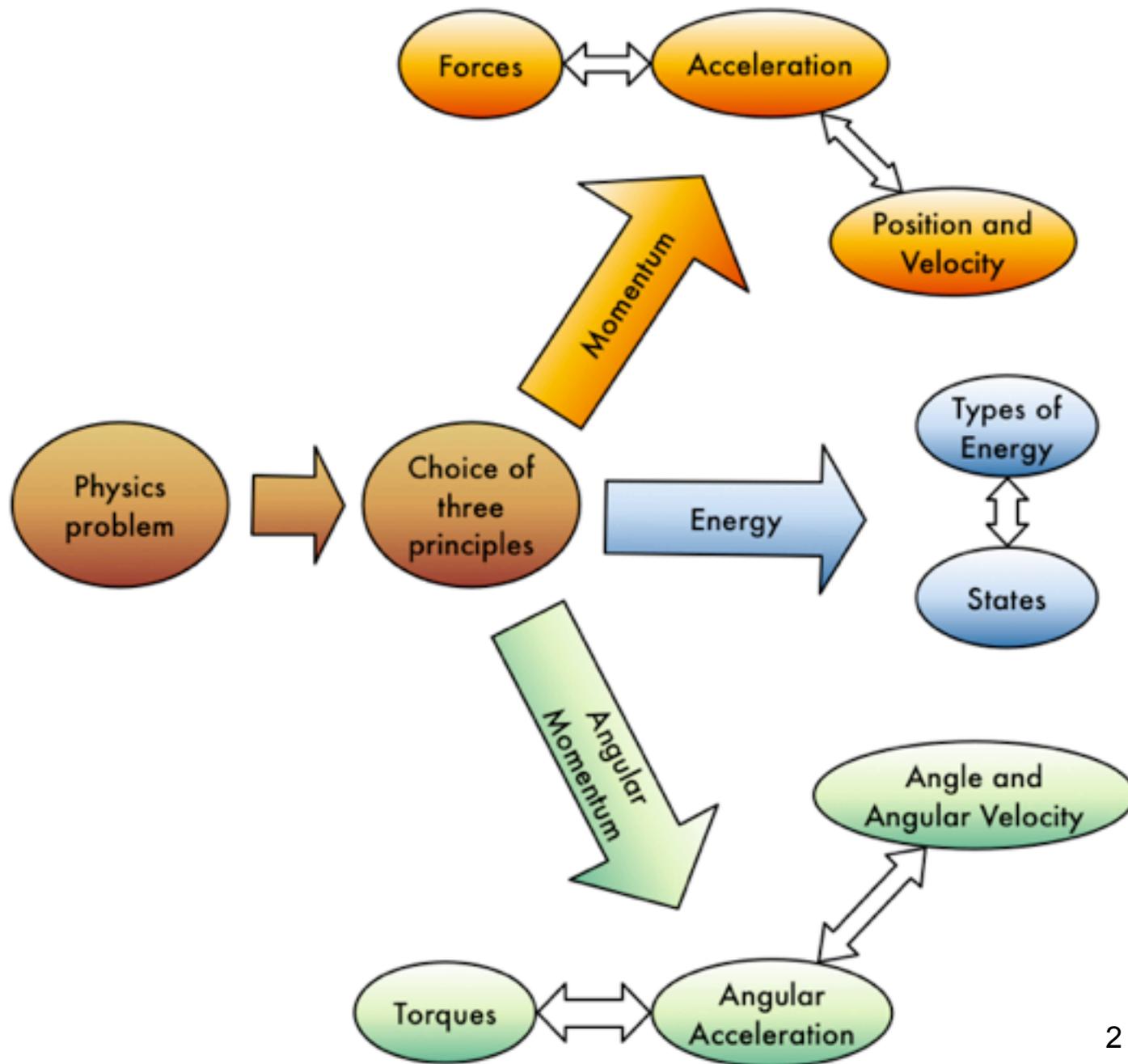


# Energy



# Energy Equations

- Energy  $E$  is a scalar. The energy of an object is given by  $E^2 = p^2 c^2 + m_0^2 c^4$

where  $p$  is the momentum,  $m_0$  the rest mass and  $c$  the speed of light.

There is also (potential) energy in fields such as gravitational or electric fields:

$$E = \frac{Gm_1m_2}{r} + \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r}$$

In a given collection of objects (a system), energy is conserved unless an external force  $f$  is applied to this system, in which case the change in energy of the system is:

$$\frac{dE}{dt} = \vec{v} \cdot \vec{F}$$

The dot is the vector dot product

# That's actually all you need to know

- But now we'll talk about what it actually means...

# Energy

- The basic principle is very familiar - things don't do stuff without energy.
- Energy can take many forms, and change from one to another, but it is always conserved and you can't get it for nothing.
- This can sometimes let you solve seemingly impossible problems with the greatest of ease

# Impossible without details

- You don't get something for nothing
- Perpetual motion machines can't exist.
- If you see something doing stuff, there must be an energy source hidden somewhere.
- If you don't have enough energy, no matter what, you can't do something.

# For example

- “All this talk of space travel is utter bilge”, Professor Woolley, ANU, 1956
- Launch of Sputnik 1, 1957
- Argument - the energy liberated by a kilogram of TNT is less than the energy needed to lift one kilogram into space.
- So the most explosive materials known cannot lift even themselves into space.

# What's wrong with this?

# Two things

- You can get much more energy per unit weight from things like petrol compared to explosives - the explosives have less energy, but liberate it faster.
- You can burn tones of fuel to get 1kg of payload into space - most of the fuel is burned low down.



- <http://www.youtube.com/watch?v=wvWHnK2FiCk>

# Energy

- Throw a ball into the audience
- Let's see what you know.
- Write down on a scrap of paper what is going on with energy while a ball is thrown across the classroom.

Less kinetic energy  
and more gravitational  
potential energy



Back to Kinetic  
energy, mostly  
in the ball but a  
bit in air  
currents

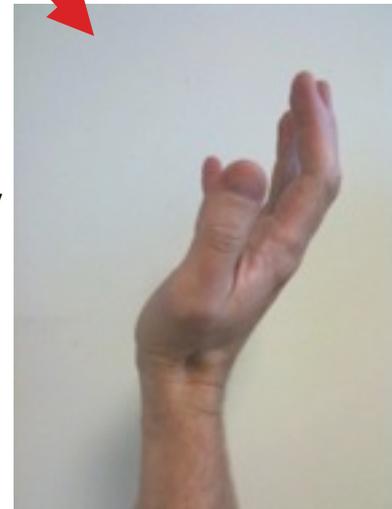
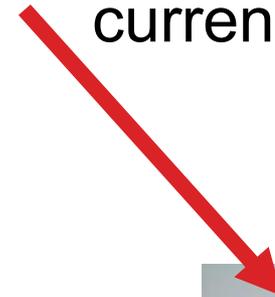
Kinetic energy



Chemical  
energy in my  
muscles



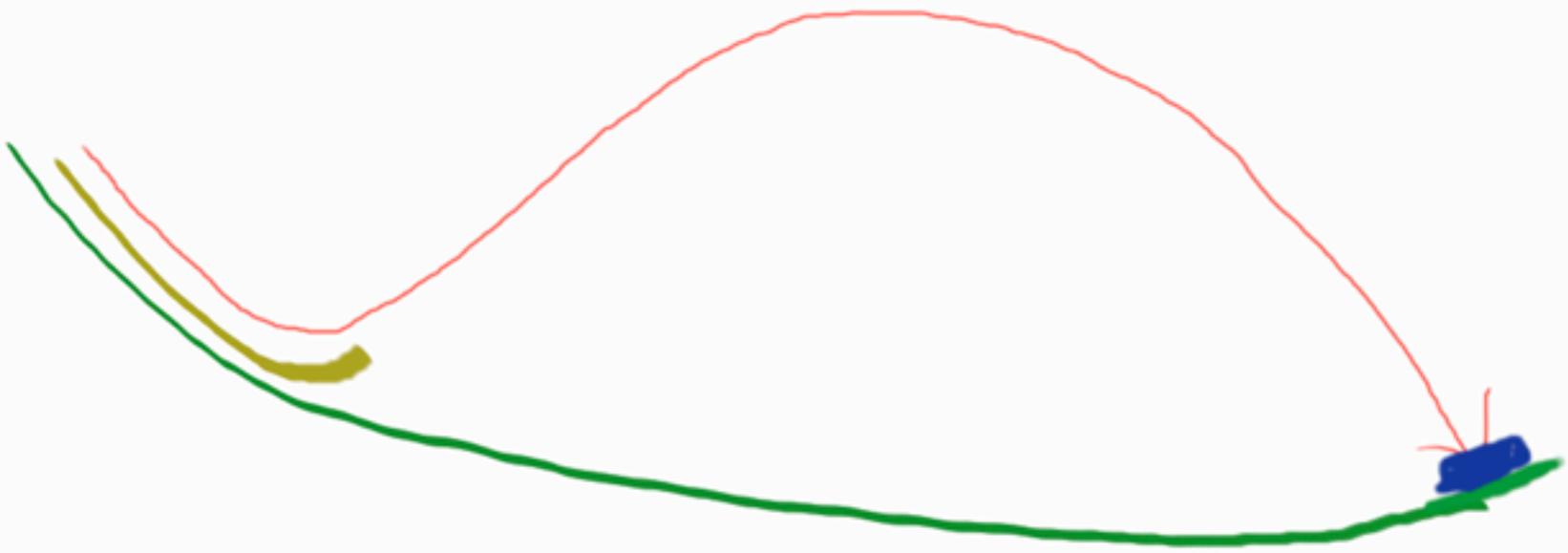
Heat energy in  
the ball and my  
hand. Maybe  
some sound  
energy?



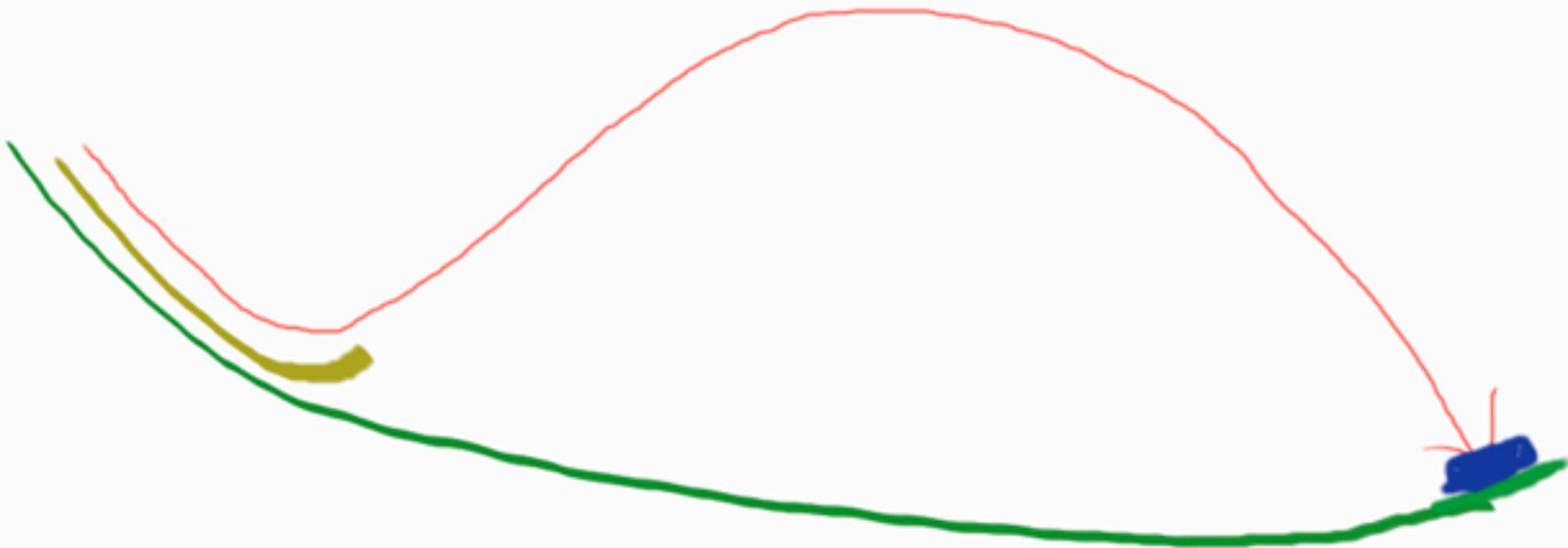
# Is this plausible?



# On energy grounds alone...



# Not plausible



He goes higher at the peak than at the start. Where did the energy for this come from?



# Maths behind this?

- The chemical energy is really hard to measure (at least without dissecting you followed by a cell-by-cell chemical analysis)
- But you can work out how much energy you used using the law of conservation of energy.
- The kinetic energy in the ball must have come from your muscles.
- And your arm probably warmed up a bit from the exercise.
- Add this heat energy to the kinetic energy and that's how much chemical energy you must have used.

# Kinetic energy

- The true energy of a moving object is given by:  $E^2 = p^2 c^2 + m_0^2 c^4$

If you set the momentum  $P$  to zero (i.e. the ball isn't moving), you get:  $E^2 = m_0^2 c^4$

Take the square root of this, and you get an equation you may recognize:

$$E = m_0 c^2$$

# Relativity

- Relativity (covered in PHYS1201) tells us that matter and energy are the same thing.
- The true energy equation takes this into account - even a stationary ball has lots of energy (you multiply the mass in kg by the velocity of light squared...)
- But in most everyday situations you don't need to worry about this - you can ignore this rest-mass energy and just look at the *change* in energy due to the motion.
- If the speed of an object is much less than the speed of light, you can approximate this using another familiar equation:

$$KE = \frac{1}{2}mv^2$$

# Kinetic and potential energy

- So if you know how fast the ball was moving when it left my hand, you can work out the kinetic energy.
- But as it moves higher into the air, it will slow down.
- Energy has been lost by the ball, and gained by the gravitational field of the Earth. This is called Potential Energy.

# Potential Energy

- The true equation for gravitational potential energy (well, almost - it does need some corrections for General Relativity which I won't go into here) is:

$$E = \frac{-GMm}{r}$$

where  $M$  in this case would be the mass of the Earth, and  $m$  the mass of the ball (or vice versa - it makes no difference).  $r$  is distance between the centre of the ball and the centre of the Earth.

# Approximation

- You can use that full equation -  $r$  might start off at 6400 km and go to 6400.005 km.
- But over this small range in  $r$  (the distance to the centre of the Earth), you can use a simpler approximate form of the potential energy equation:

$$PE = mgh$$

Where  $h$  is the height,  $m$  the mass of the ball, and  $g = 9.8 \text{ m s}^{-2}$ .

# Straight up?

- If I threw it straight up, all the kinetic energy would turn into potential energy for a moment when it's at the top of its arc.
- So you could work out how high it would go, using conservation of energy.
- The Kinetic energy when it leaves my hand must equal the potential energy at the top of its motion.

$$\frac{1}{2}mv^2 = mgh$$

Cancel  $m$

$$\frac{1}{2}v^2 = gh$$

Divide both sides by  $g$ , and write it down backwards

$$h = \frac{1}{2} \frac{v^2}{g}$$

# Other forms of energy

- Energy in a spring:  $E = \frac{1}{2}kD^2$
- where  $k$  is the spring constant and  $D$  the distance by which the spring is extended or compressed.
- Rotational Energy:  $E = \frac{1}{2}I\omega^2$
- where  $I$  is the moment of inertia and  $\omega$  is the angular velocity

# General Procedure

- Pick states (like beginning and end)
- Write down all the various forms of energy at each state
- Set them equal to each other
- Solve for whatever it is you want to know.