{\text{ff}}$  (theory) = **0.18**

Magnetic field reduces SFR and fragmentation (by factor 2) → **IMF**

Federrath & Klessen (2012)

# The role of magnetic field structure



# Magnetohydrodynamics (MHD)

Most gases in the Universe are electrically conductive.

For example:

- Stars are fully ionised.
- The interstellar medium has mostly neutral particles, but even a very small fraction of ions and electrons make the ISM an excellent conductor. What physical processes cause the small ionisation fraction ( $\sim 10^{-7}$ ) in molecular clouds?

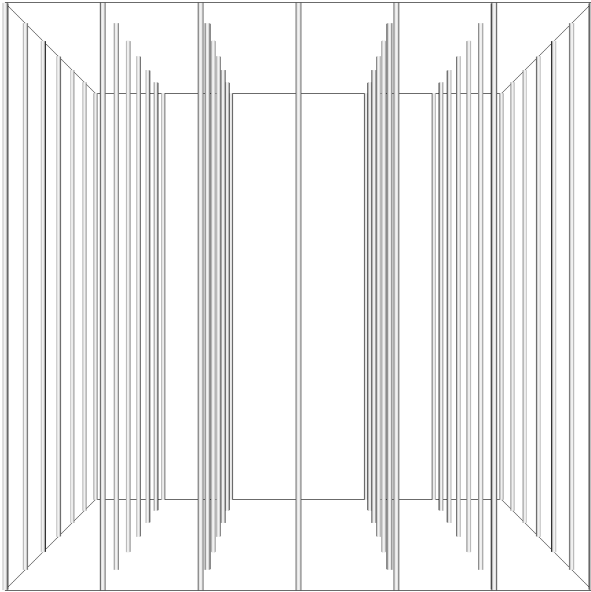
At first it may seem that one needs to treat ions, electrons and neutral particles all separately, because the Lorentz force only acts on the charged particles and depends on the charge. However, in the general approximation of hydrodynamics, namely that the mean free path is small compared to the system size (recall earlier discussion on the validity of the fluid approximation), collisions between neutrals, ions and electrons are so frequent that they can be treated together in a one-component (single fluid) approximation.

This theory is called MAGNETOHYDRODYNAMICS (MHD).

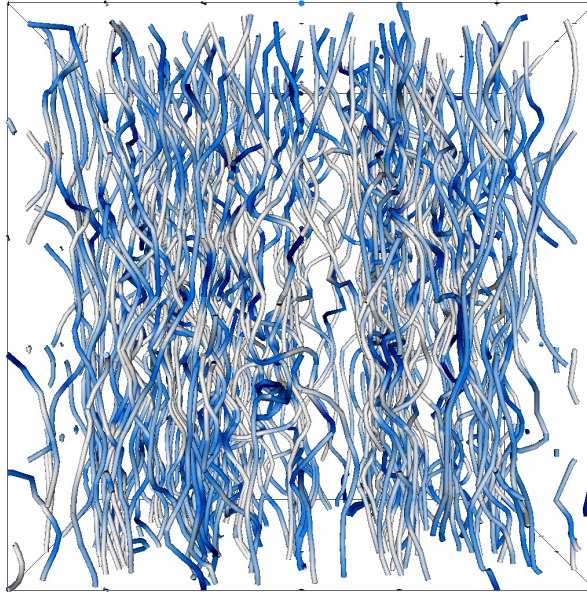


# The role of magnetic field structure

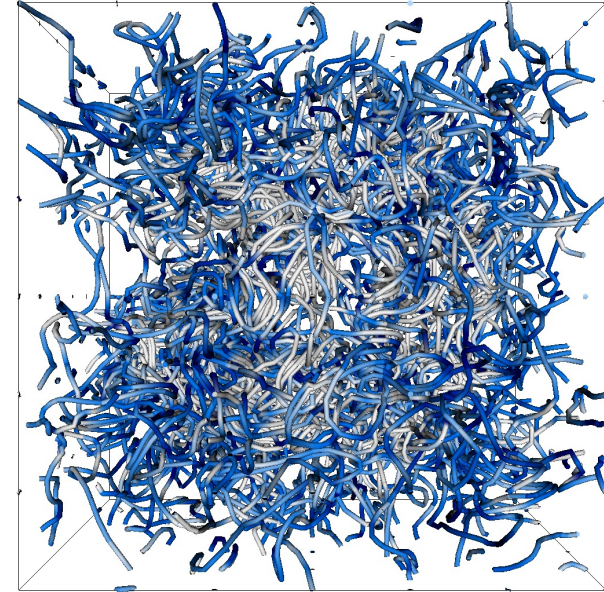
Uniform Magnetic Field



Partially Turbulent Field



Fully Turbulent Field



Gerrard et al. (2019)

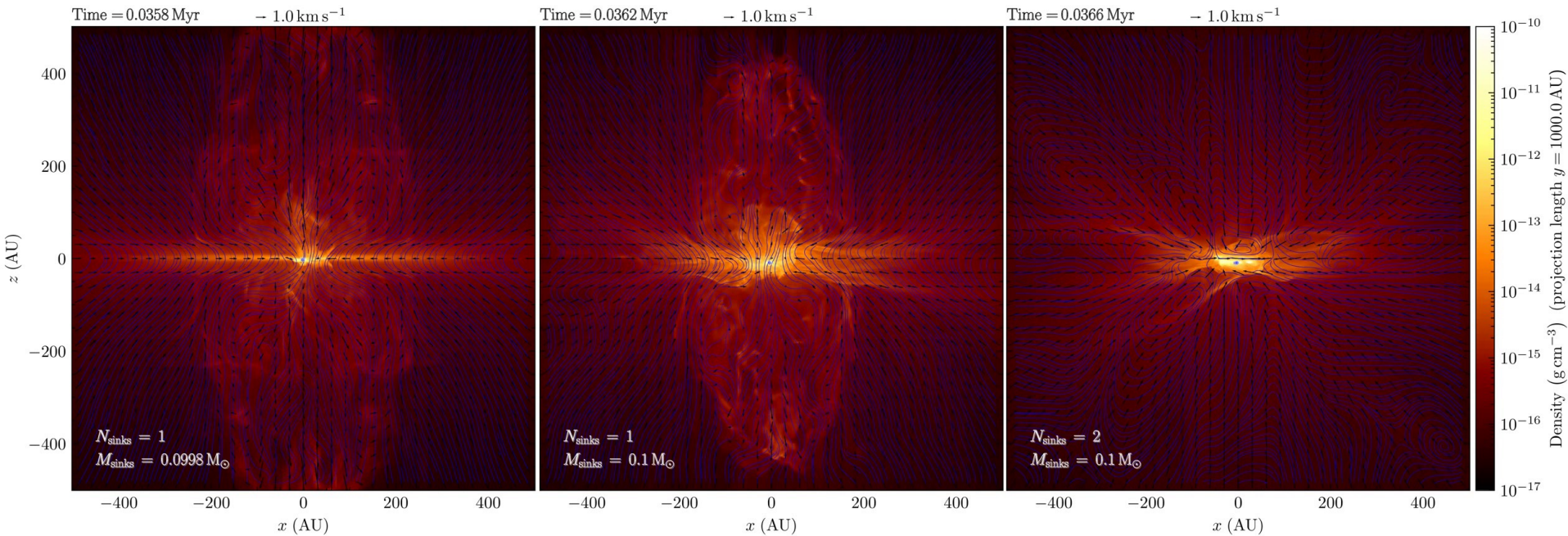
# The role of magnetic field structure for jet launching

Movies available: [https://www.mso.anu.edu.au/~chfeder/pubs/turb\\_b\\_jets/turb\\_b\\_jets.html](https://www.mso.anu.edu.au/~chfeder/pubs/turb_b_jets/turb_b_jets.html)

Uniform Magnetic Field

Partially Turbulent Field

Fully Turbulent Field



Gerrard et al. (2019)

→ Need ordered magnetic field component for jet launching

(Blandford & Payne 1982)



# Astrophysical Gas Dynamics

*NEXT TIME:*

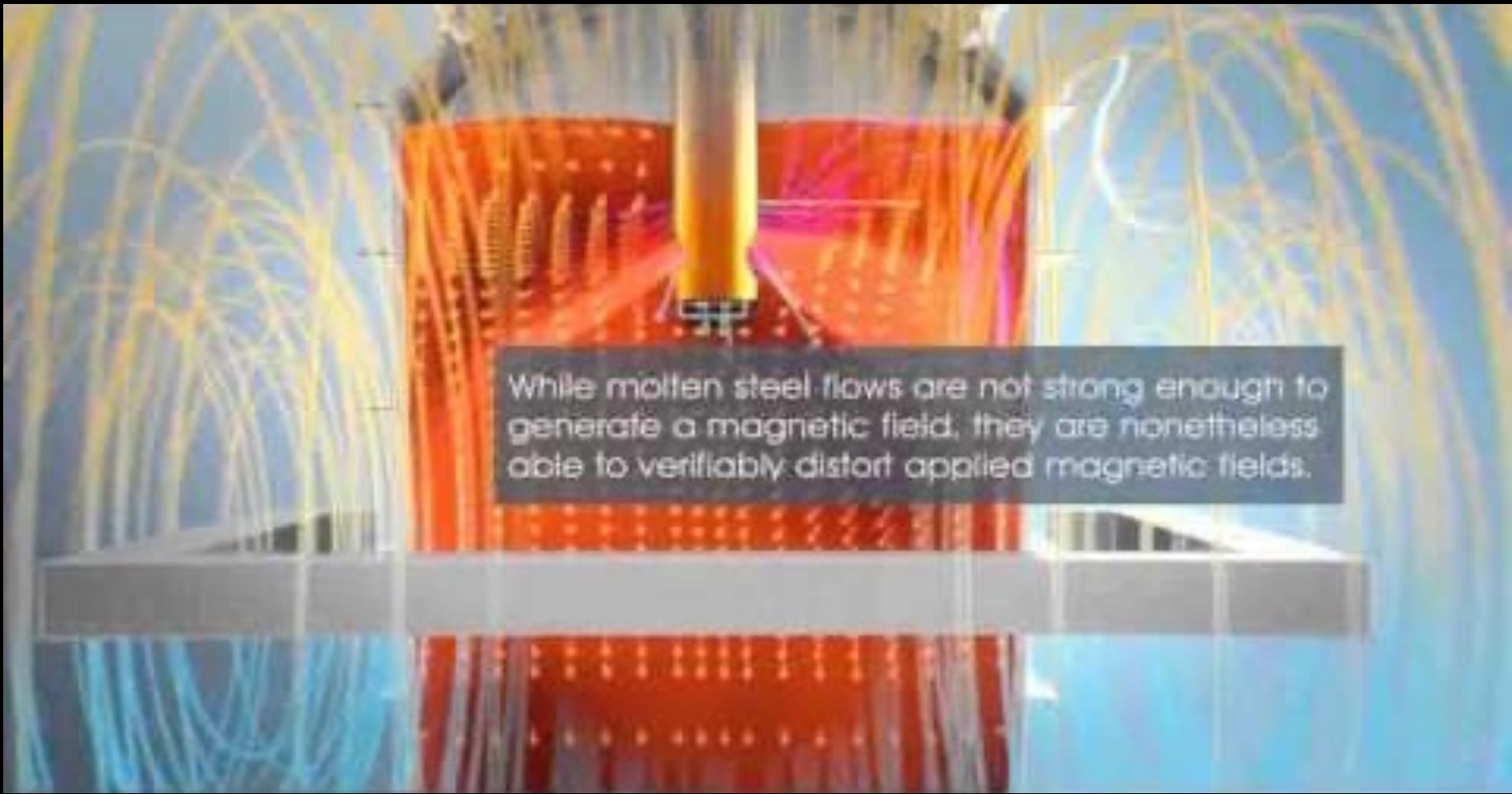
- *no course on Thursday (QEII day)*
- *then: more on MHD (pressure, tension, non-ideal MHD, PIC)*



# Astrophysical Gas Dynamics

Magnetohydrodynamics in the Cosmos and in the Lab

-- Magnetic fields „calm“ turbulent flows :-)



While molten steel flows are not strong enough to generate a magnetic field, they are nonetheless able to verifiably distort applied magnetic fields.