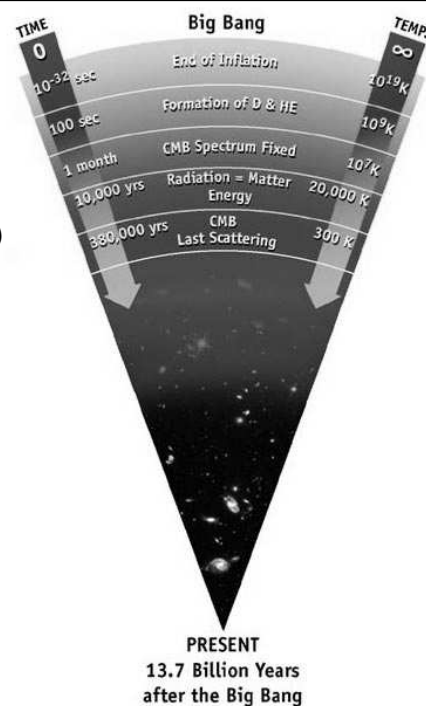


## WMAP CMB Conclusions

- *A flat universe with a scale-invariant spectrum of adiabatic Gaussian fluctuations, with re-ionization, is an acceptable fit to the WMAP data.*
- *The correlations of polarisation and the acoustic peaks imply the initial fluctuations were primarily adiabatic (the primordial ratios of dark matter/photons & baryons/photons do not vary spatially).*
- *The initial fluctuations are consistent with a Gaussian field, as expected from most inflationary models.*

## WMAP's cosmic timeline

- **CMB last scattering surface:**  
 $t_{\text{dec}} = 379 \pm 8 \text{ kyr}$  ( $z_{\text{dec}} = 1089 \pm 1$ )
- **Epoch of re-ionization:**  
 $t_r = 100 - 400 \text{ Myr}$  (95% c.l.)



## ***Large Scale Structure***

***With Thanks to Matthew Colless,  
leader of Australian side of 2dF  
redshift survey.***

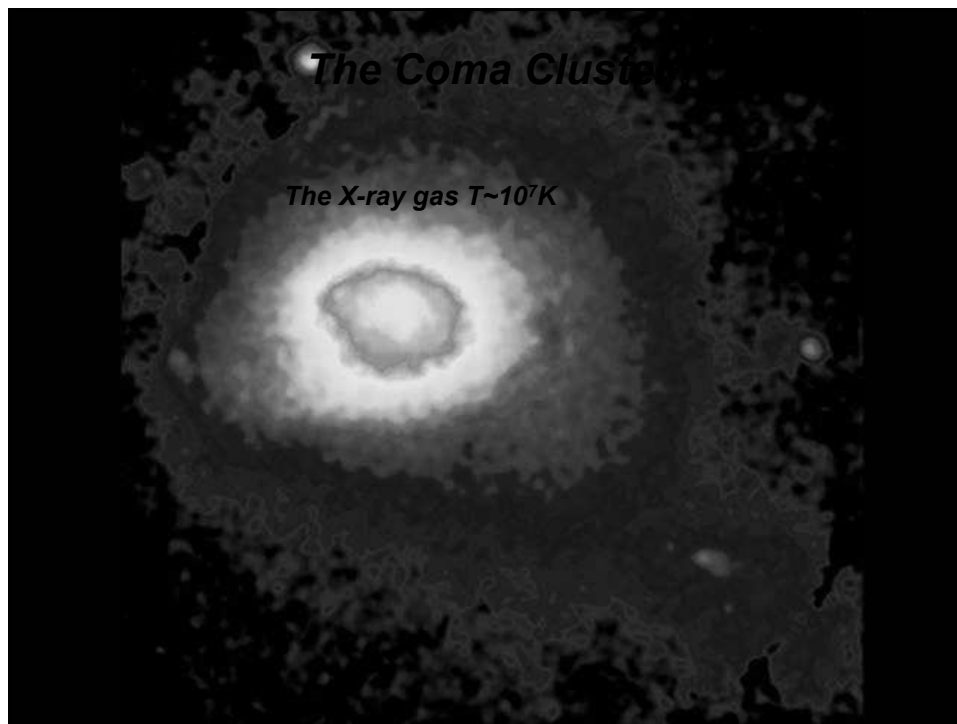


***The Local Group***

© Anglo-Australian Observatory

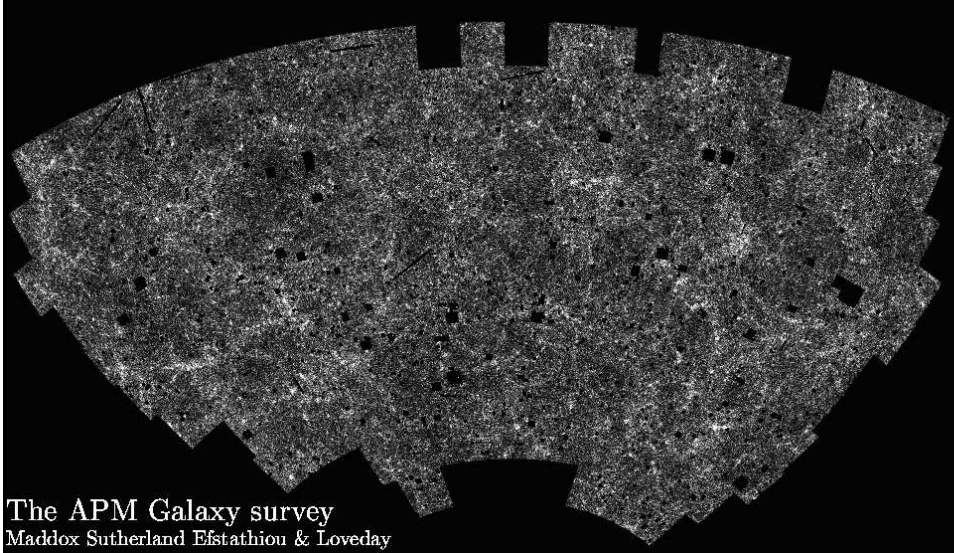
***The Hydra cluster***





## ***Large-scale structure in the local universe***

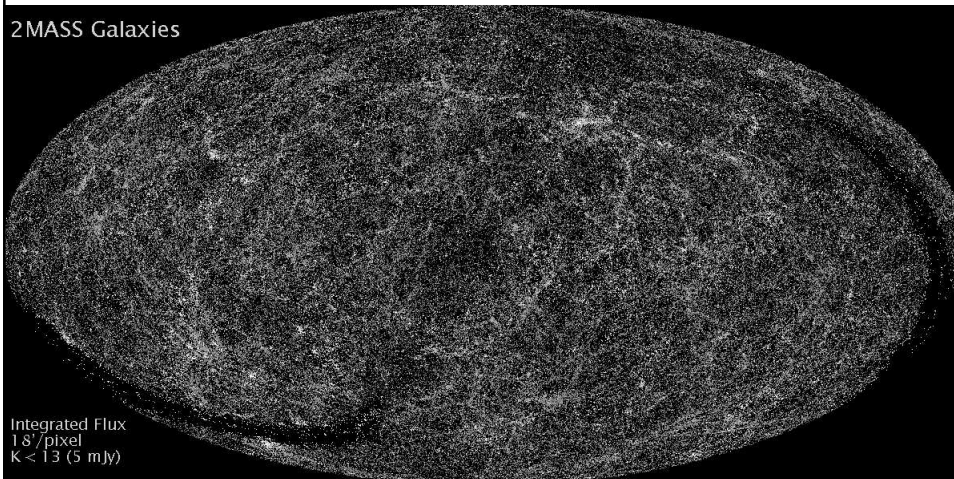
*Going deeper,  $2 \times 10^6$  optical galaxies over 4000 sq. deg.*



## ***Large-scale structure in the local universe***

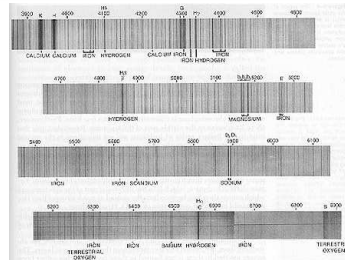
*The  $10^6$  near-infrared brightest galaxies on the sky*

2MASS Galaxies



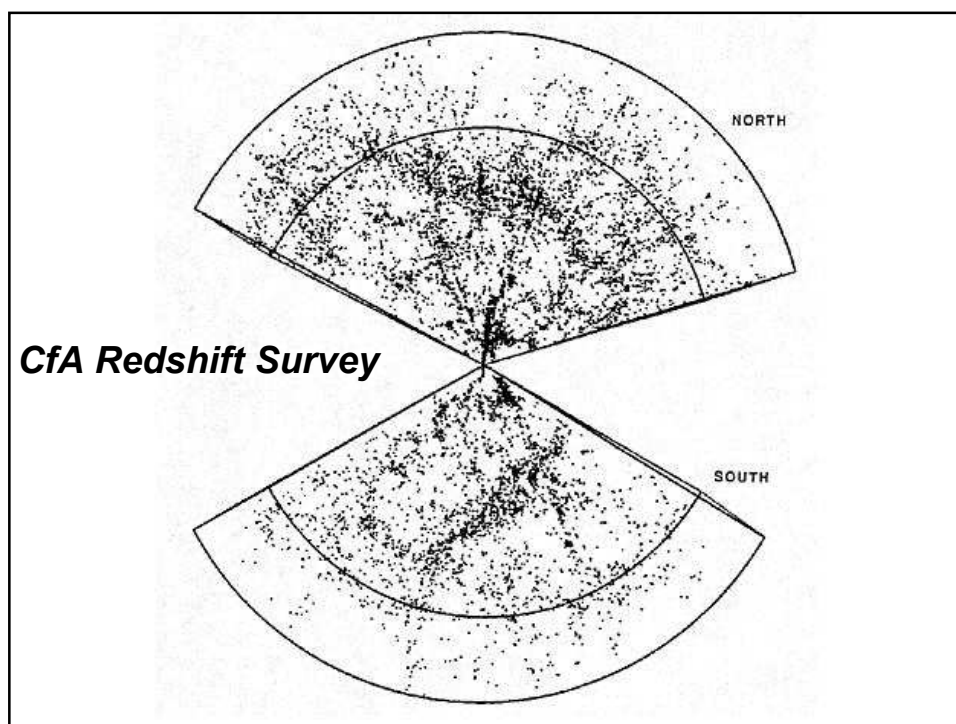
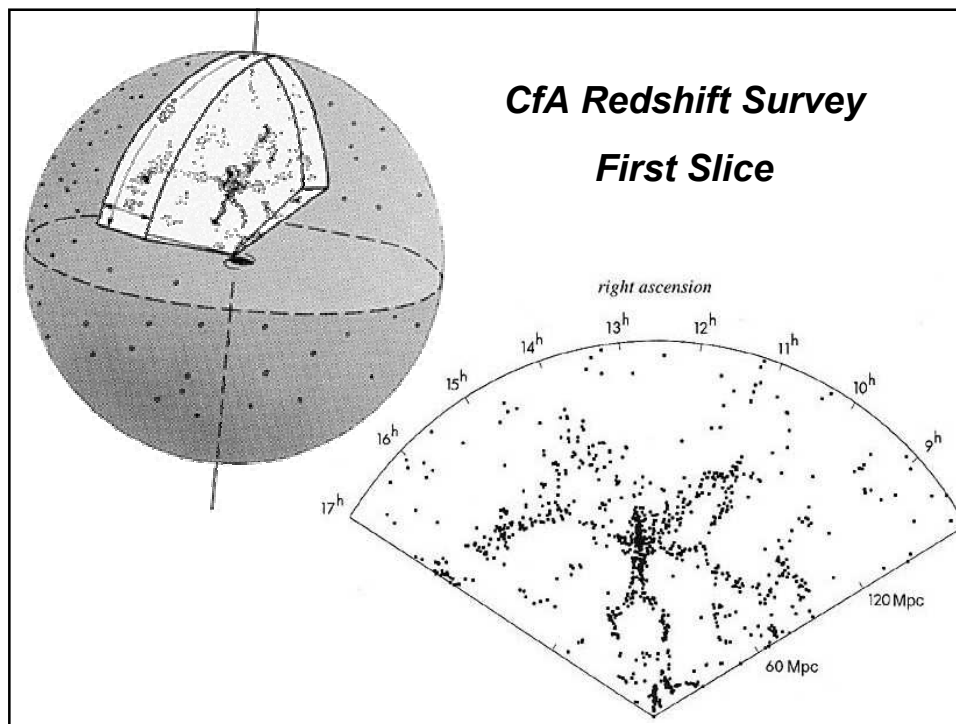
## Redshift surveys

- A z-survey is a systematic mapping of a volume of space by measuring redshifts:  $z = \lambda_1/\lambda_0 - 1 = a - 1$
- Redshifts as distance coordinates...  
 $H_0 D_L = c(z + (1 - q_0)z^2/2 + \dots)$   
*...this is the viewpoint in low-z surveys of spatial structure.*
- For low-z surveys of structure, the Hubble law applies:  
 $cz = H_0 d$  (for  $z \ll 1$ )
- For pure Hubble flow, redshift distance = true distance, i.e.  $s = r$ , where  $s$  and  $r$  are conveniently measured in km/s.
- But galaxies also have 'peculiar motions' due to the gravitational attraction of the surrounding mass field, so the full relation between z-space and real-space coordinates is :  
 $s = r + v_p \cdot r/r = r + v_p$  (for  $s \ll c$ )



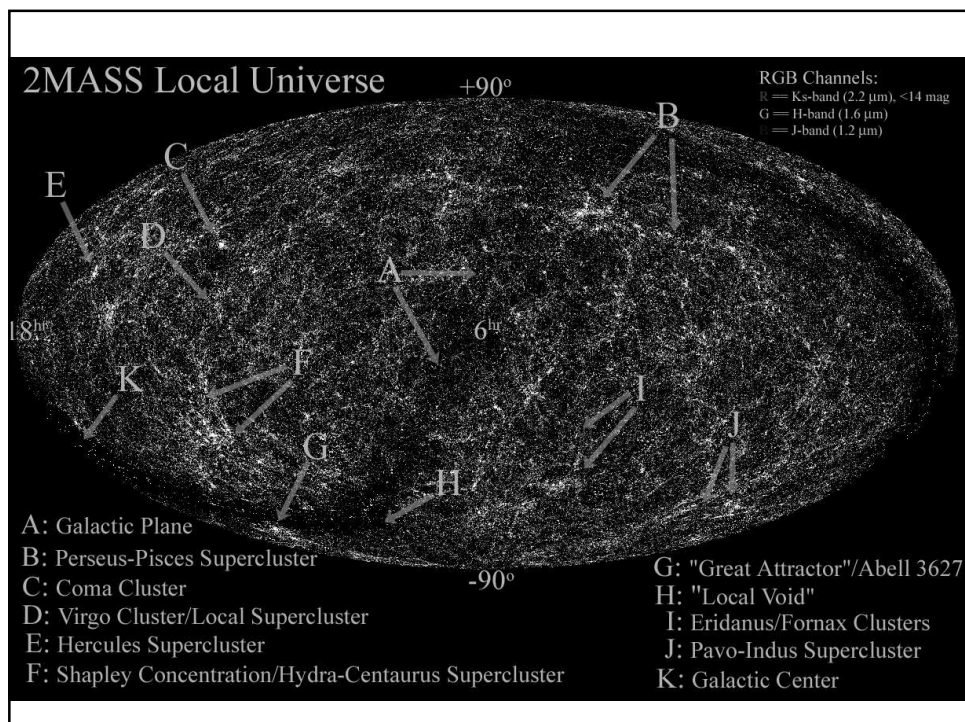
## Uses of z-surveys

- Three (partial) views of redshift:
  - $z$  measures the distance needed to map 3D positions
  - $z$  measures the look-back time needed to map histories
  - $cz - H_0 d$  measures the peculiar velocity needed to map mass
- Three main uses of z-surveys:
  - to map the large-scale structures, in order to...
    - do cosmography and chart the structures in the universe
    - test growth of structure through gravitational instability
    - determine the nature and density of the dark matter
  - to map the large-velocity field, in order to
    - 'see' the mass field through its gravitational effects
  - to probe the history of galaxy formation, in order to...
    - characterise the galaxy population at each epoch
    - determine the physical mechanisms by which the population evolves



## Cosmography

- **The main features of the local galaxy distribution include:**
  - **Local Group:** Milky Way, Andromeda and retinue.
  - **Virgo cluster:** nearest significant galaxy cluster, LG→Virgo.
  - **Local Supercluster (LSC):** flattened distribution of galaxies  $cz < 3000$  km/s; defines supergalactic plane (X,Y,Z).
  - **'Great Attractor':** LG/Virgo→GA, lies at one end of the LSC, (X,Y,Z)=(-3400,1500,±2000).
  - **Perseus-Pisces supercluster:** (X,Y,Z)=(+4500, ±2000,-2000), lies at the other end of the LSC.
  - **Coma cluster:** nearest very rich cluster, (X,Y,Z)=(0,+7000,0); a major node in the 'Great Wall' filament.
  - **Shapley supercluster:** most massive supercluster within  $z < 0.1$ , at a distance of 14,000 km/s behind the GA.
  - **Voids:** the Local Void, Sculptor Void, and others lie between these mass concentrations.
- **Yet larger structures are seen at lower contrast to  $>100 h^{-1}$  Mpc.**



## **Evolution of Structure**

- *The goal is to derive the evolution of the mass density field, represented by the dimensionless density perturbation:*  

$$\delta(\mathbf{x}) = \rho(\mathbf{x})/\langle\rho\rangle - 1$$
- *The framework is the growth of structures from 'initial' density fluctuations by gravitational instability.*
- *Up to the decoupling of matter and radiation, the evolution of the density perturbations is complex and depends on the interactions of the matter and radiation fields - 'CMB physics'*
- *After decoupling, the linear growth of fluctuations is simple and depends only on the cosmology and the fluctuations in the density at the surface of last scattering - 'large-scale structure in the linear regime'.*
- *As the density perturbations grow the evolution becomes non-linear and complex structures like galaxies and clusters form - 'non-linear structure formation'. In this regime additional complications emerge, like gas dynamics and star formation.*

## **The power spectrum**

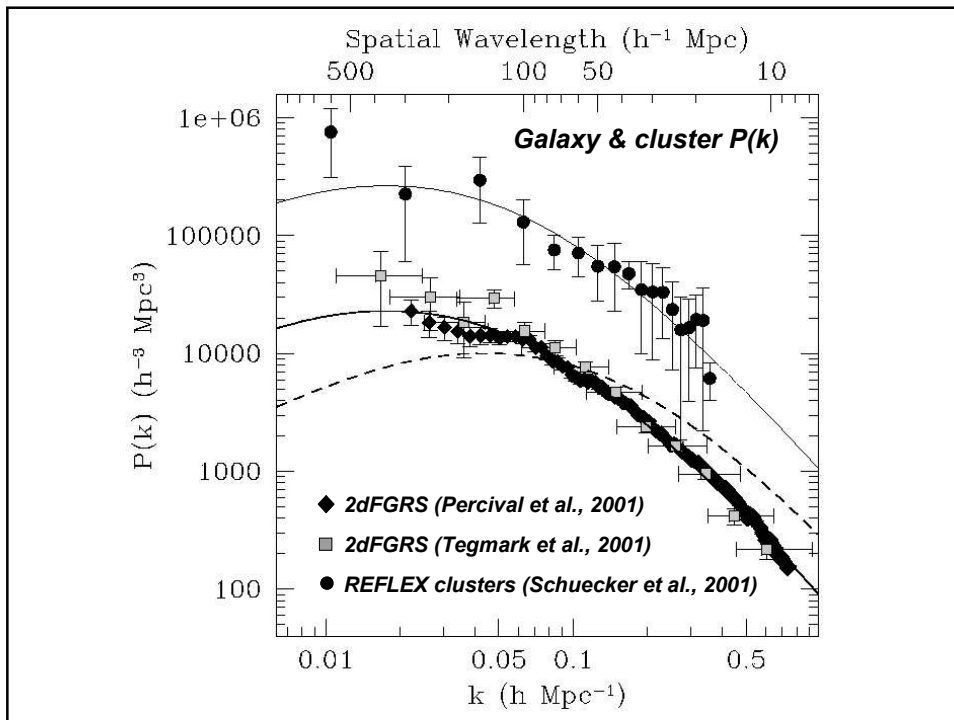
- *It is helpful to express the density distribution  $\delta(\mathbf{r})$  in the Fourier domain:*  

$$\delta(\mathbf{k}) = V^{-1} \int \delta(\mathbf{r}) e^{i\mathbf{k}\cdot\mathbf{r}} d^3\mathbf{r}$$
- *The power spectrum (PS) is the mean squared amplitude of each Fourier mode:*  

$$P(\mathbf{k}) = \langle |\delta(\mathbf{k})|^2 \rangle$$
  - *Note  $P(\mathbf{k})$  not  $P(k)$  because of the (assumed) isotropy of the distribution (i.e. scales matter but directions don't).*
  - *$P(k)$  gives the power in fluctuations with a scale  $r=2\pi/k$ , so that  $k=(1.0, 0.1, 0.01) \text{ Mpc}^{-1}$  correspond to  $r \approx (6, 60, 600) \text{ Mpc}$ .*
- *The PS can be written in dimensionless form as the variance per unit  $\ln k$ :*  

$$\Delta^2(k) = d\langle |\delta(\mathbf{k})|^2 \rangle / d\ln k = (V/2\pi)^3 4\pi k^3 P(k)$$
  - *e.g.  $\Delta^2(k) = 1$  means the modes in the logarithmic bin around wavenumber  $k$  have rms density fluctuations of order unity.*





## The correlation function

- The autocorrelation function of the density field (often just called 'the correlation function', CF) is:

$$\xi(r) = \langle \delta(x)\delta(x+r) \rangle$$

- The CF and the PS are a Fourier transform pair:

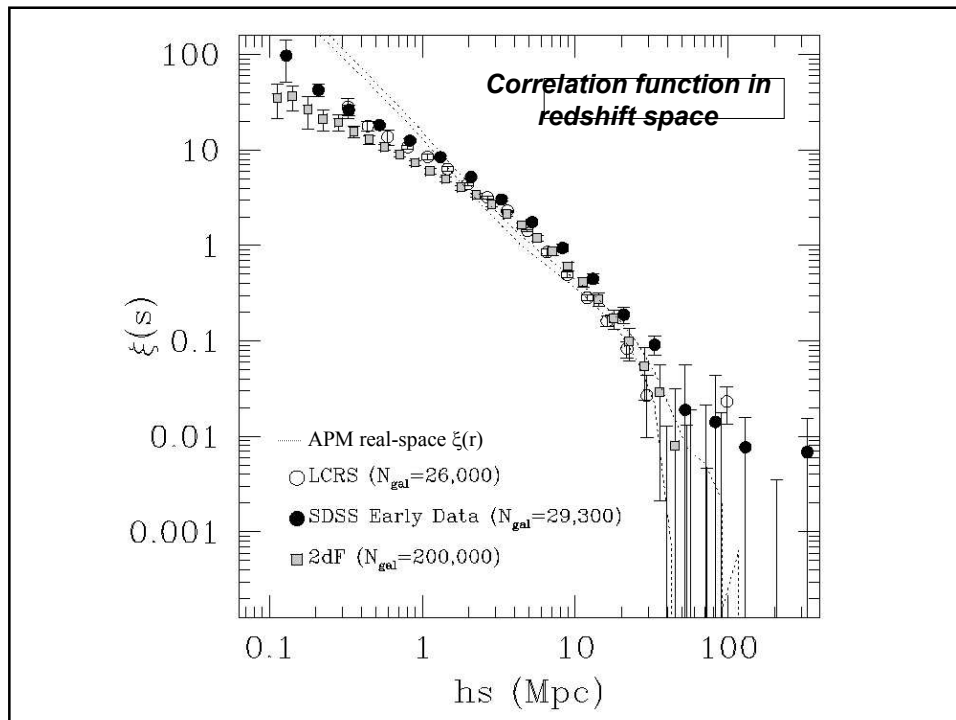
$$\begin{aligned} \xi(r) &= V/(2\pi)^3 \int |\delta_k|^2 \exp(-ik \cdot r) d^3k \\ &= (2\pi^2)^{-1} \int P(k) [(\sin kr)/kr] k^2 dk \end{aligned}$$

- Because  $P(k)$  and  $\xi(r)$  are a Fourier pair, they contain precisely the same information about the density field.

- When applied to galaxies rather than the density field,  $\xi(r)$  is often referred to as the 'two-point correlation function', as it gives the excess probability (over the mean) of finding two galaxies in volumes  $dV$  separated by  $r$ :

$$dP = \rho_0^2 [1 + \xi(r)] d^2V$$

- By isotropy, only separation  $r$  matters, and not the vector  $r$ .
- Can thus think of  $\xi(r)$  as the mean over-density of galaxies at distance  $r$  from a random galaxy.



## Gaussian fields

- **A Gaussian density field has the property that the joint probability distribution of the density at any number of points is a multivariate Gaussian.**
- **Superposing many Fourier density modes with random phases results, by the central limit theorem, in a Gaussian density field.**
- **A Gaussian field is fully characterized by its mean and variance (as a function of scale).**
- **Hence  $\langle \rho \rangle$  and  $P(k)$  provide a complete statistical description of the density field if it is Gaussian.**
- **Most simple inflationary cosmological models predict that Fourier density modes with different wavenumbers are independent (i.e. have random phases), and hence that the initial density field will be Gaussian.**
- **Linear amplification of a Gaussian field leaves it Gaussian, so the large-scale galaxy distribution should be Gaussian.**

## ***The initial power spectrum***

- *Unless some physical process imposes a scale, the initial PS should be scale-free, i.e. a power-law,  $P(k) \propto k^n$ .*
- *The index  $n$  determines the balance between large- and small-scale power, with rms fluctuations on a mass scale  $M$  given by:*  
$$\delta_{\text{rms}} \propto M^{-(n+3)/6}$$
- *The 'natural' initial power spectrum is the power-law with  $n=1$  (called the Zel'dovich, or Harrison-Zel'dovich, spectrum).*
- *The  $P(k) \propto k^1$  spectrum is referred to as the scale-invariant spectrum, since it gives variations in the gravitational potential that are the same on all scales.*
- *Since potential governs the curvature, this means that space-time has the same amount of curvature variation on all scales (i.e. the metric is a fractal).*
- *In fact, inflationary models predict that the initial PS of the density fluctuations will be approximately scale-invariant.*